



Marketing Mix Optimization

Causal Inference in Marketing Science

The webinar will start at:

13:00:00

The current time is:

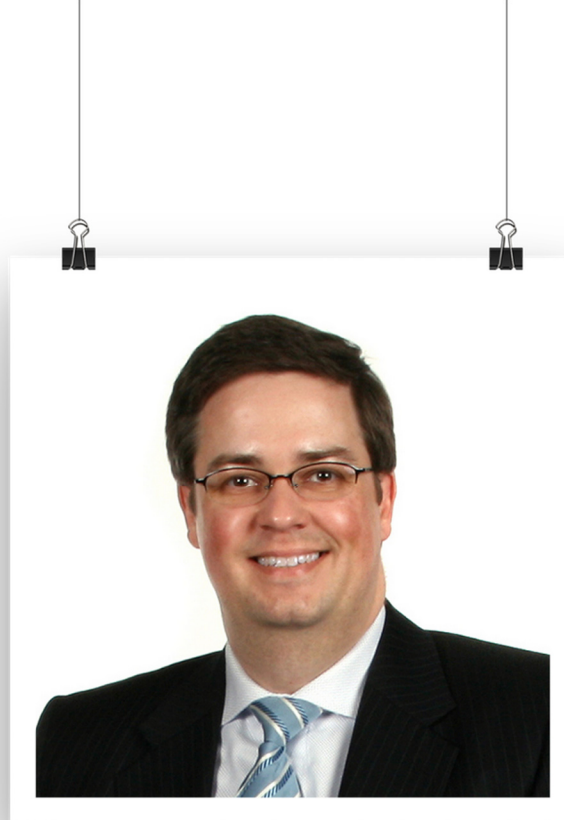
12:47:30

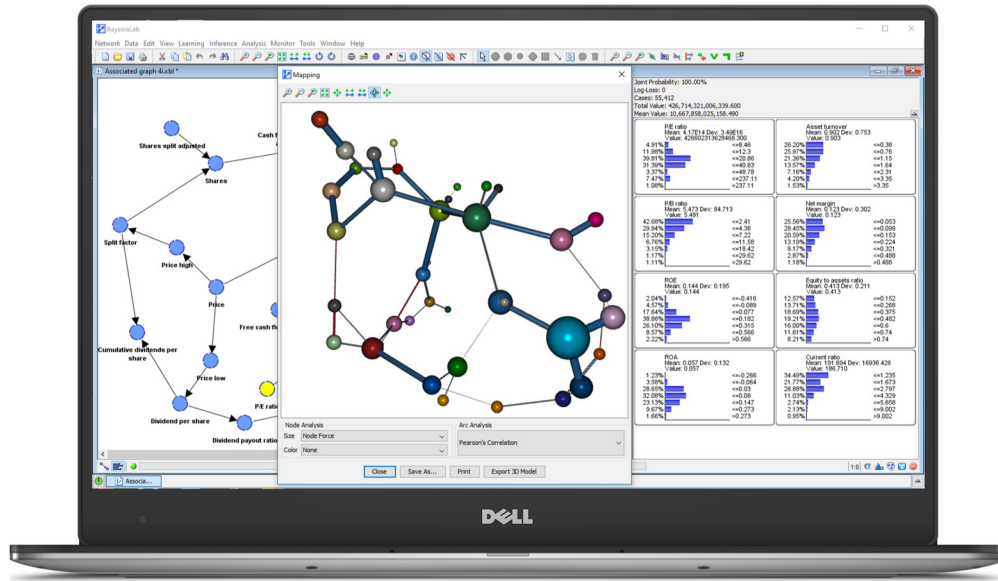
Central Daylight Time, UTC-5



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A desktop software for:

- encoding
 - learning
 - editing
 - performing inference
 - analyzing
 - simulating
 - optimizing
- with Bayesian networks.

Today's Program

1. Motivation & Background

- Introductory Example:
The Generic 2000 Commercial
- Simpson's Paradox & Causality

