



The presentation will start at:

**13:00:00**

The current time is:

**13:00:42**

Central Standard Time, UTC-6

# Probabilistic Reasoning with Bayesian Networks and BayesiaLab

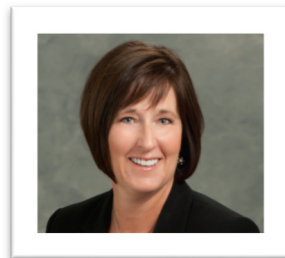
# Introduction

## Your Hosts Today

- Stefan Conrady  
[stefan.conrady@bayesia.us](mailto:stefan.conrady@bayesia.us)



- Stacey Blodgett  
[stacey.blodgett@bayesia.us](mailto:stacey.blodgett@bayesia.us)



# Today's Agenda

## Motivation & Background

- Logic vs. Probabilistic Reasoning

## Examples of Probabilistic Reasoning

- Example 1: What color is the taxi?
- Bayesian Networks to the Rescue!
- Knowledge Encoding & Inference with Bayesian Networks & BayesiaLab
- Example 2: Where is my bag?

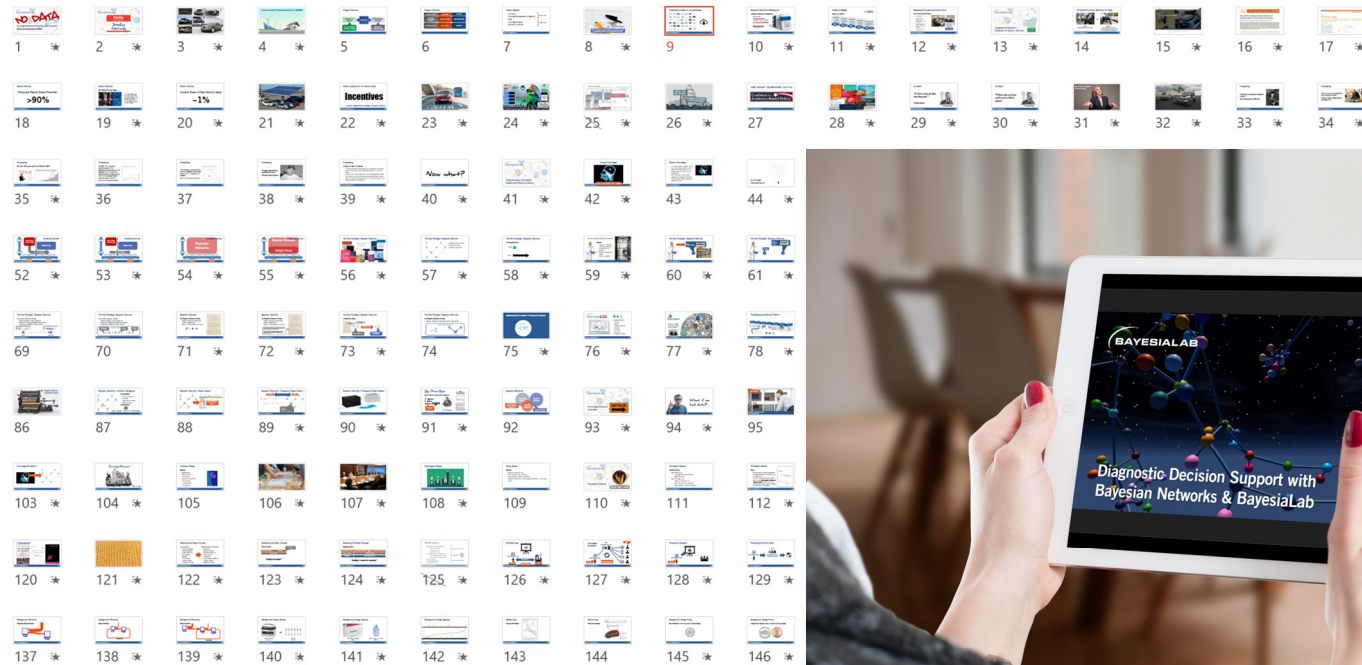


10 min.



50 min.

# Webinar Slides & Recording Available

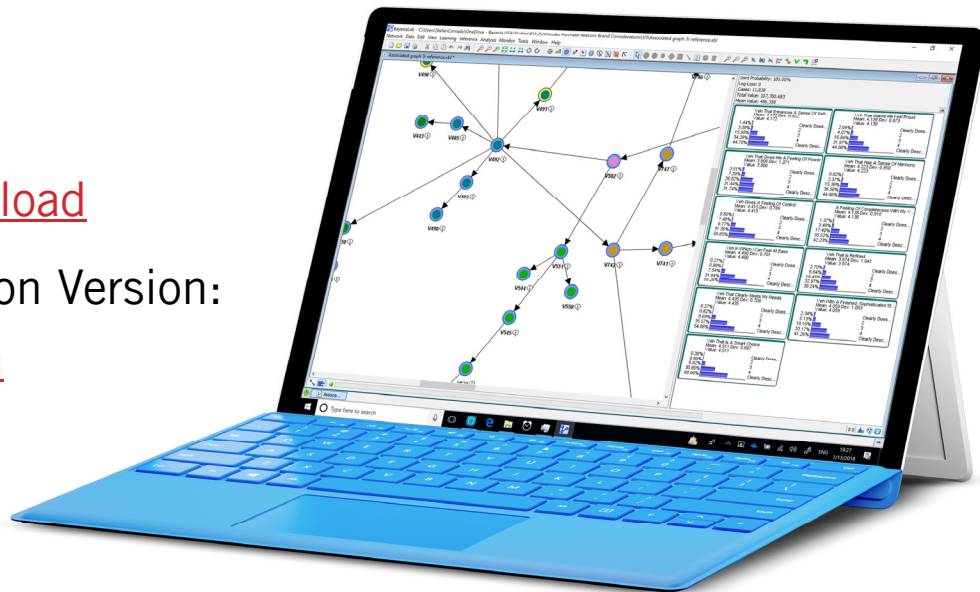




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# Questions



File View Help

Audio

Sound Check [Signal Icon] ?

☒ Computer audio  
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**MUTED**

Microphone (Pro 9000) [Dropdown Arrow]

[Volume Bar]

DELL U3415W (Intel(R) Display... [Dropdown Arrow]

Questions

Q: How do I choose from the available discretization algorithms?

[Send]

**Webinar Now**  
Webinar ID: 256-442-531

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**Latest New Top**

 **Webinar on Diagnostic Decision Support with Bayesian Networks**  
a minute ago by [stefanconrady](#): The answers to all webinar questions will be posted here.

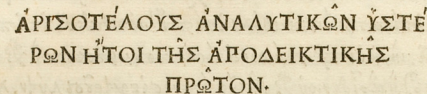
💬 0 👍 0 👁 0  
Started by [stefanconrady](#) a minute ago

🌐 English ▾



# Motivation & Background: Reasoning

## Aristotle (384-322 BC)





# Deductive Logic

## Limitations of Logic

- “Classical logic has no explicit mechanism for representing the degree of certainty of premises in an argument, nor the degree of certainty in a conclusion, given those premises.”

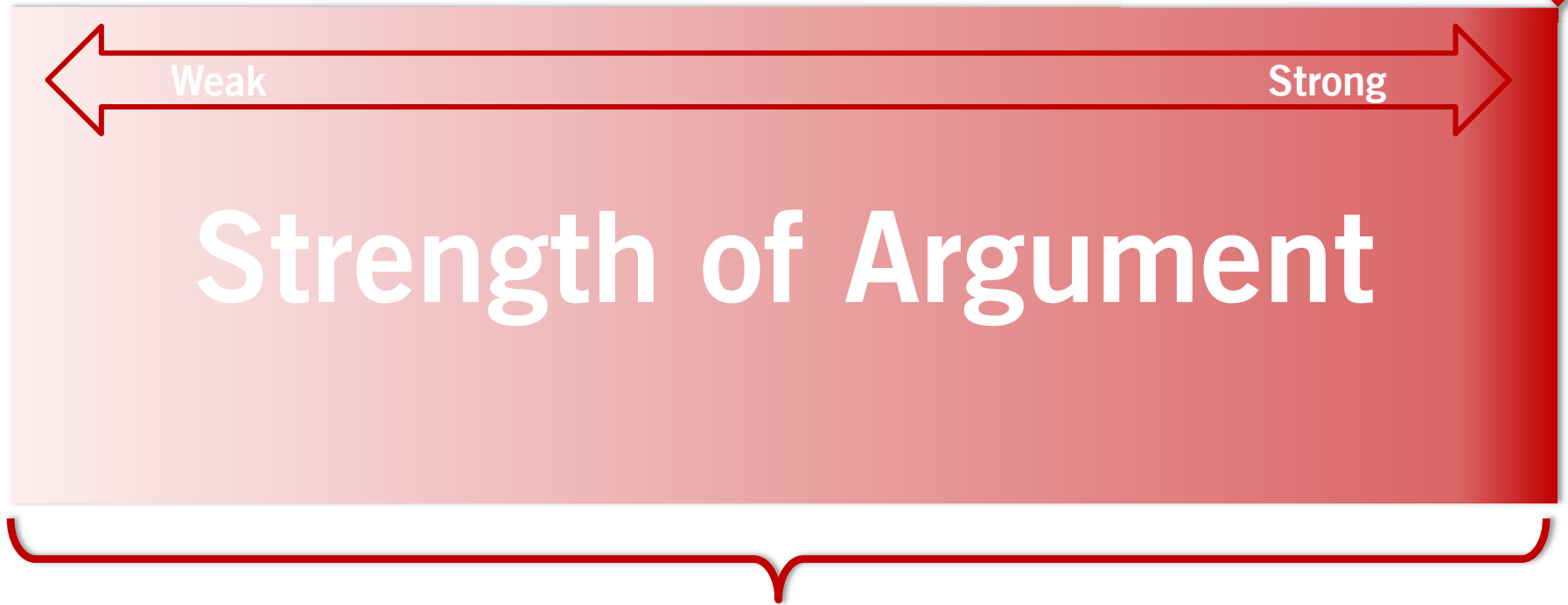
*Source: J. Williamson, Handbook of the Logic of Argument and Inference: The Turn Toward the Practical*

**LOGIC IS NOT ENOUGH!**



# Inductive vs. Deductive Logic

Formal Deductive Logic



Inductive Logic = Probabilistic Reasoning

# 2000 YEARS LATER...

## Bayes' Theorem for Conditional Probabilities

$H$ : Hypothesis

$E$ : Evidence

$$P(H | E) = \frac{P(E | H)P(H)}{P(E)}$$

“Probability of  
H given E”



*T. Bayes.*

## 1763 PHILOSOPHICAL TRANSACTIONS

[ 37° ]

quodque solum, certa nitri signa præbere, sed plura  
concurrere debere, ut de vero nitro producto dubium  
non relinquatur.

LII. *An Essay towards solving a Problem in  
the Doctrin of Chances. By the late Rev.  
Mr. Bayes, F. R. S. communicated by Mr.  
Price, in a Letter to John Canton, A. M.  
F. R. S.*

Dear Sir,

Read Dec. 23, 1763. I Now send you an essay which I have

found among the papers of our deceased friend Mr. Bayes, and which, in my opinion, has great merit, and well deserves to be preserved. Experimental philosophy, you will find, is nearly interested in the subject of it; and on this account there seems to be particular reason for thinking that a communication of it to the Royal Society cannot be improper.

He had, you know, the honour of being a member of that illustrious Society, and was much esteemed by many in it as a very able mathematician. In an introduction which he has writ to this Essay, he says, that his design at first in thinking on the subject of it was, to find out a method by which we might judge concerning the probability that an event has to happen, in given circumstances, upon supposition that we know nothing concerning it but that, under the same circum-

# Probabilistic Reasoning

## Mathematical Formulation of Inductive Reasoning

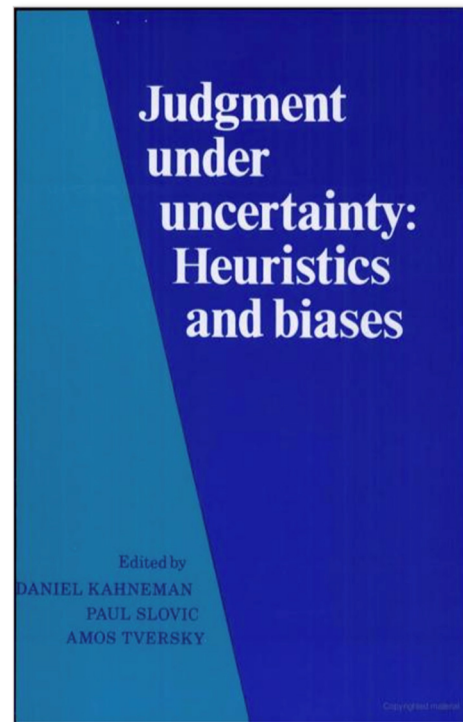
- “Bayesian inference is important because it provides a **normative and general-purpose procedure for reasoning under uncertainty.**”

*Source: Inductive Reasoning: Experimental, Developmental, and Computational Approaches, edited by Aidan Feeney and Evan Heit*