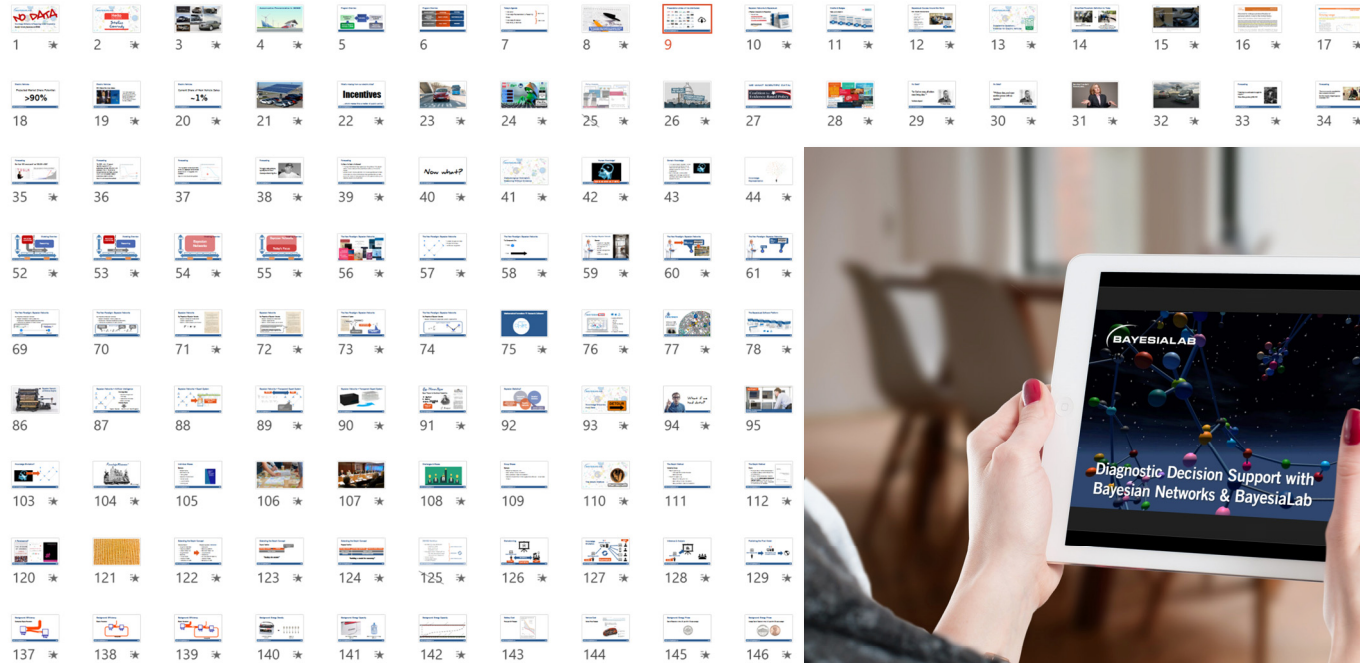


2. Marketing Mix Modeling Workflow

- Causal Assumptions?
- Disjunctive Cause Criterion
- Machine-Learning with BayesiaLab
- Causal Inference & Optimization



Webinar Slides, Data, and Recording Available



Bayesian Networks & BayesiaLab

A Practical Introduction for Researchers

- Free download:
www.bayesia.com/book
- Hardcopy available on Amazon:
<http://amzn.com/0996533303>



Introductory Example

GENERIC
2000



- The Generic Car Company runs a commercial at the Super Bowl for its new model, the Generic 2000.



- The Generic Car Company runs a commercial at the Super Bowl for its new model, the Generic 2000.



Introductory Example

Telephone Survey

- Afterwards, Generic conducts a telephone survey of 1,000 car shoppers to understand the effect of the Super Bowl commercial on shopping and purchase behavior.

Ad Exposure	Gender	Test Drive	Purchase
0	1	0	0
0	0	1	1
0	1	0	0
0	0	0	0
1	1	0	1
1	1	0	0
		1	1
		1	0
		1	1
		1	0



Observational Data

Introductory Example

Analyzing the survey with a cross-tab...

Ad Exposure	Gender	Test Drive	Purchase
0	1	0	0
0	0	1	1
0	1	0	0
0	0	0	0
1	1	0	1
1	1	0	0
1	0	1	1
0	1	1	0
⋮	⋮	⋮	⋮
0	1	1	0

Ad Exposure	Purchase
No	<div><div></div></div> 60%
Yes	<div><div></div></div> 45%



-15%

Introductory Example

However, grouping the survey data by Gender reveals:



Ad Exposure	Gender	Test Drive	Purchase
0	1	0	0
0	0	1	1
0	1	0	0
0	0	0	0
1	1	0	1
1	1	0	0
1	0	1	1
0	1	1	0
⋮	⋮	⋮	⋮
0	1	1	0

Gender	Ad Exposure	Purchase
Male	No	<div><div></div></div> 30%
	Yes	<div><div></div></div> 35%
Female	No	<div><div></div></div> 70%
	Yes	<div><div></div></div> 75%







Introductory Example

How is this possible?

Ad Exposure	Purchase
No	 60%
Yes	 45%



Gender	Ad Exposure	Purchase
Male	No	 30%
	Yes	 35%
Female	No	 70%
	Yes	 75%



Simpson's Paradox

Simpson's paradox is a phenomenon in probability and statistics, in which an effect appears in subgroups of data but disappears or reverses when these groups are combined.

Introductory Example

Grouping the data by Test Drive shows:

Ad Exposure	Gender	Test Drive	Purchase
0	1	0	0
0	0	1	1
0	1	0	0
0	0	0	0
1	1	0	1
1	1	0	0
1	0	1	1
0	1	1	0
⋮	⋮	⋮	⋮
0	1	1	0

Test Drive	Ad Exposure	Purchase
No	No	<div><div></div></div> 60%
	Yes	<div><div></div></div> 50%
Yes	No	<div><div></div></div> 60%
	Yes	<div><div></div></div> 30%

-10%

-40%



Introductory Example

Finally, grouping the data by Gender and Test Drive reveals:

Ad Exposure	Gender	Test Drive	Purchase
0	1	0	0
0	0	1	1
0	1	0	0
0	0	0	0
1	1	0	1
1	1	0	0
1	0	1	1
0	1	1	0
⋮	⋮	⋮	⋮
0	1	1	0

Test Drive	Gender	Ad Exposure	Purchase
No	Male	No	30%
		Yes	40%
	Female	No	70%
		Yes	80%
Yes	Male	No	30%
		Yes	20%
	Female	No	70%
		Yes	60%



So, what's the advertising effect?

Test Drive	Gender	Ad Exposure	Purchase
No	Male	No	30%
		Yes	40%
	Female	No	70%
		Yes	80%
Yes	Male	No	30%
		Yes	20%
	Female	No	70%
		Yes	60%

≈ 0

Gender	Ad Exposure	Purchase
Male	No	30%
	Yes	35%
Female	No	70%
	Yes	75%

$+0.05$

Ad Exposure	Purchase
No	60%
Yes	45%

-0.15

Test Drive	Ad Exposure	Purchase
No	No	60%
	Yes	50%
Yes	No	60%
	Yes	30%

-0.2



Your Opinion?

Did this commercial have a positive or negative effect on purchase?