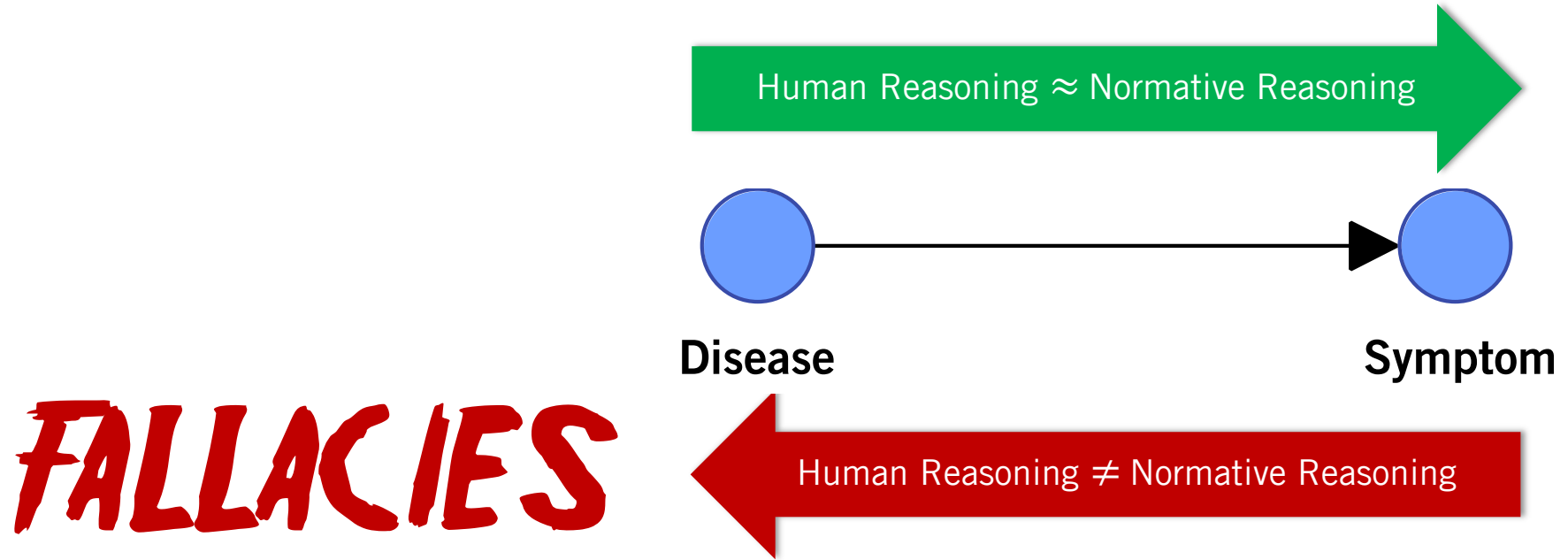
# Probabilistic Reasoning

Human reasoning  
is flawed!



# Why is this so important?

## Human Cognitive Limitations and Biases Under Uncertainty



# 250 Years Later...

- “...despite the mathematization of probability in the Enlightenment, mathematical probability theory remains, to this very day, entirely unused in criminal courtrooms, when evaluating the ‘probability’ of the guilt of a suspected criminal.”

*James Franklin, The Science of Conjecture:  
Evidence and Probability before Pascal,  
2001 The Johns Hopkins Press*

THE  
DOCTRINE  
OF  
CHANCES:  
OR,

A METHOD of Calculating the Probabilities  
of Events in PLAY.

---

THE THIRD EDITION,  
*Fuller, Clearer, and more Correct than the Former.*

---

By A. DE MOIVRE,  
*Fellow of the ROYAL SOCIETY, and Member of the ROYAL ACADEMIES  
OF SCIENCES of Berlin and Paris.*



LONDON:  
Printed for A. MILLAR, in the Strand.  
MDCCLVI.



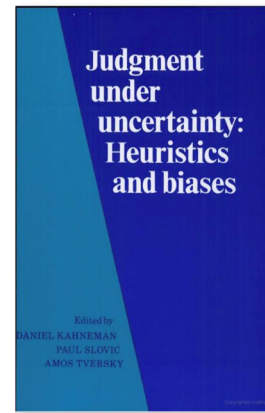


# Example 1: What Color is the Taxi?

Knowledge Modeling & Reasoning Under Uncertainty

# What Color is the Taxi?

\*adapted from  
Kahneman &  
Tversky, 1980



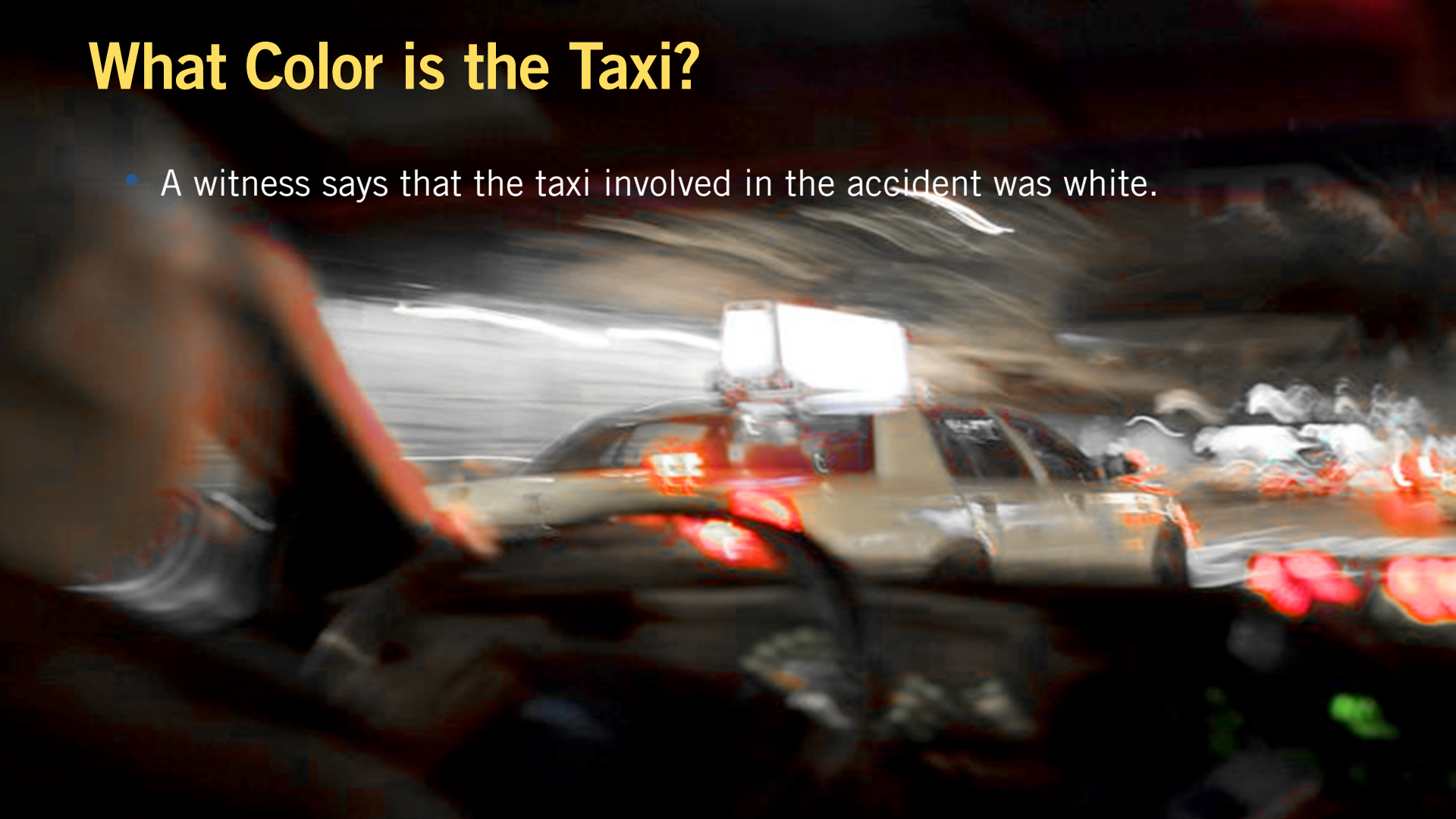
## Human Reasoning Experiment\*

- A taxi was involved in a hit-and-run accident at night.
- Only two taxi companies operate in this city, the Yellow Cab Co. and the White Cab Co.
  - 85% of taxis belong to the Yellow Cab Co.
  - 15% of taxis belong to the White Cab Co.



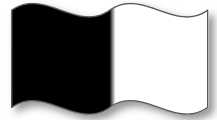
# What Color is the Taxi?

- A witness says that the taxi involved in the accident was white.



# What Color is the Taxi?

At the trial in “Logiland,” where formal deductive logic rules...

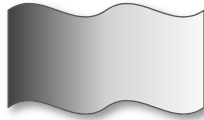


- Premise 1
  - Taxi caused accident ✓
- Premise 2
  - Two taxi companies in town, yellow and white ✓
- Premise 3
  - Accident witness: Taxi was white ✓
- Conclusion
  - White Taxi Co. is responsible for accident



# What Color is the Taxi?

## At the Trial in “Likeliland”



- An expert witness explains that human vision has an 80% accuracy in terms of distinguishing between white and yellow given light conditions at the time of the accident.
  - $P(\text{Witness}=\text{white} \mid \text{Color}=\text{white})=80\%$
  - $P(\text{Witness}=\text{yellow} \mid \text{Color}=\text{white})=20\%$
  - $P(\text{Witness}=\text{yellow} \mid \text{Color}=\text{yellow})=80\%$
  - $P(\text{Witness}=\text{white} \mid \text{Color}=\text{yellow})=20\%$





# What Color is the Taxi?

You are the jury in “Likeliland”!

- Given the three premises and the expert witness statement, what is the probability that the taxi was white?

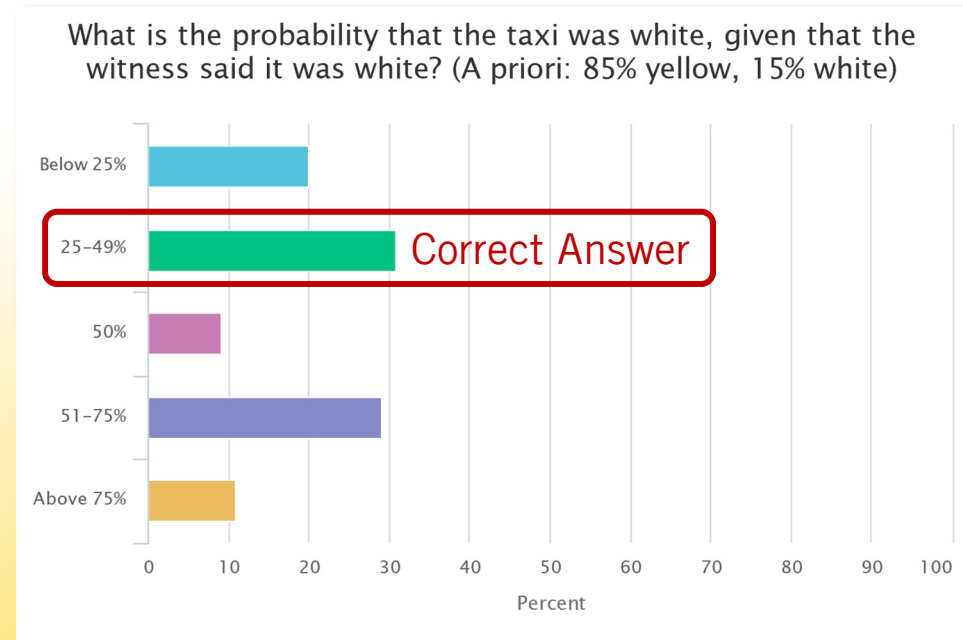




# What Color is the Taxi?

## Results from Webinar Poll

- Correct Answer: 41.38%



# What Color is the Taxi?

- We need to perform probabilistic inference to answer this question.
- Bayes' Rule allows us to compute the probability  $P(\text{Taxi}=\text{white} \mid \text{Witness}=\text{white})$ :