RUSSELL GLASS · SEAN CALLAHAN

THE

DATA-DRIVEN
BUSINESS
MAKING
DATA-DRIVEN
DECISIONS

BUSINESS

MAKING
DATA-DRIVEN
DECISIONS

with



DATA
DRIVEN



O'REILL

Data
Driven

Creating a Data Culture

5 Steps To Powering
Data Driven Decision Making

Data-Driven

Decision-Making

increasing sales with
DATA - DRIVEN
MARKETING



loginradius

DATA-DRIVEN
FORTUNE 500

decisions in a



Data
driven
decisions

GET #DATADRIVEN

THE DATA-DRIVEN
FUTURE

Data-Driven
Marketing

Data Driven
Business



Introductory Example

$$\text{Purchase} = -0.15 \cdot \text{Ad Exposure} + 0.6 \quad (R^2 = 0.02)$$

-0.15

$$\text{Purchase} = 0.05 \cdot \text{Ad Exposure} + 0.4 \cdot \text{Gender} + 0.3 \quad (R^2 = 0.14)$$


+0.05

$$\text{Purchase} = -0.2 \cdot \text{Ad Exposure} - 0.1 \cdot \text{Test Drive} + 0.67 \quad (R^2 = 0.03)$$

-0.2

$$\text{Purchase} = 0.001 \cdot \text{Ad Exposure} + 0.4 \cdot \text{Gender} - 0.1 \cdot \text{Test Drive} + 0.37 \quad (R^2 = 0.15)$$

≈ 0


$$y = f(x)$$

Observational vs. Causal Inference

Observational Inference (Prediction)

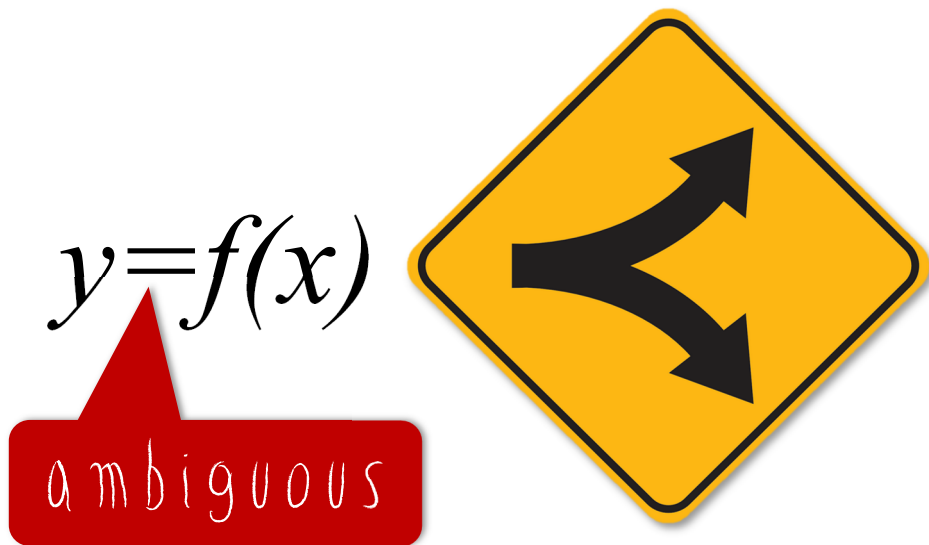
$$y = f(\textit{see}(x))$$

“given that I **see**”

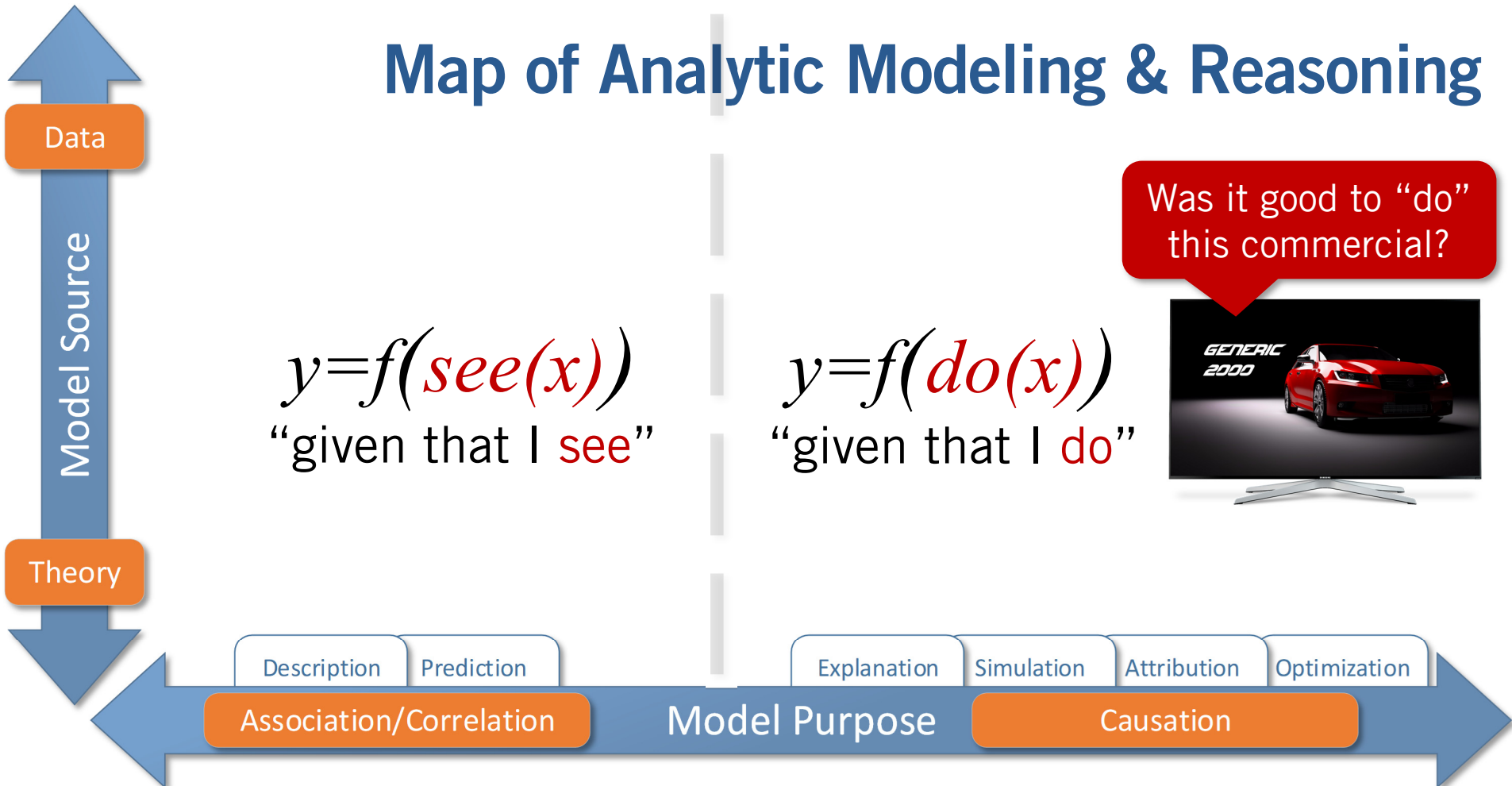
Causal Inference (Intervention)