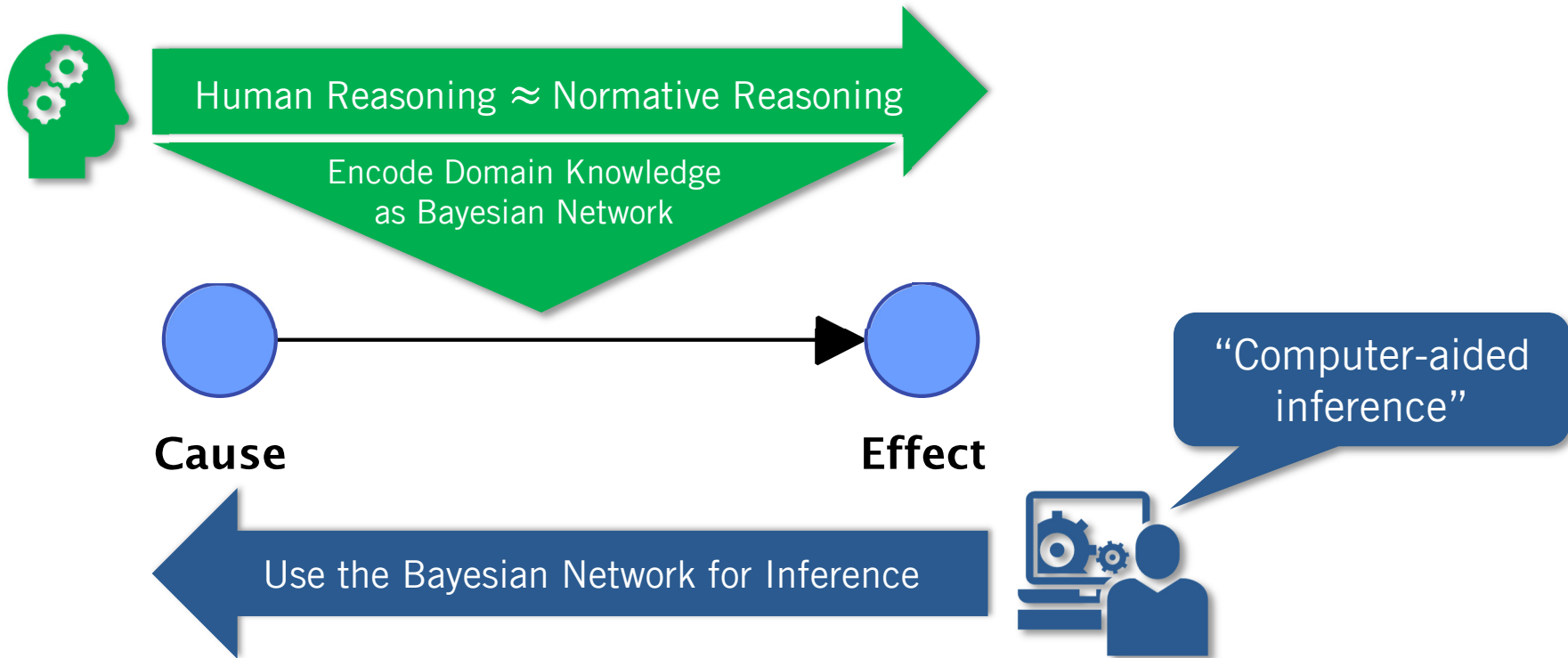
$$P(H \mid E) = \frac{P(E \mid H)P(H)}{P(E)}$$

$$P(\text{Taxi} = \text{white} \mid \text{Witness} = \text{white}) = \frac{P(\text{Witness} = \text{white} \mid \text{Taxi} = \text{white})P(\text{Taxi} = \text{white})}{P(\text{Witness} = \text{white})} =$$
$$\frac{P(\text{Witness} = \text{white} \mid \text{Taxi} = \text{white})P(\text{Taxi} = \text{white})}{P(\text{Witness} = \text{white} \mid \text{Taxi} = \text{white})P(\text{Taxi} = \text{white}) + P(\text{Witness} = \text{white} \mid \text{Taxi} = \text{yellow})P(\text{Taxi} = \text{yellow})}$$

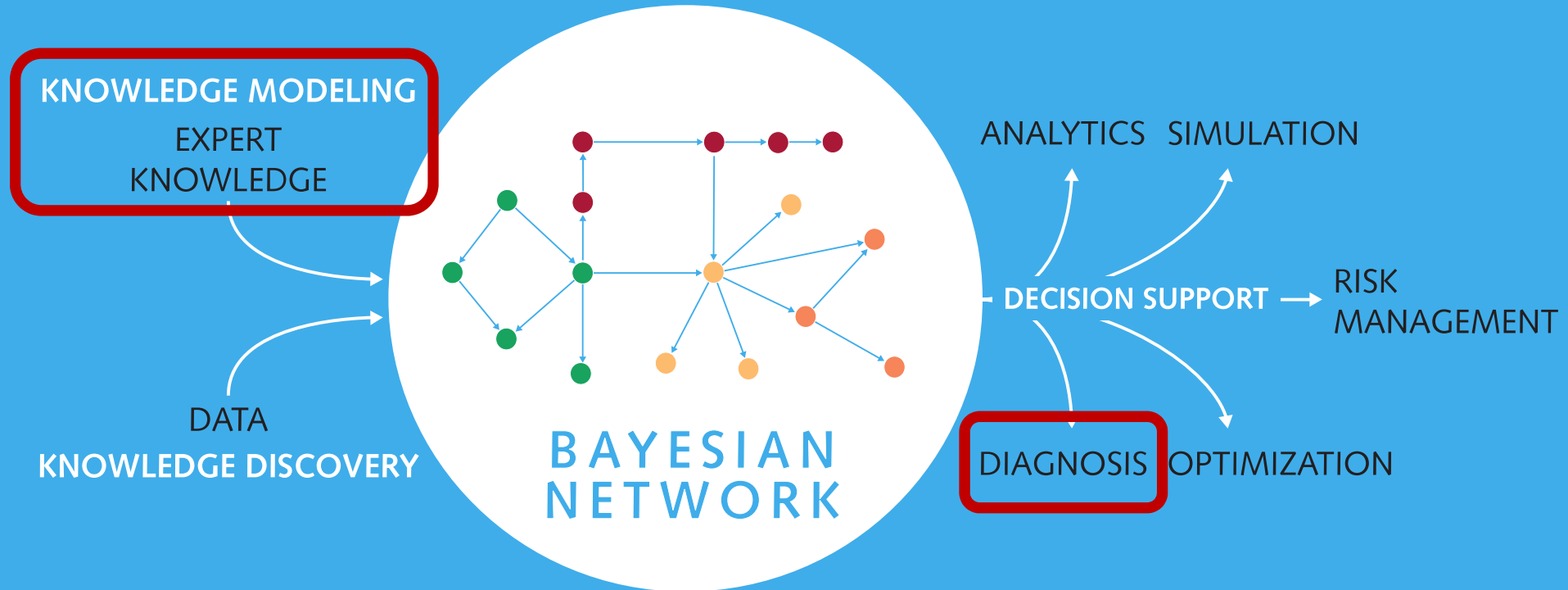
Correct, but impractical

# Bayesian Networks to the Rescue!

## Overcoming our Limitations



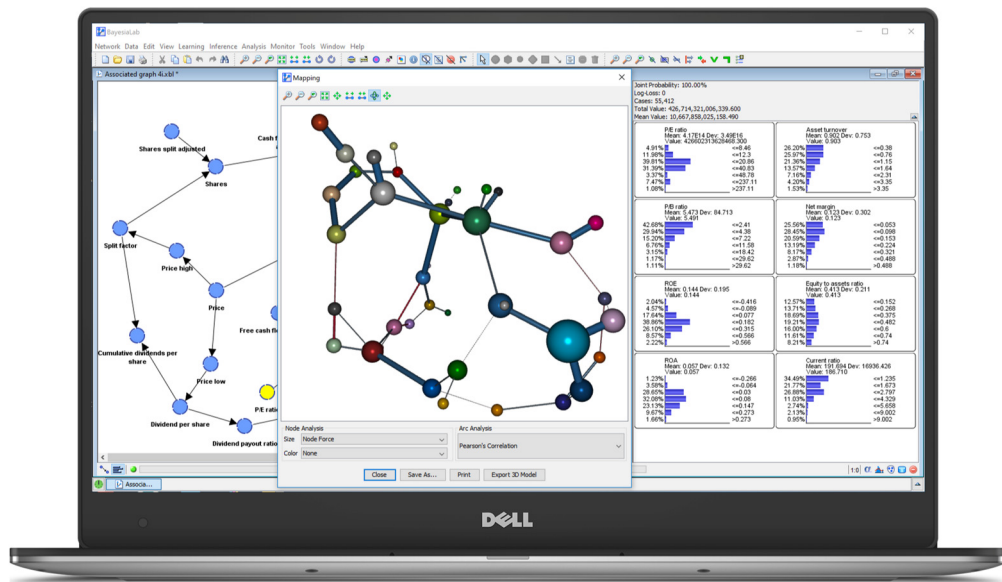
# The BayesiaLab Workflow

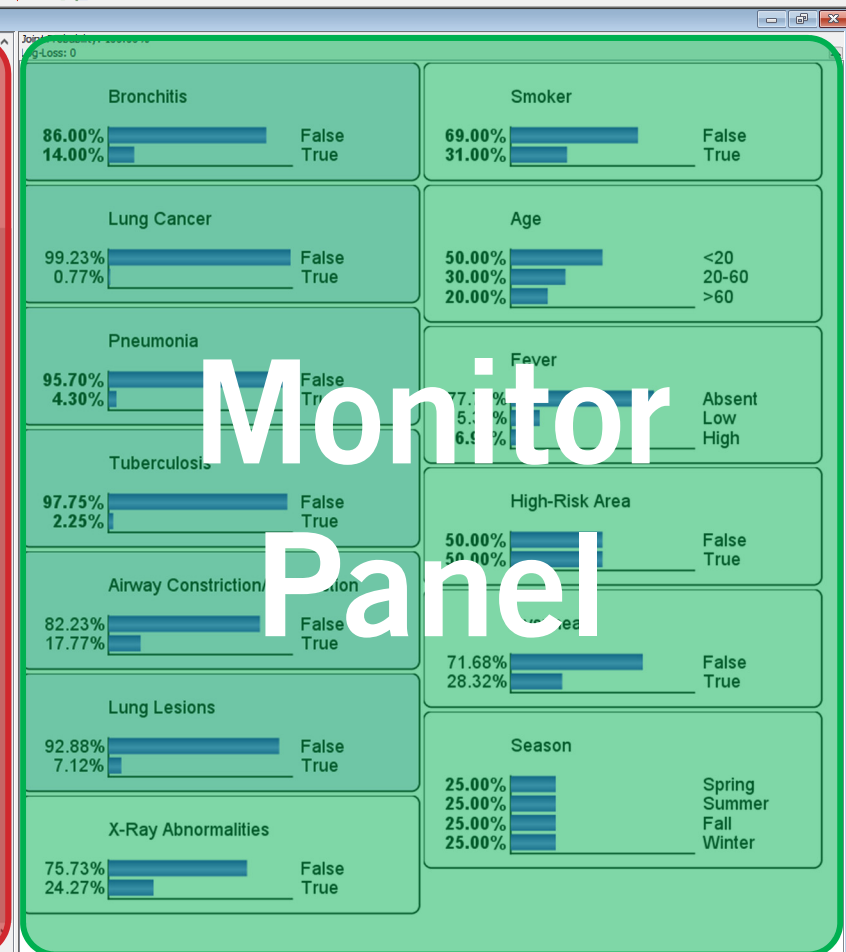
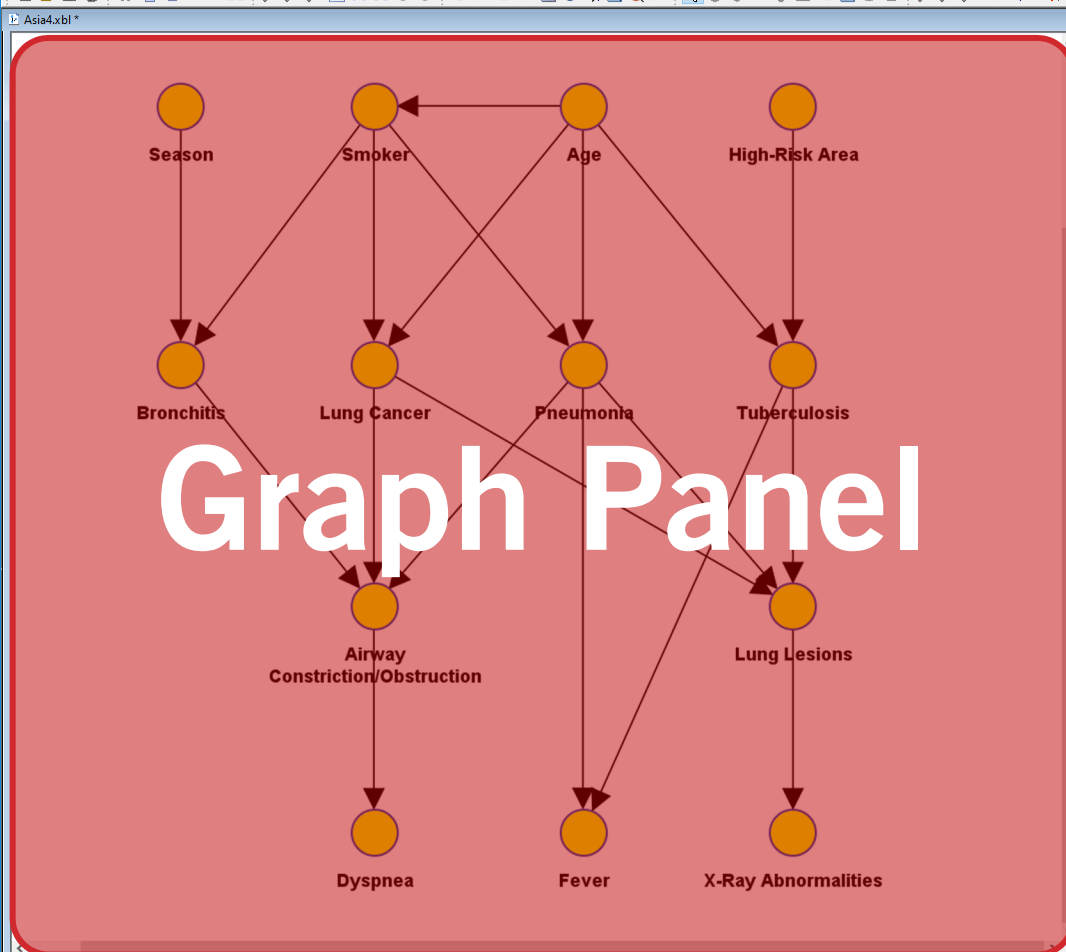




A desktop software for:

- **encoding**
  - learning
  - editing
  - **performing inference**
  - analyzing
  - simulating
  - optimizing
- with Bayesian networks.







# What Color is the Taxi?

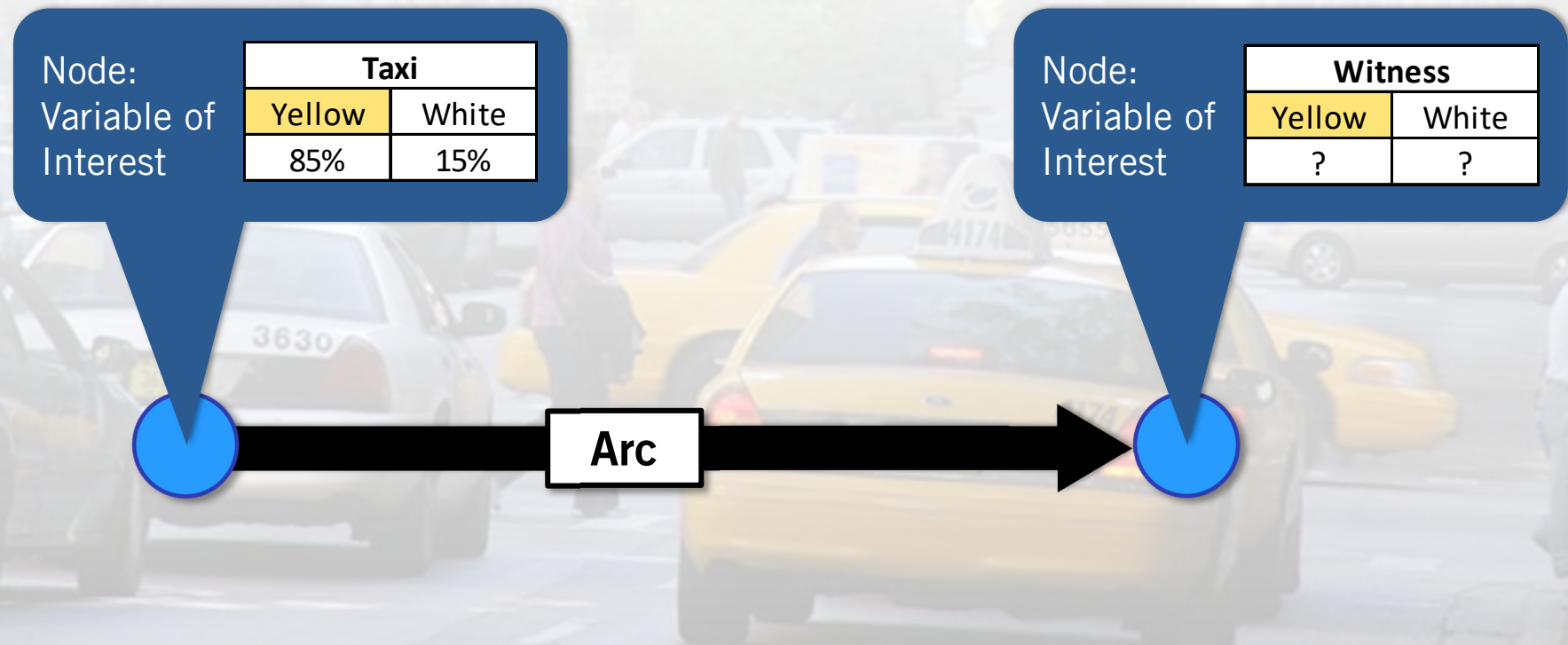
We encode our domain knowledge regarding the taxi cab example:

Node:  
Variable of  
Interest

Taxi	
Yellow	White
85%	15%

# What Color is the Taxi?

We encode our domain knowledge regarding the taxi cab example:



# What Color is the Taxi?

We encode our domain knowledge

Node:  
Variable of  
Interest

Taxi	
Yellow	White
85%	15%

Arc:  
Discrete & Nonparametric  
Probabilistic Relationship

		Witness	
		Yellow	White
Taxi	Yellow	80%	20%
	White	20%	80%

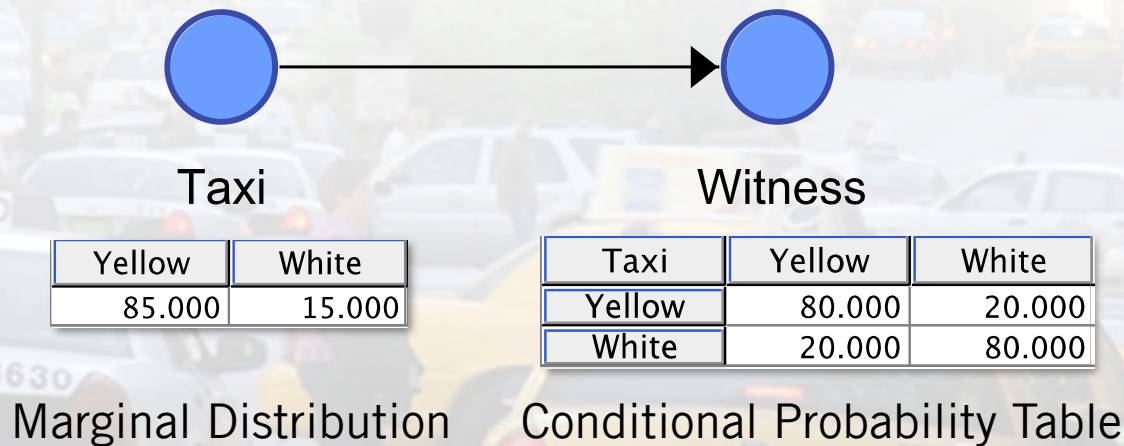
Node:  
Variable of  
Interest

Witness	
Yellow	White
?	?

Arc

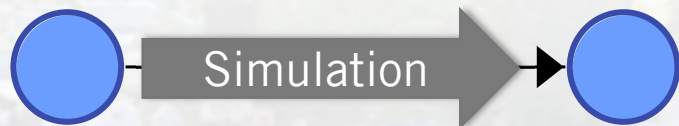
# What Color is the Taxi?

We encode our domain knowledge regarding the taxi cab example:



# What Color is the Taxi?

Inference based on evidence:

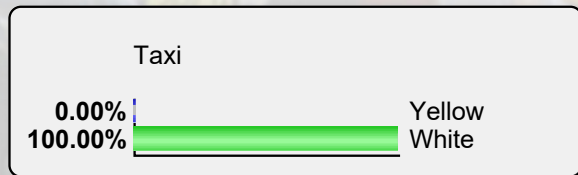


Taxi

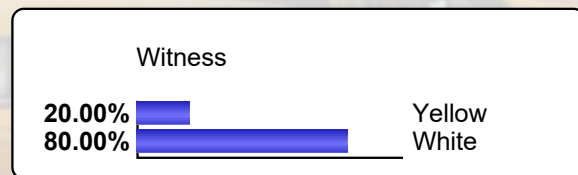
Yellow	White
85.000	15.000

Witness

Taxi	Yellow	White
Yellow	80.000	20.000
White	20.000	80.000



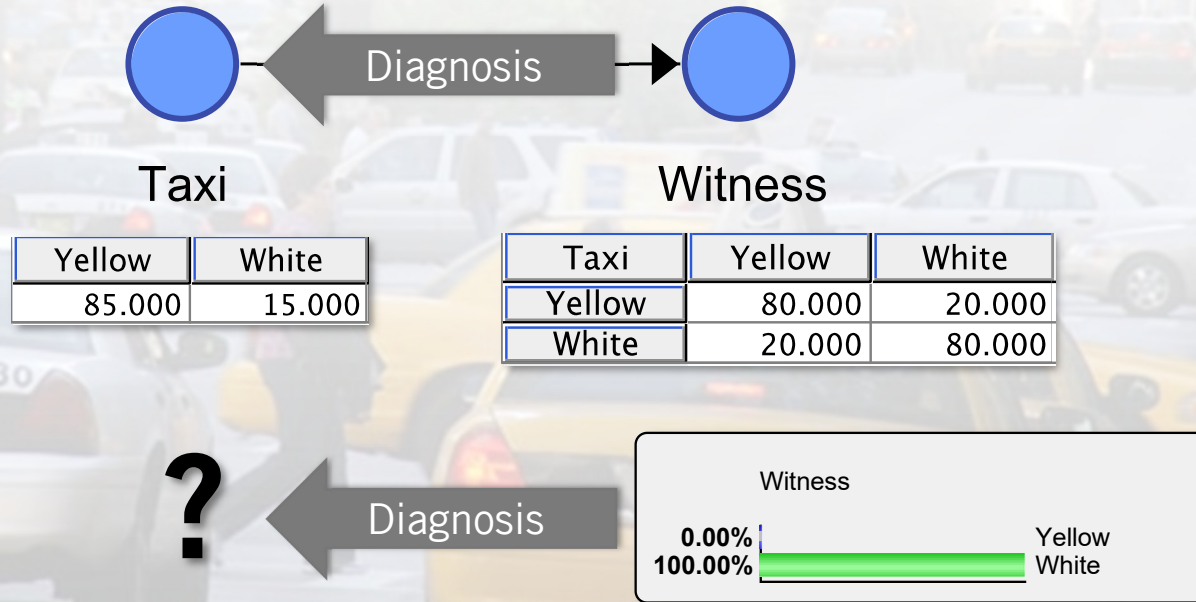
Simulation





# What Color is the Taxi?

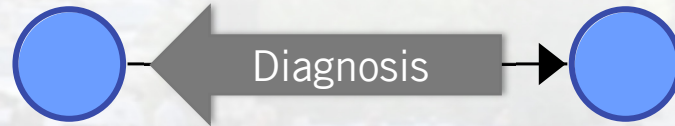
Performing inference based on observing evidence:





# What Color is the Taxi?

Performing inference based on observing evidence:

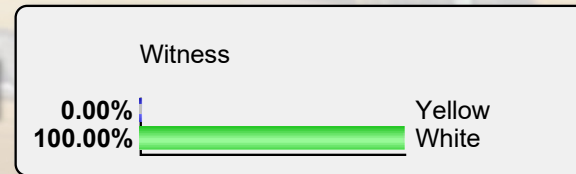
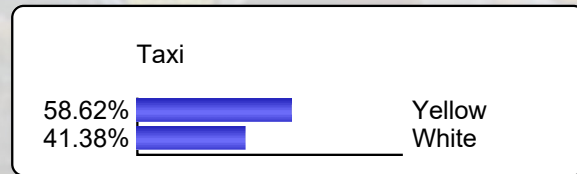