$$y = f(\textit{do}(x))$$

“given that I **do**”



Map of Analytic Modeling & Reasoning



So, what's the advertising effect?

"given that I see"

Test Drive	Gender	Ad Exposure	Purchase
No	Male	No	30%
		Yes	40%
	Female	No	70%
		Yes	80%
Yes	Male	No	30%
		Yes	20%
	Female	No	70%
		Yes	60%

≈ 0

"given that I see"

Test Drive	Ad Exposure	Purchase
No	No	60%
	Yes	50%
Yes	No	60%
	Yes	30%

-0.2

"given that I see"

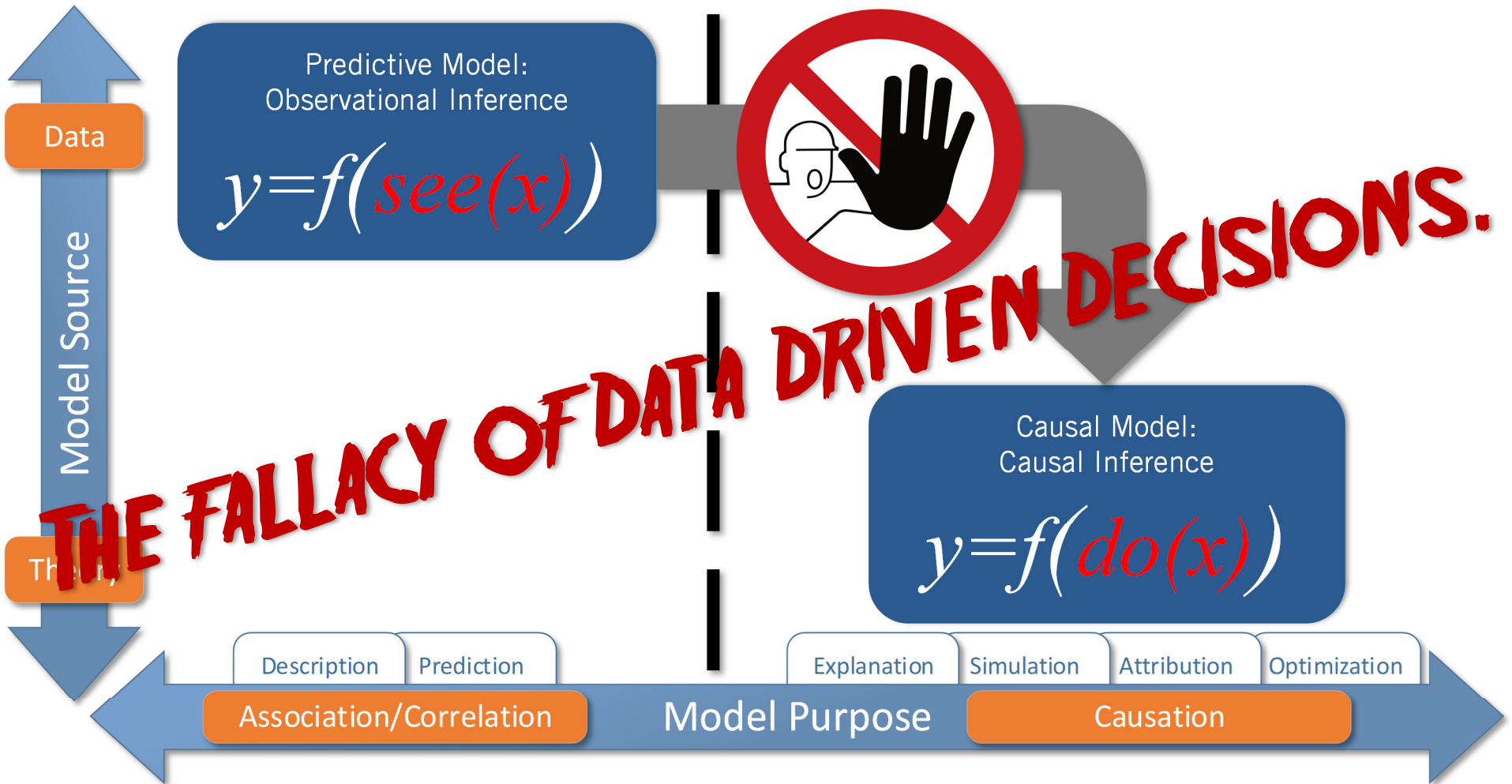
Gender	Ad Exposure	Purchase
Male	No	30%
	Yes	35%
Female	No	70%
	Yes	75%