Taxi

Yellow	White
85.000	15.000

Witness

Taxi	Yellow	White
Yellow	80.000	20.000
White	20.000	80.000



Diagnosis



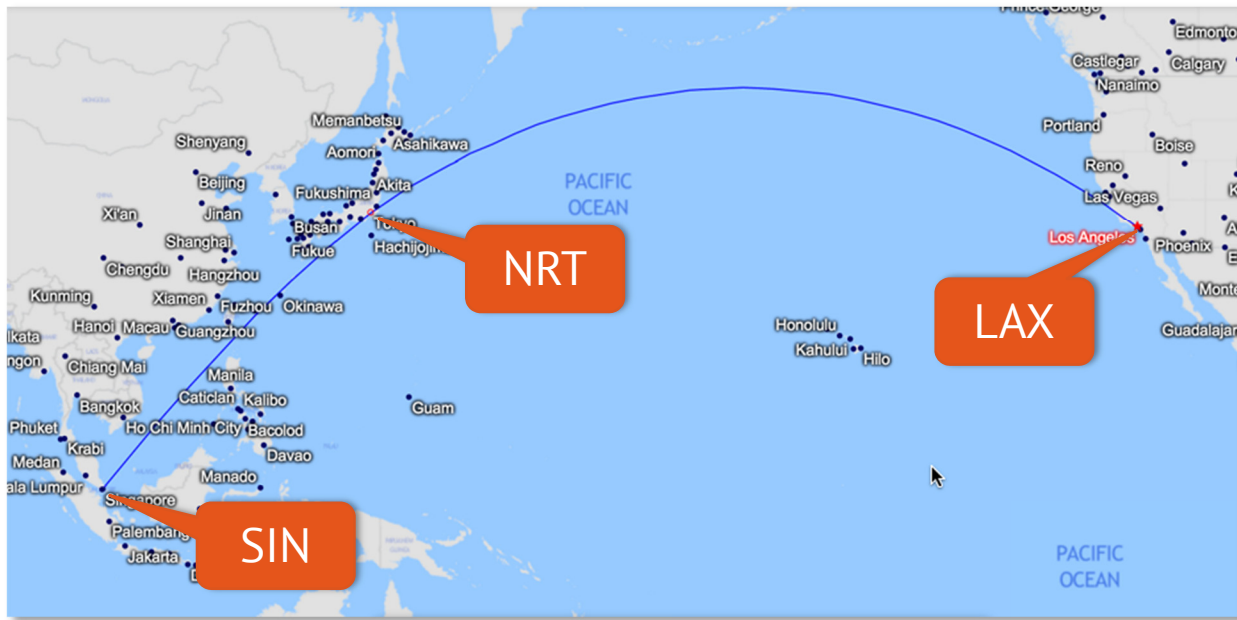
See Chapter 4

## Example 2: Where is my bag?

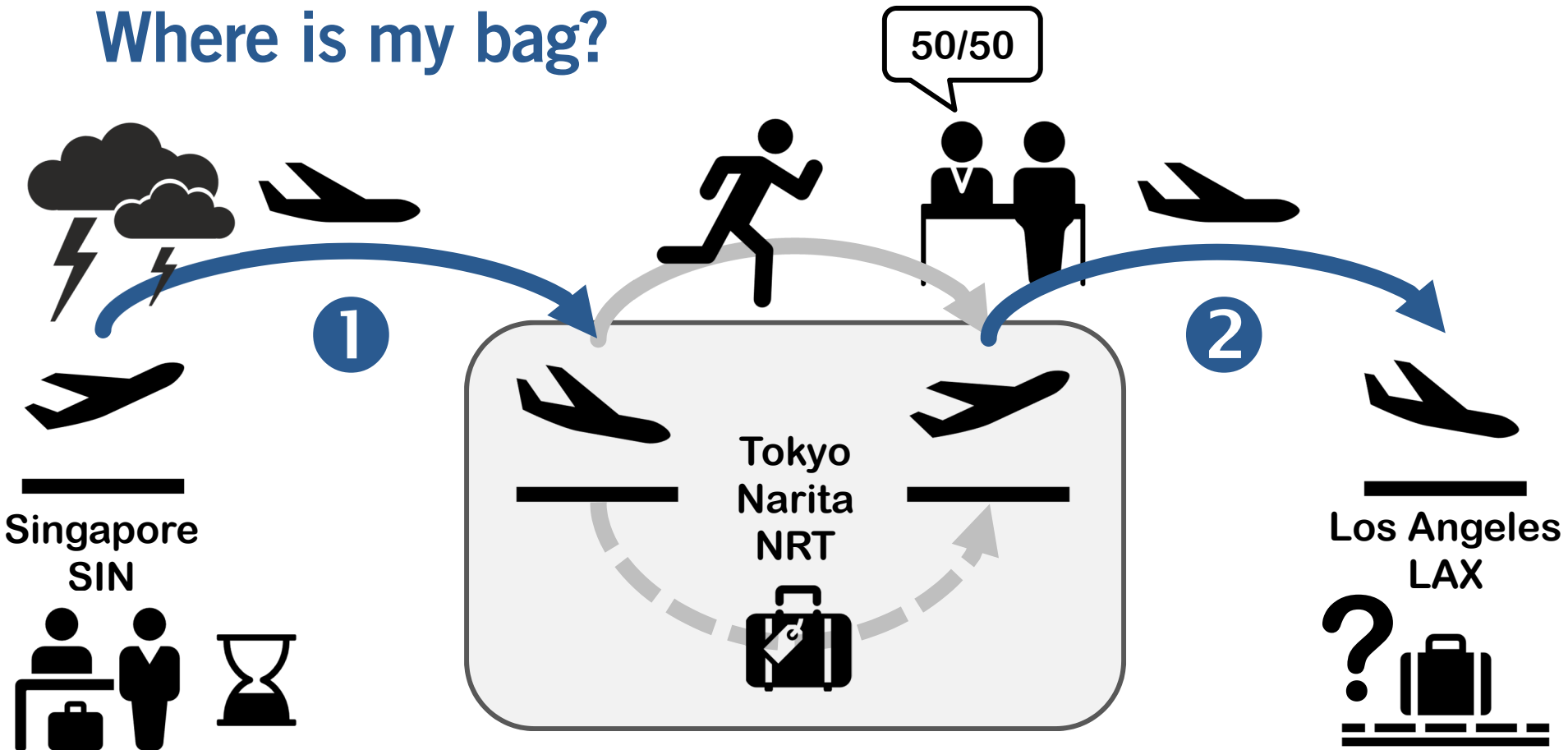
Knowledge Modeling & Reasoning Under Uncertainty

# Example 2: Where is my bag?

Travel Route: Singapore (SIN) → Tokyo/Narita (NRT) → Los Angeles (LAX)



# Where is my bag?

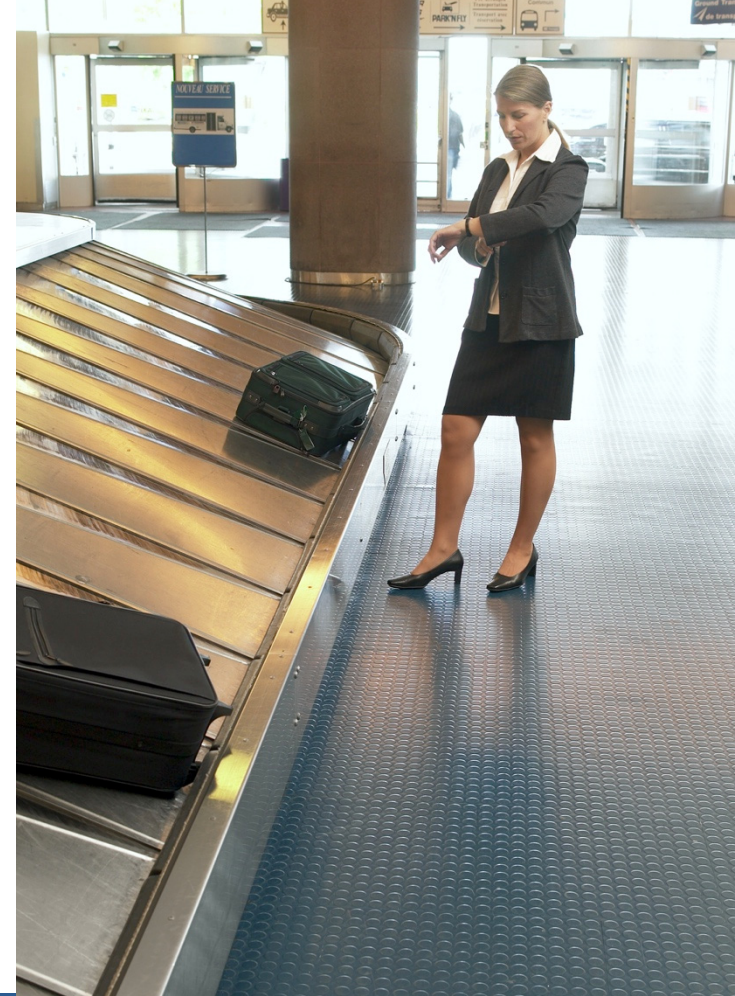




# Where is my bag?

## Scenario 1

- Luggage delivery starts onto the carousel.
- **After 5 minutes**, I still do not see my bag.
- What is the probability that I will still get my bag?









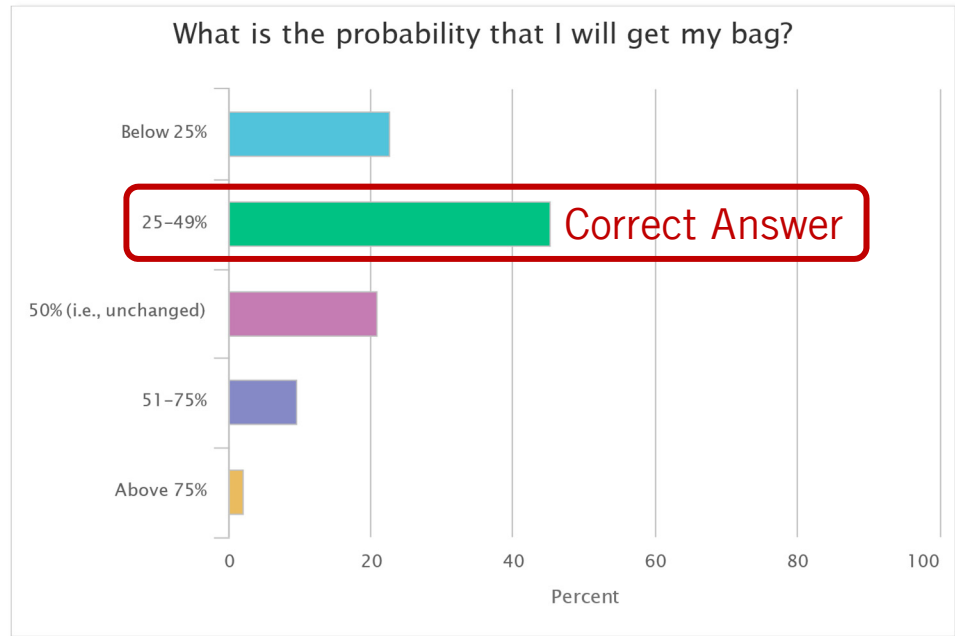
IS MY BAG  
IN THERE?