$+0.05$

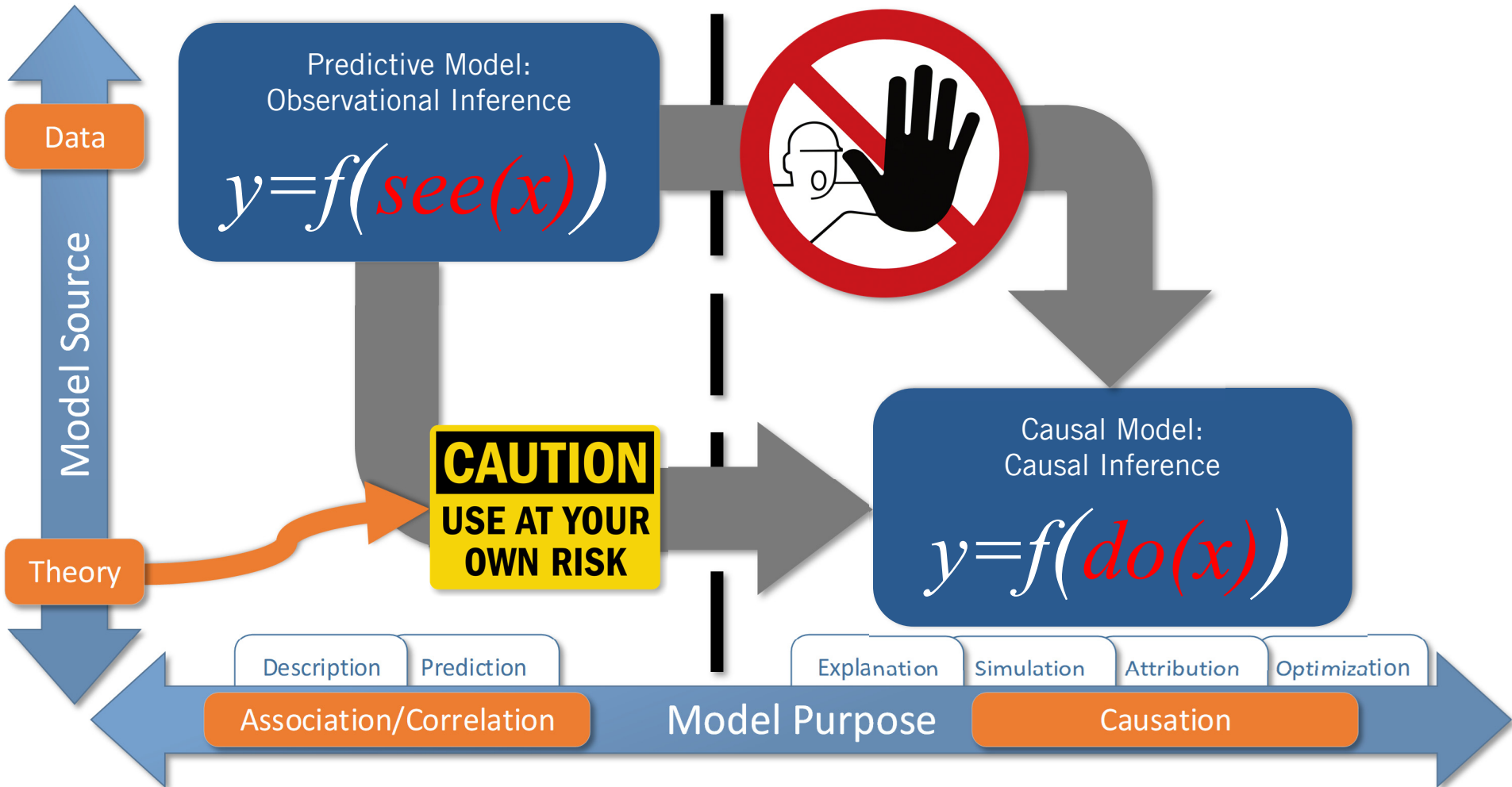
Ad Exposure	Purchase
No	60%
Yes	45%

-0.15

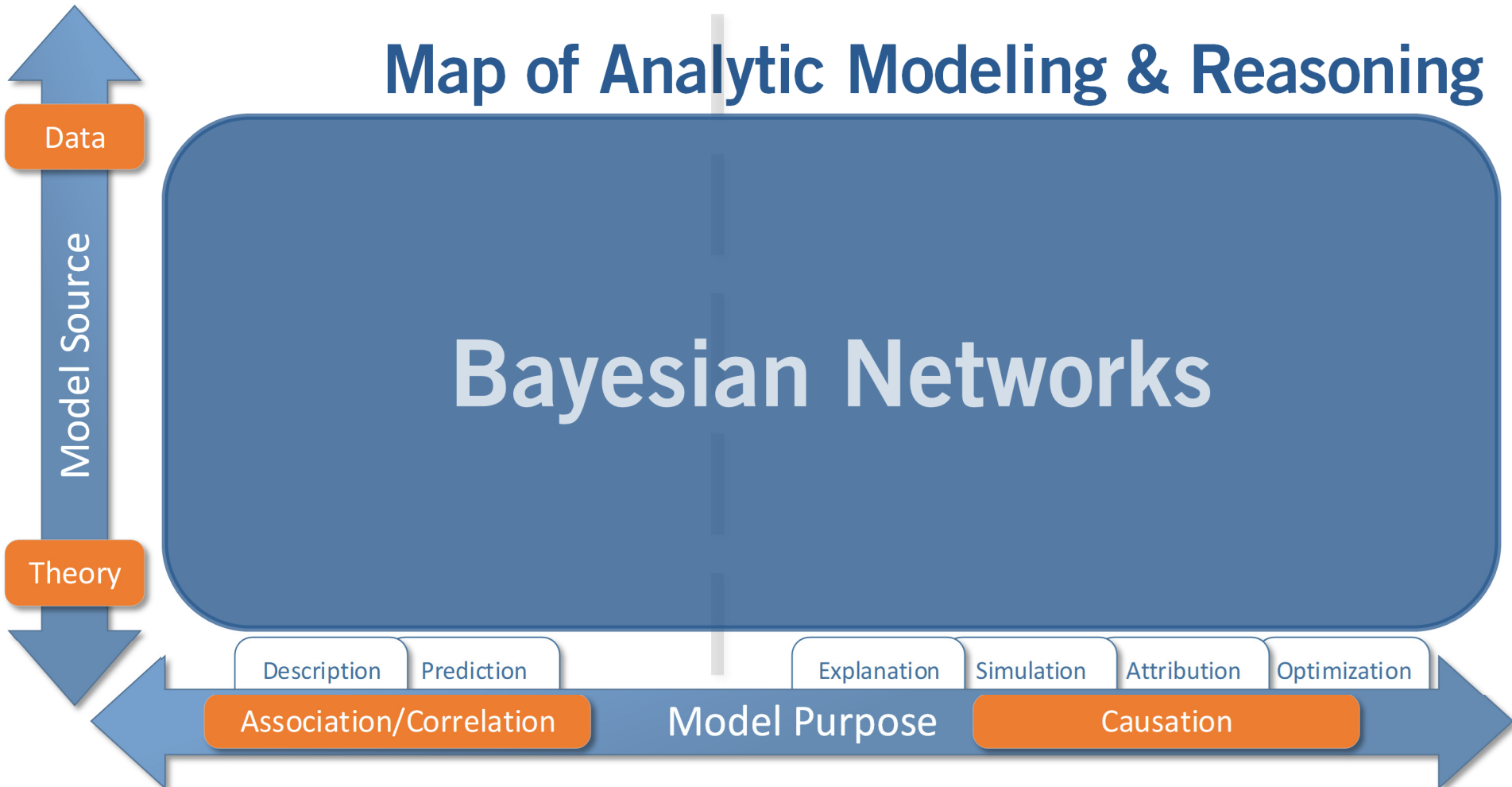
"given that I see"



Once upon a time. . .



Map of Analytic Modeling & Reasoning



Introductory Example

Develop Theory

What's the story here?



Gender



Ad Exposure



Test Drive



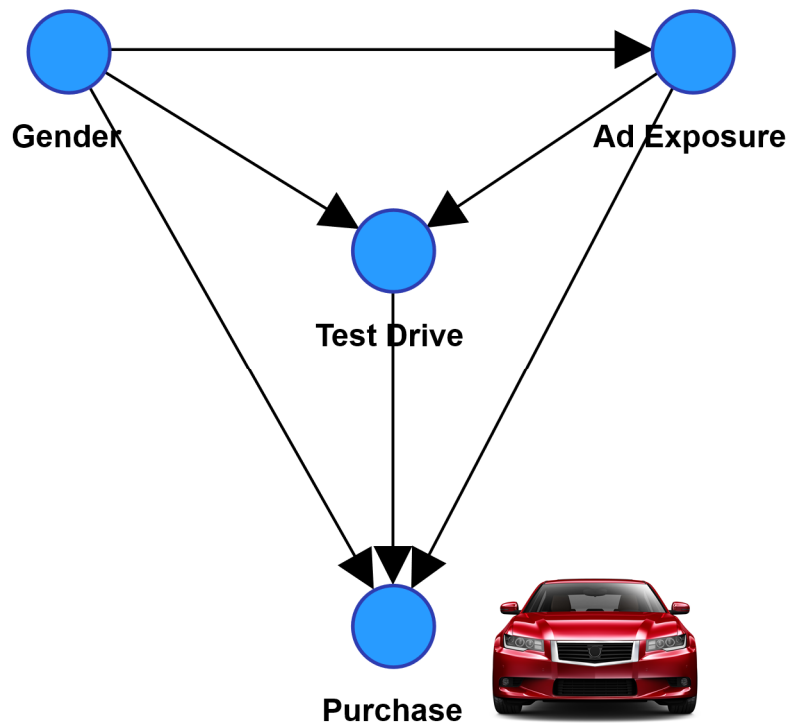
Purchase



Introductory Example

Our Theory!