# Where is my bag?

## Results from Webinar Poll

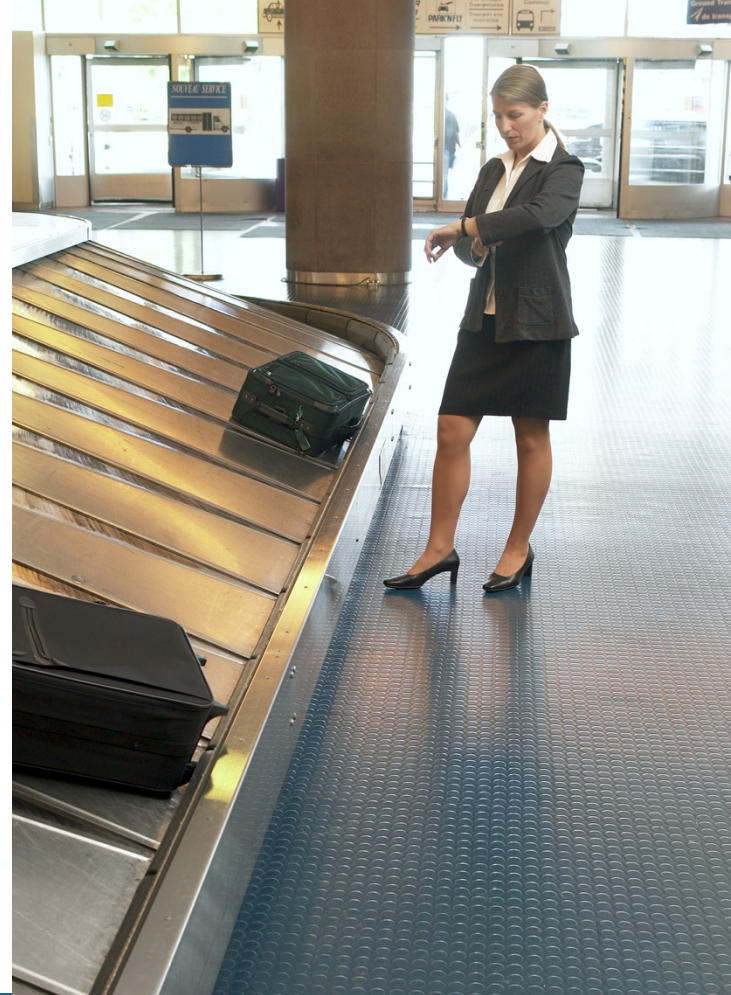
- Correct Answer: 33%

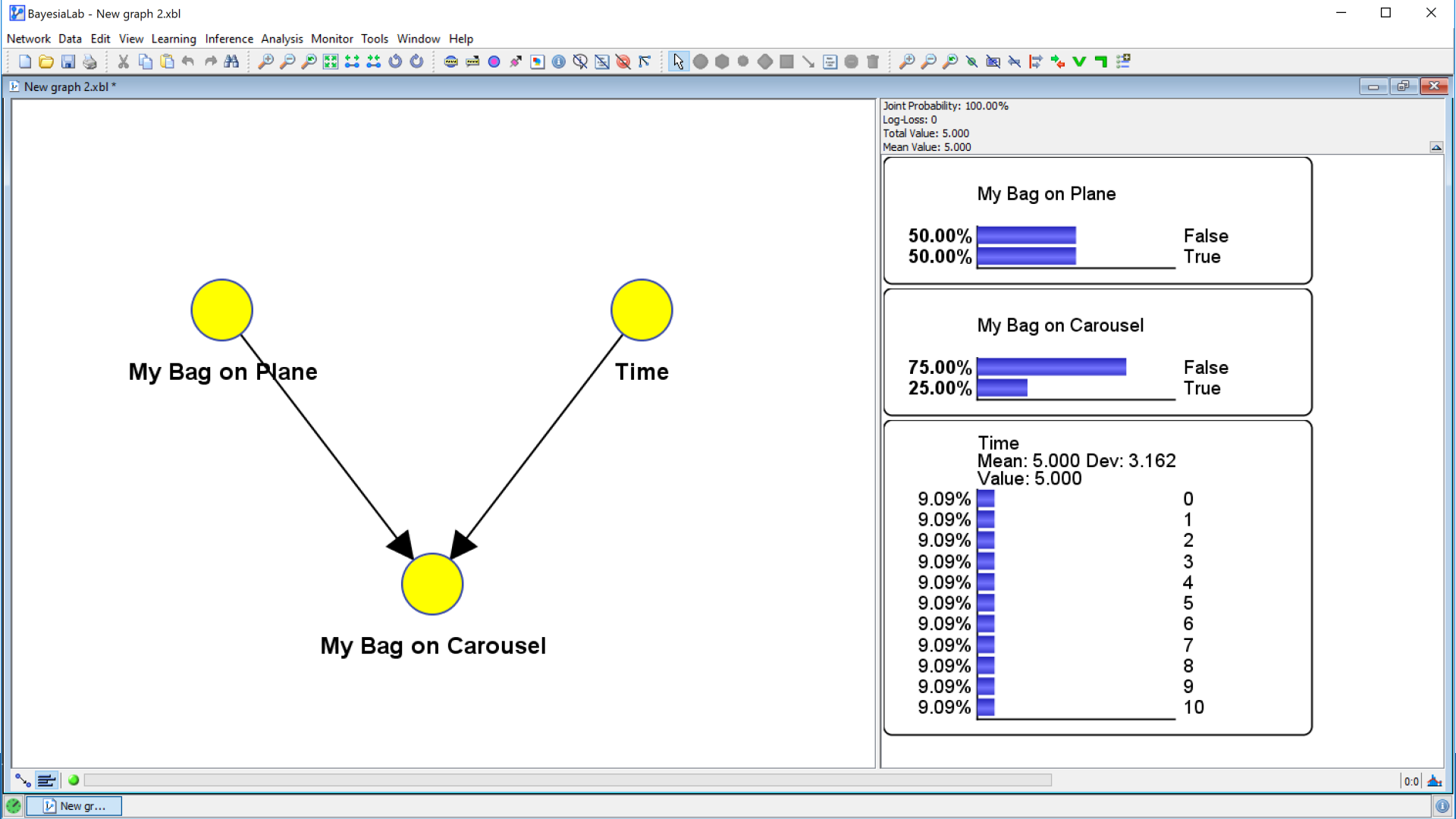


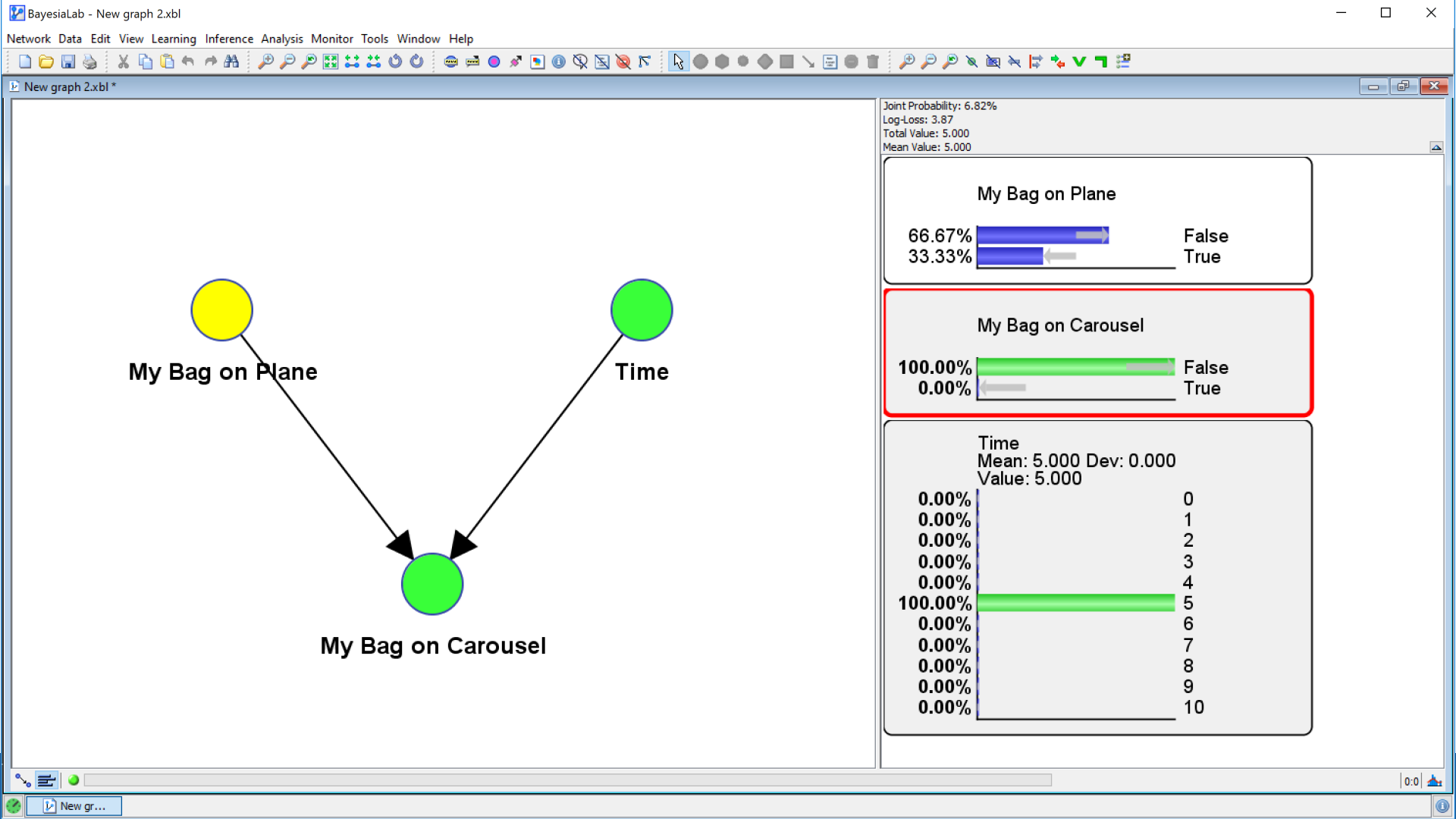
# Where is my bag?

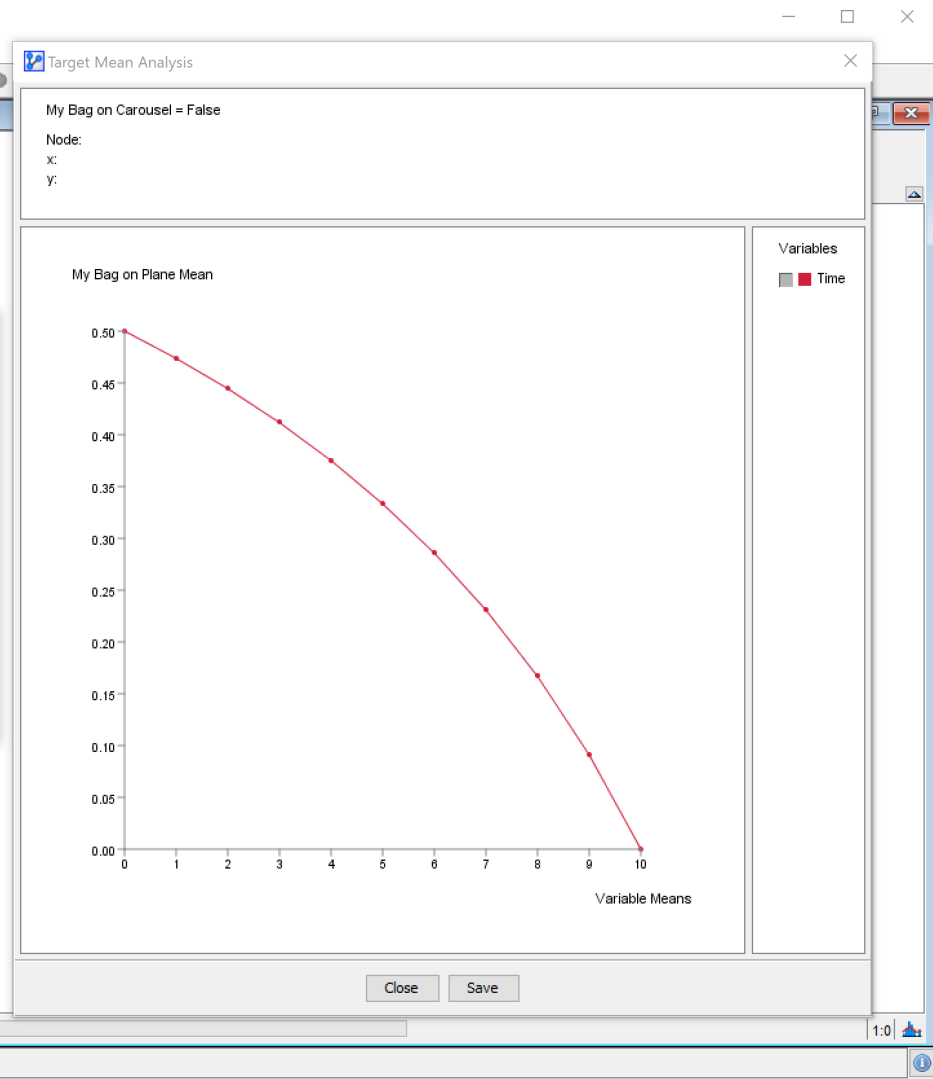
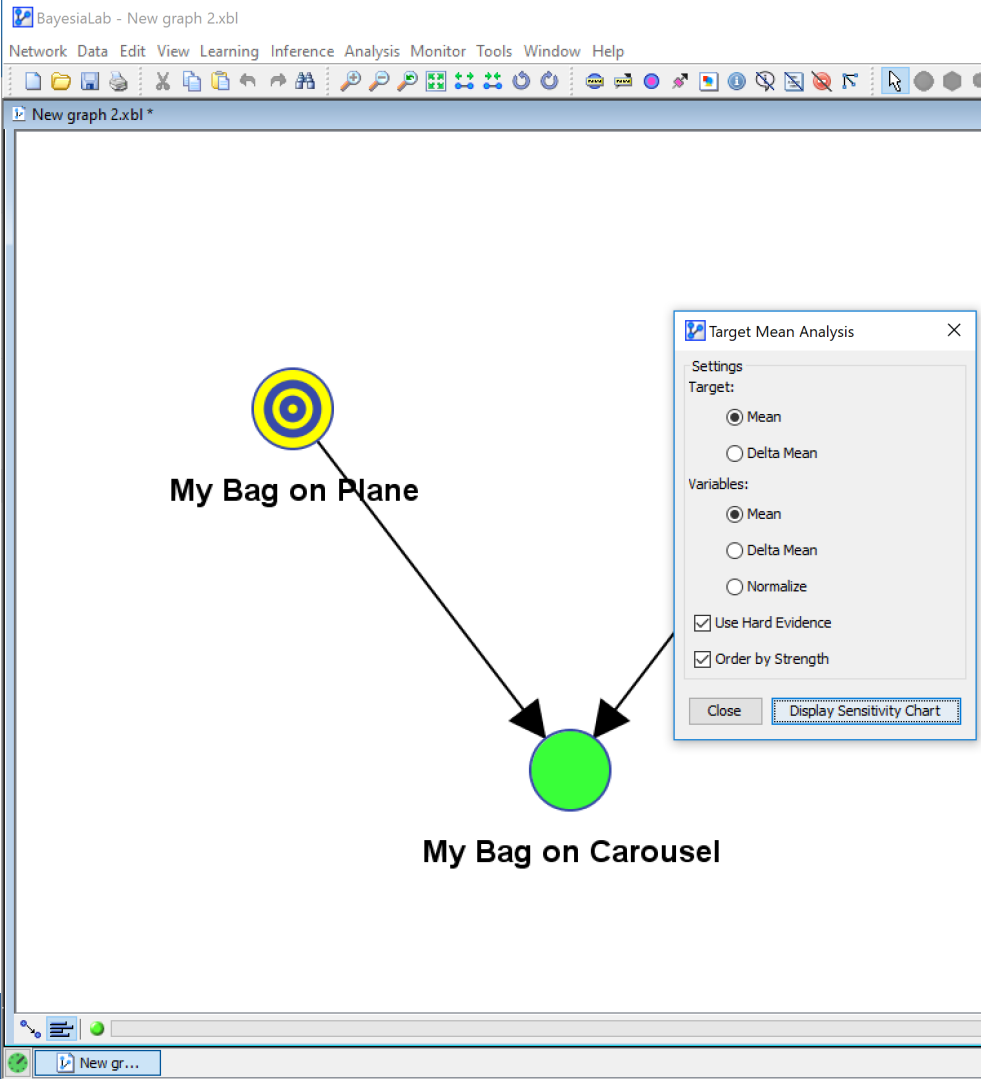
## Proposed Workflow

- Encode the available — albeit very limited — knowledge into a Bayesian network.
- Use BayesiaLab to perform probabilistic inference given our observations.