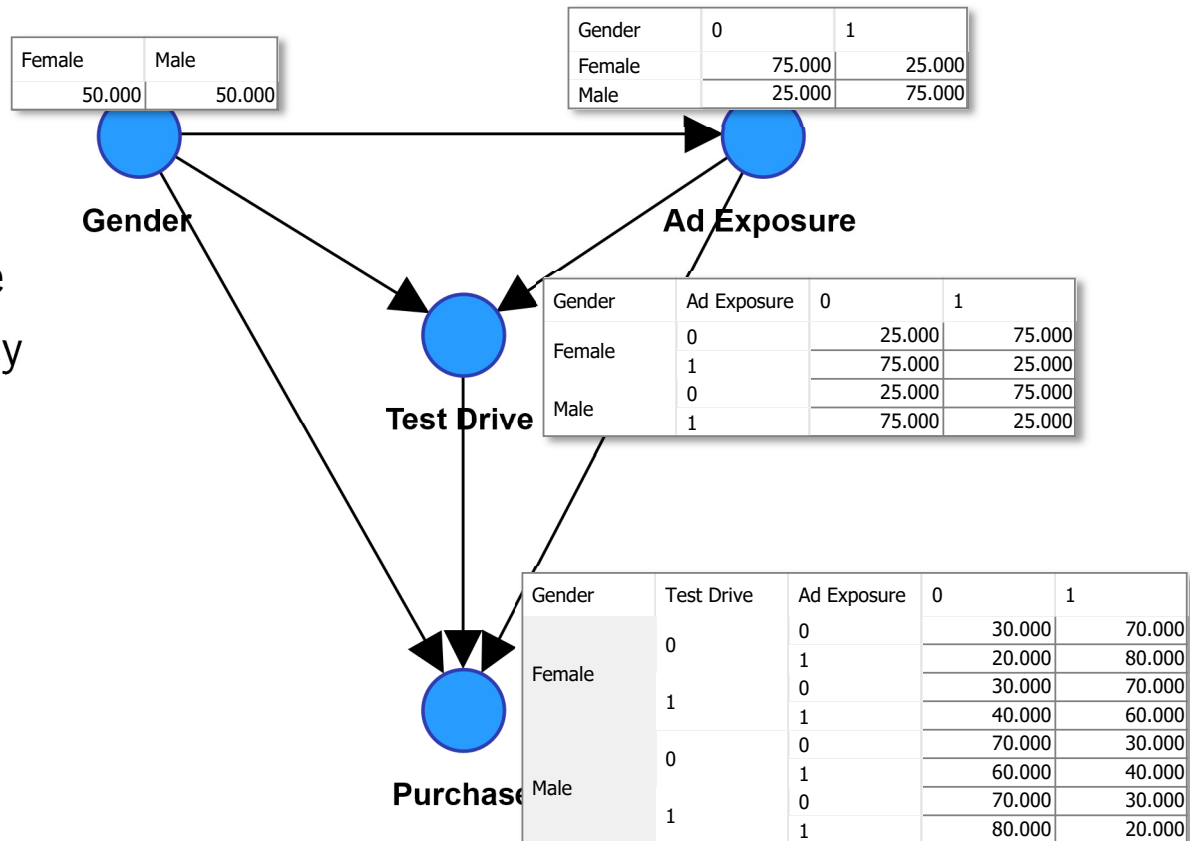
That's the story! Now we have the qualitative part of a causal Bayesian network.



Introductory Example

“Parameters”

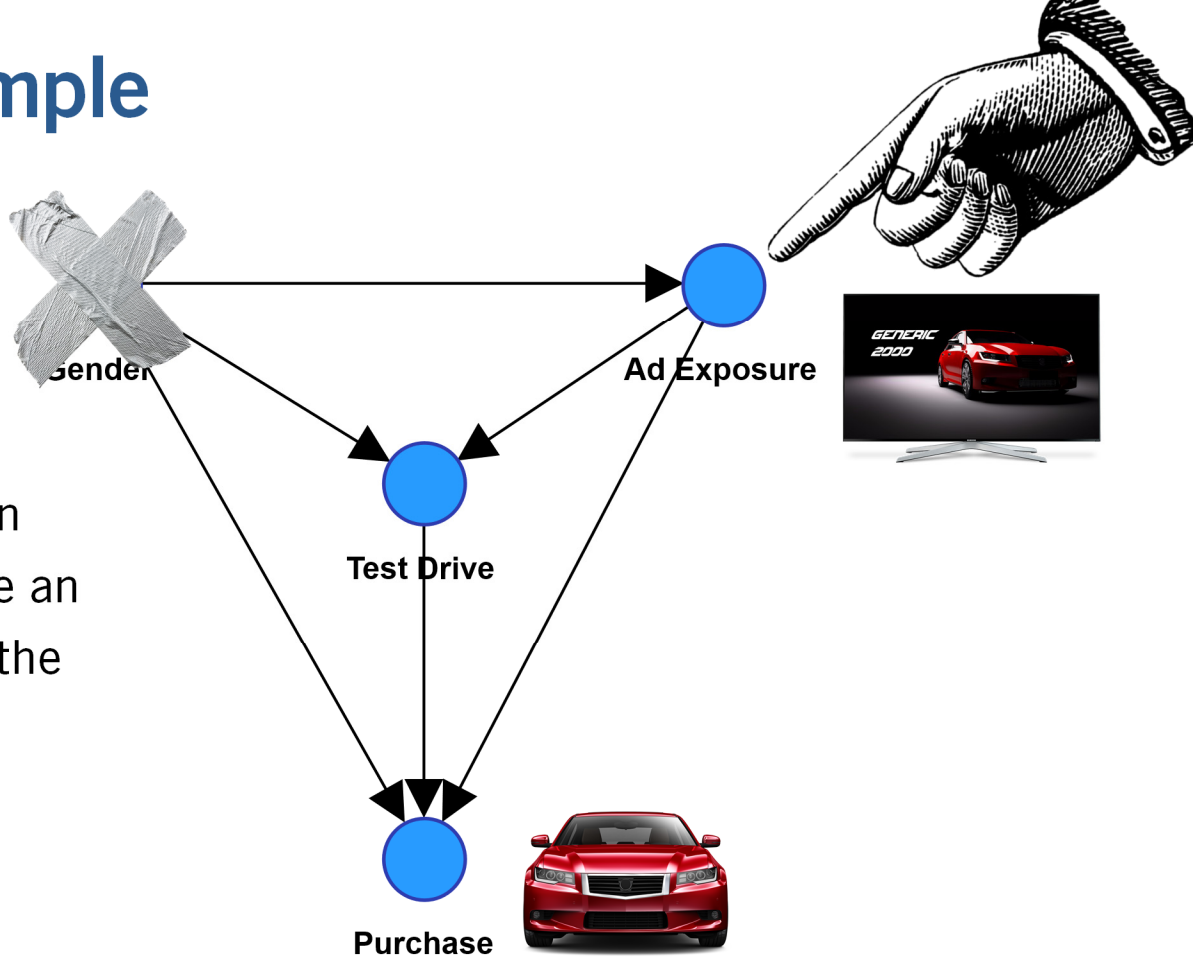
- We can estimate the quantitative part of the network from the survey data.
- As a result, we have a Bayesian network, which we can use for inference.