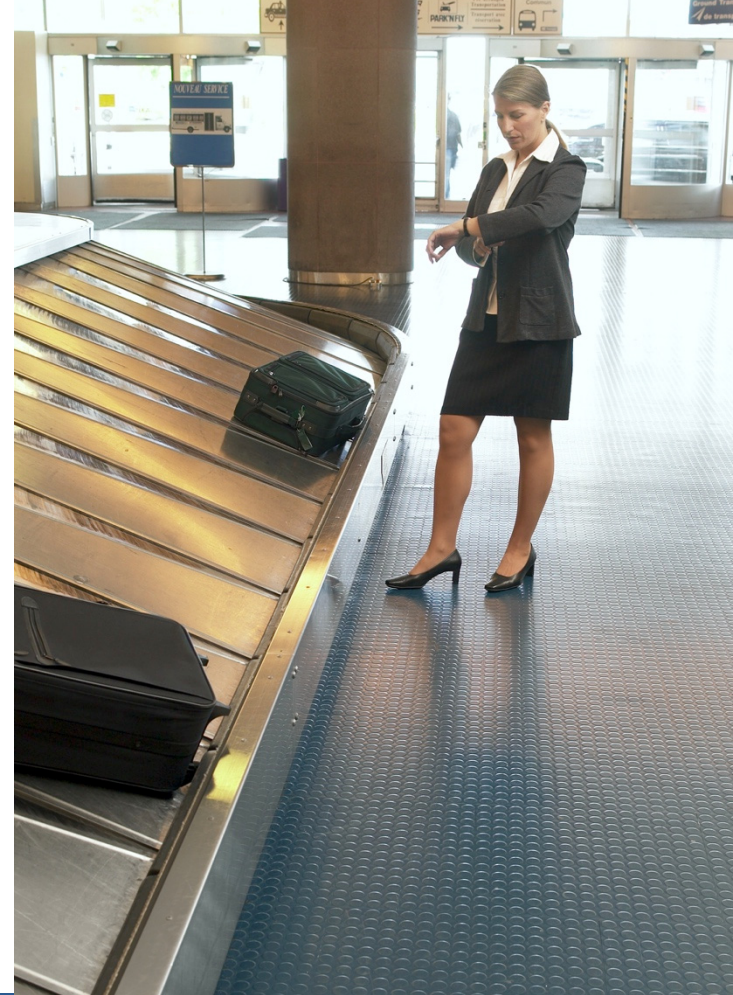


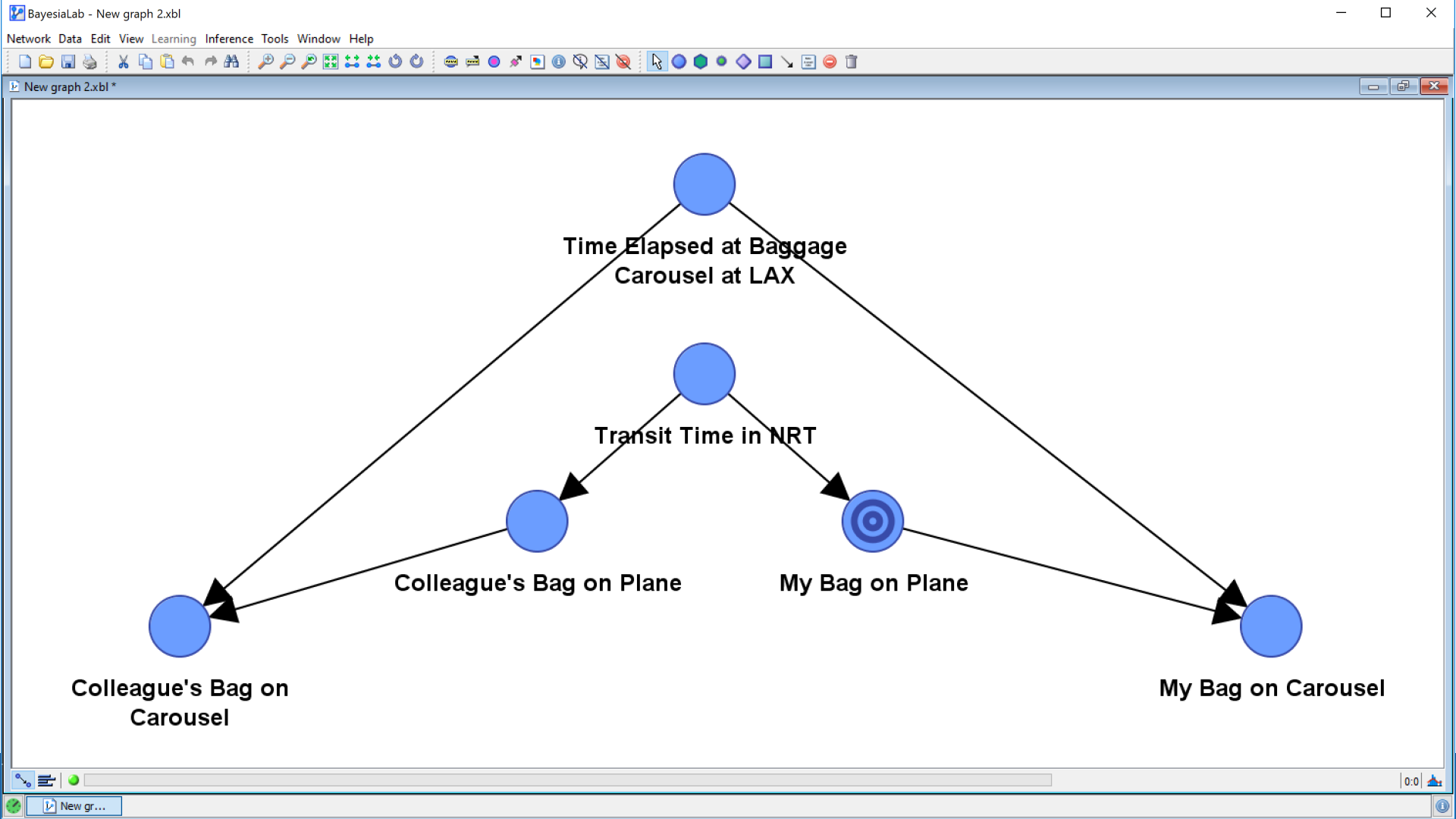


# Where is my bag?

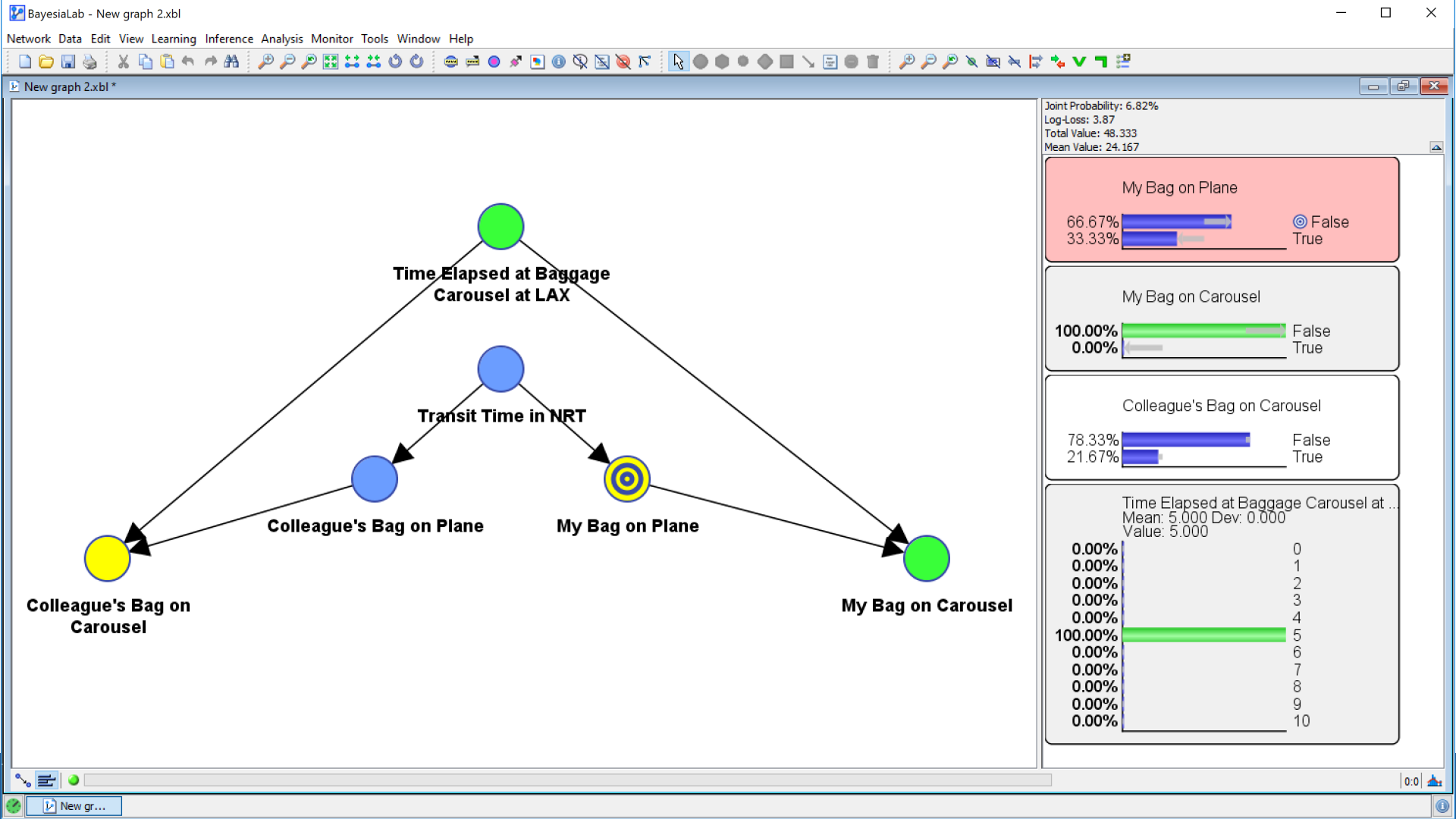
## Scenario 2

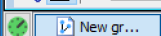
- Luggage delivery starts onto the carousel.
- After 5 minutes, I still do not see my bag.
- However, now I see a colleague, who traveled on the same itinerary, pick up his bag.
- What is now the probability that I will still get my bag?

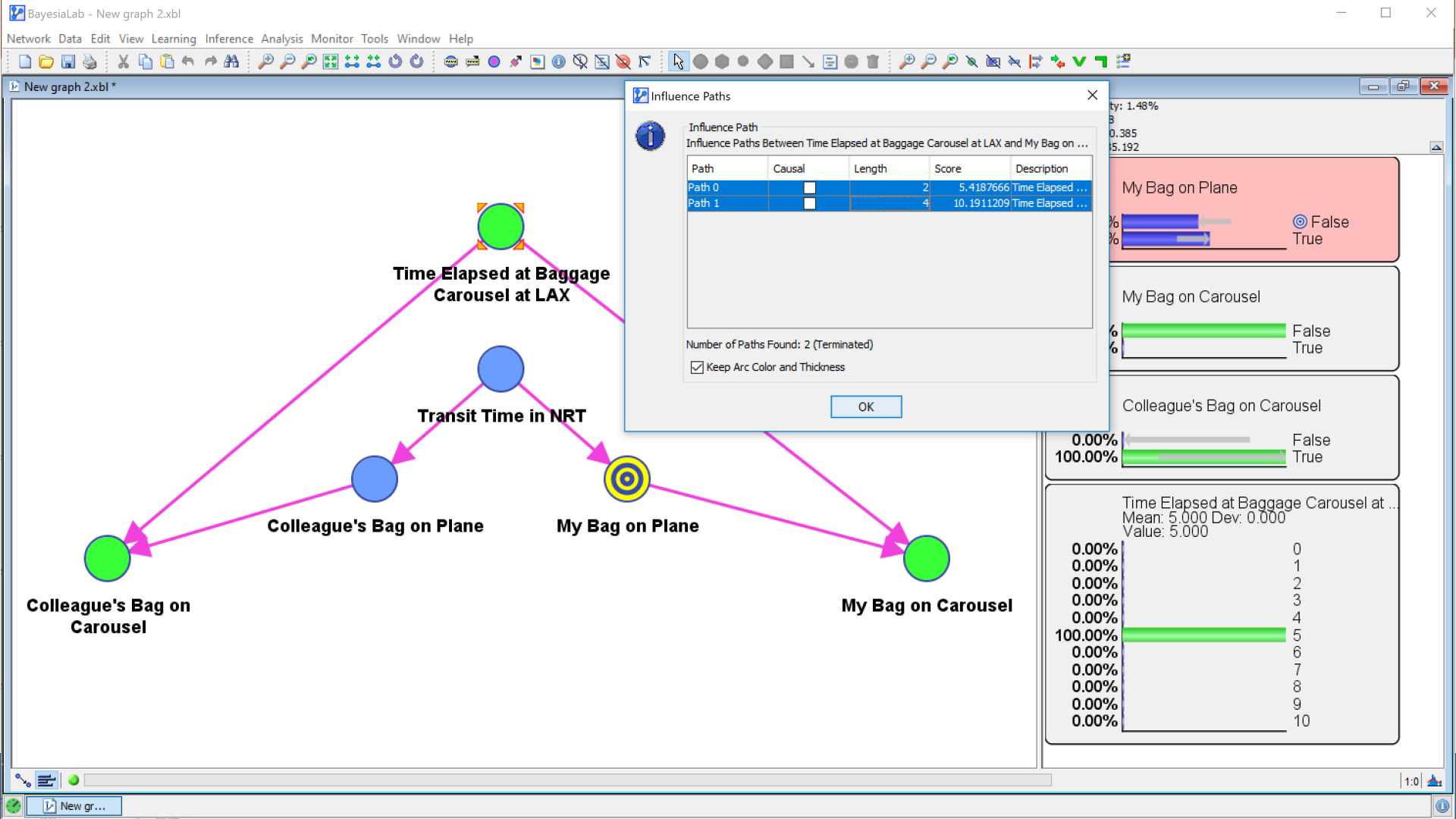








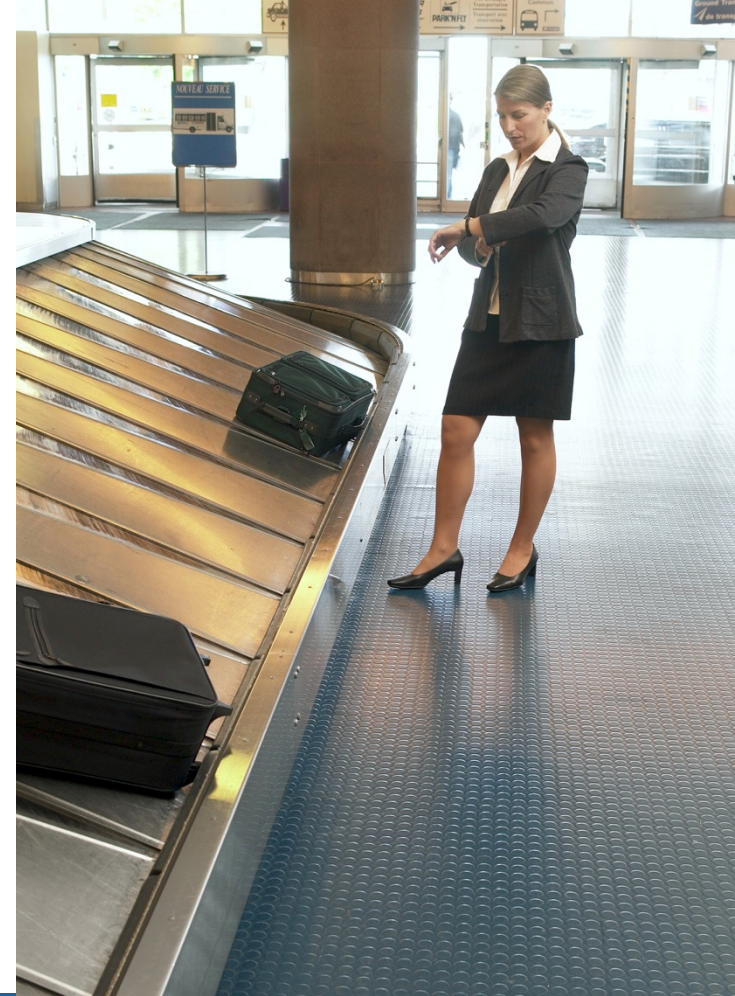




# Where is my bag?

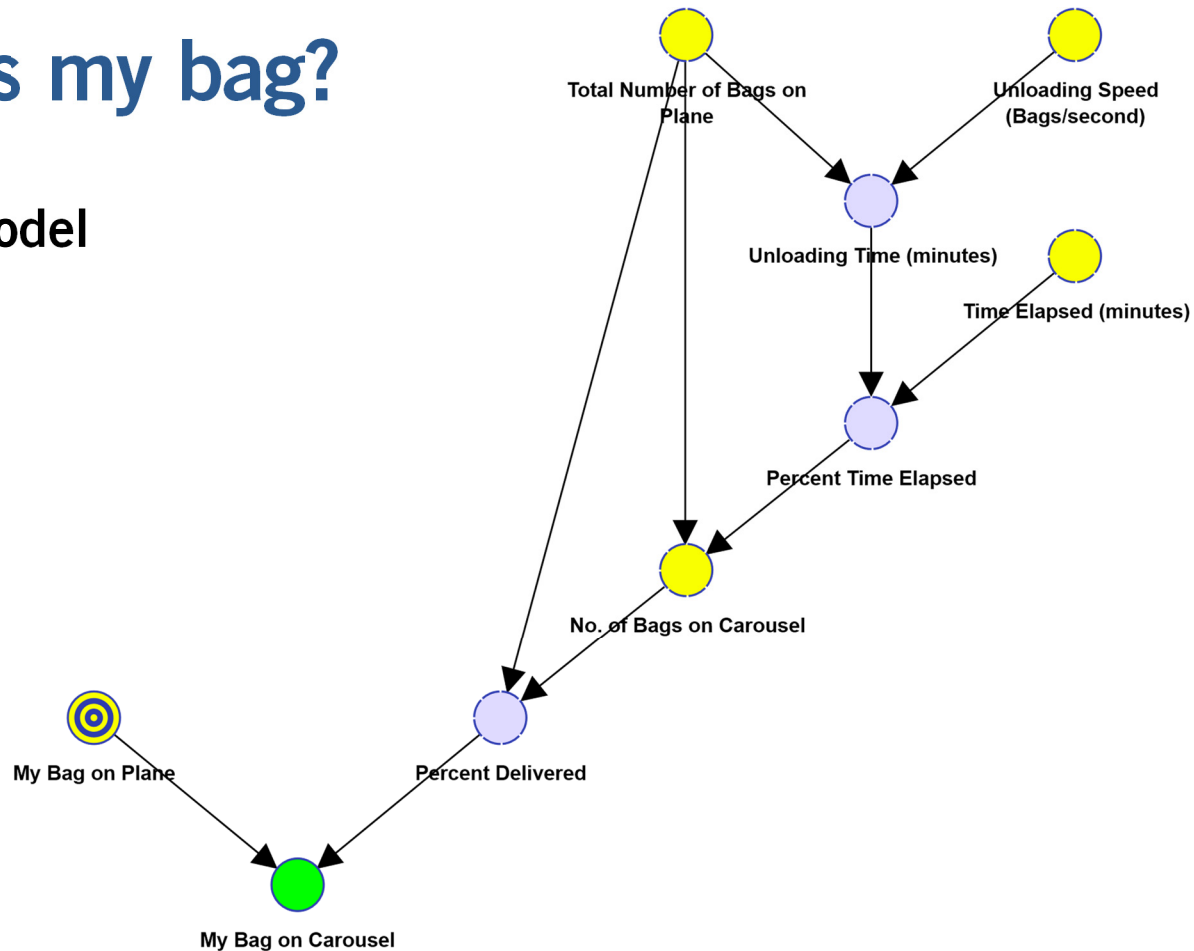
## Scenario 3

- Luggage is delivered on the carousel, **a total of 50 bags in the first 5 minutes**, yet I still do not see my bag.
- What is the probability that I will still get my bag?



# Where is my bag?

## Extended Model



# Where is my bag?

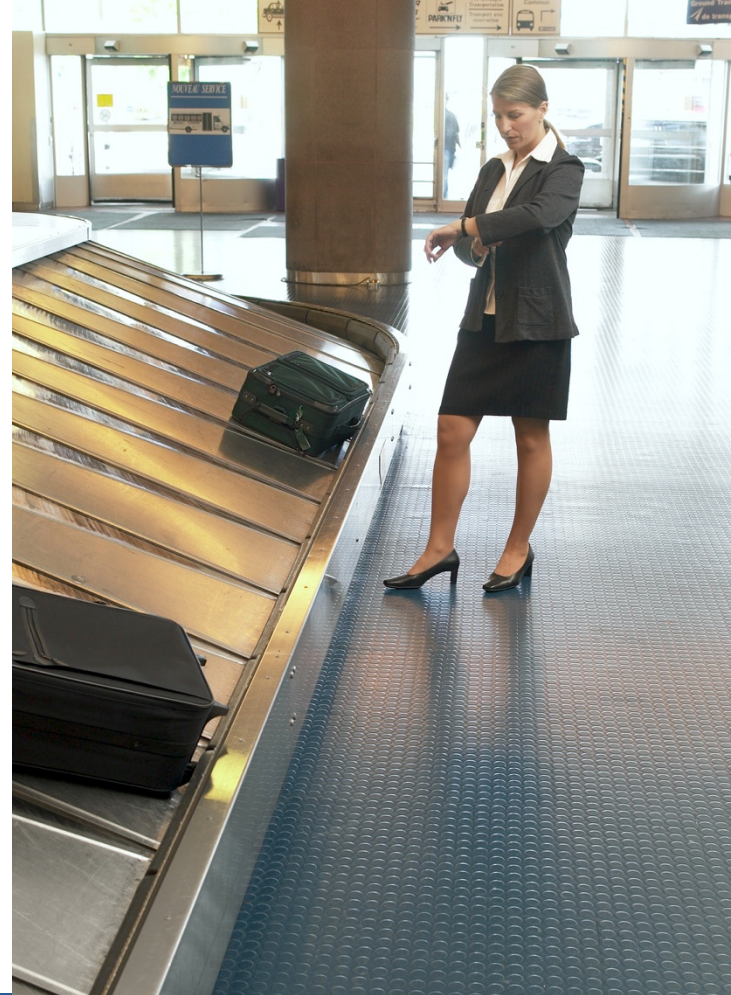
## More important questions:

- Will the patient ultimately respond to the current treatment?
- Should we continue a search and rescue effort?
- Should we still follow the original business strategy, i.e. “hold the course”?

# Where is my bag?

## Key Points

- Encoding of knowledge
- Reasoning under uncertainty
- Reasoning
  - from cause to effect (simulation)
  - from effect to cause (diagnosis)
- Inter-causal reasoning







**In Conclusion...**

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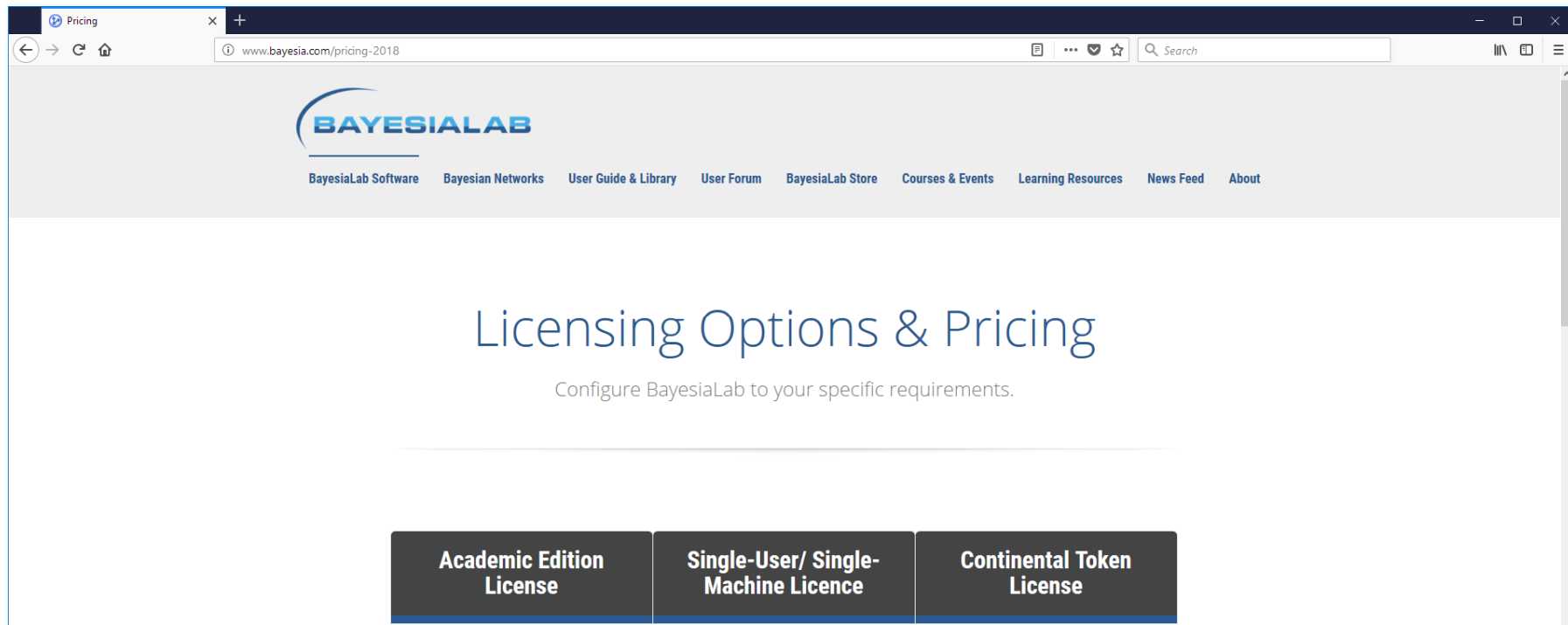
**Latest New Top**

 **Webinar on Diagnostic Decision Support with Bayesian Networks**  
a minute ago by [stefanconrady](#): The answers to all webinar questions will be posted here.

💬 0 👍 0 👁 0  
Started by [stefanconrady](#) a minute ago

🌐 English ▼

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BayesiaLab is suite of powerful Artificial Intelligence programs that provide researchers a comprehensive “lab” environment for machine learning, knowledge modeling, analytics, simulation, and optimization — all based on the Bayesian network paradigm.

Support

# Webinar Series: Friday at 1 p.m. (Central)

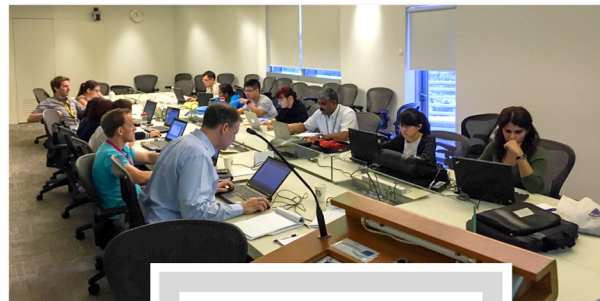
## Upcoming Webinars:

- March 9      Bayesian Networks for Risk Management without Data
- March 16     Optimizing Health Policies with Bayesian Networks
- March 23     t.b.d.

**Register here: [bayesia.com/events](https://bayesia.com/events)**


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- August 29–31  
London, UK
- September 26–28  
New Delhi, India
- October 29–31  
Chicago, IL
- December 4–6  
New York, NY



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A nighttime photograph of a city street. On the right, a large, classical-style building with prominent white columns and a pediment is illuminated with warm yellow lights. The building's facade is made of light-colored stone or concrete. To the left of this building, several modern skyscrapers with glass facades are visible, some of which have interior lights glowing. The street in the foreground shows light trails from cars, indicating a long exposure. The sky is a deep blue, suggesting twilight. A semi-transparent white box containing text is overlaid on the bottom left of the image.

Introductory BayesiaLab Course  
in San Francisco, California  
March 13–15, 2018



# 6<sup>th</sup> Annual BayesiaLab Conference in Chicago

## November 1–2, 2018



# Thank You!



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