Introductory Example

Our “Model of the World”

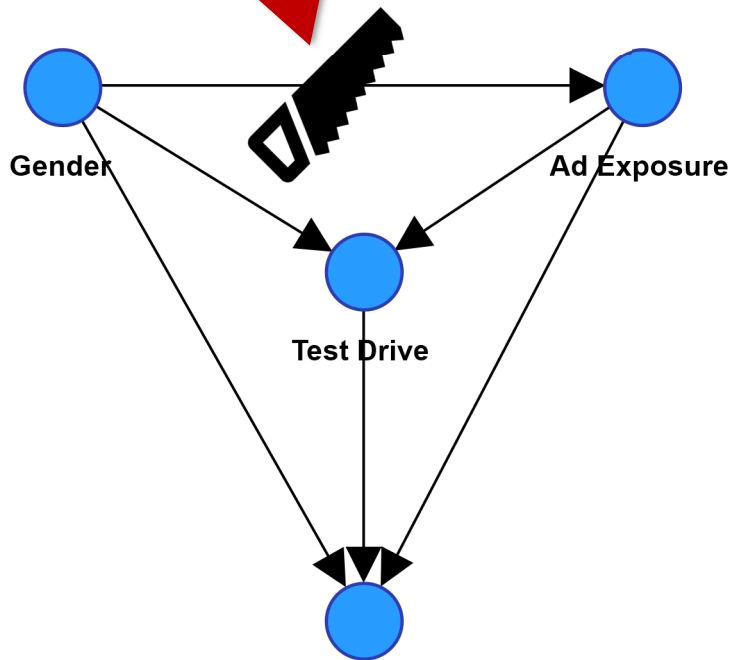
- How can we obtain the effect of Ad Exposure?
- With this causal Bayesian network, we can simulate an intervention to estimate the causal effect.



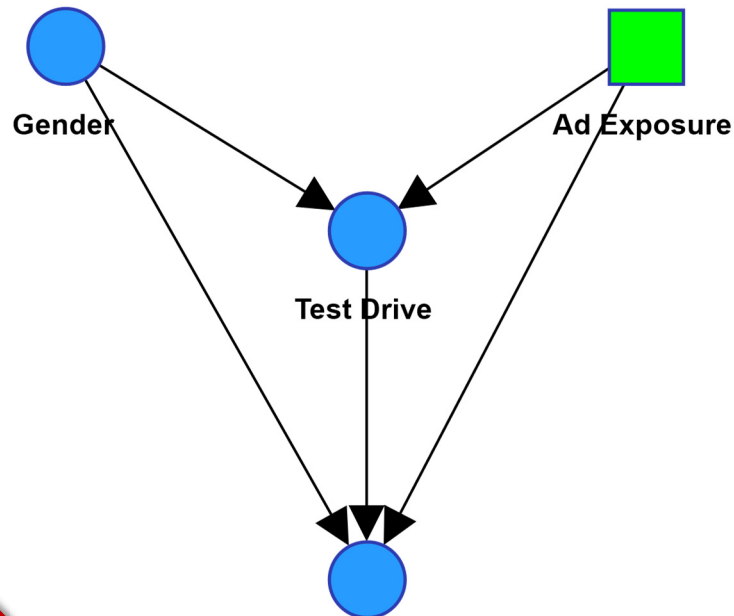
Introductory Example

Causal Model → Intervening an Intervention

“Graph Surgery”



Causal Model

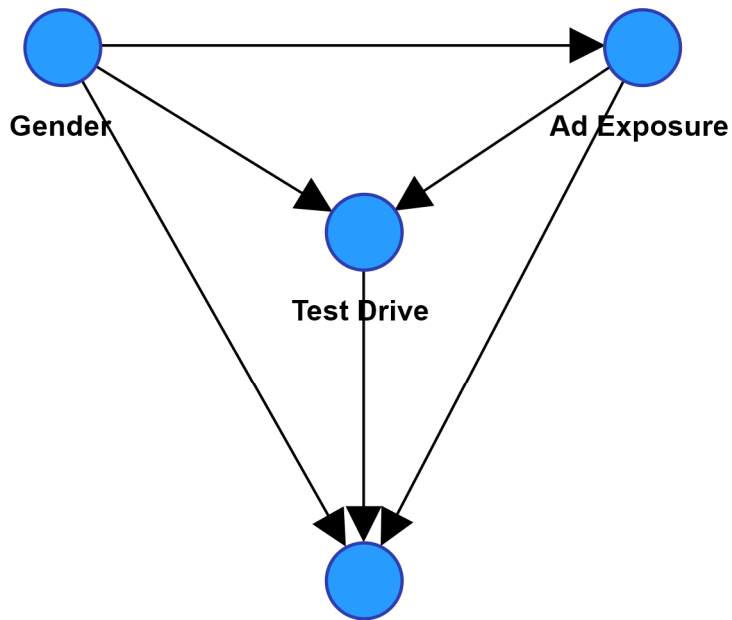
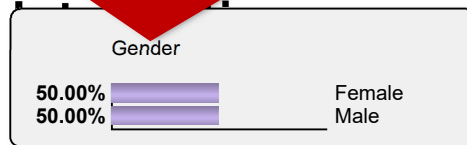
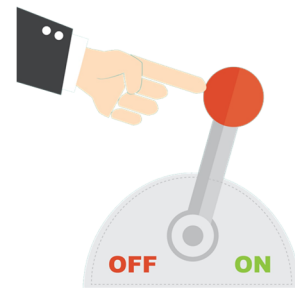


Intervention Model

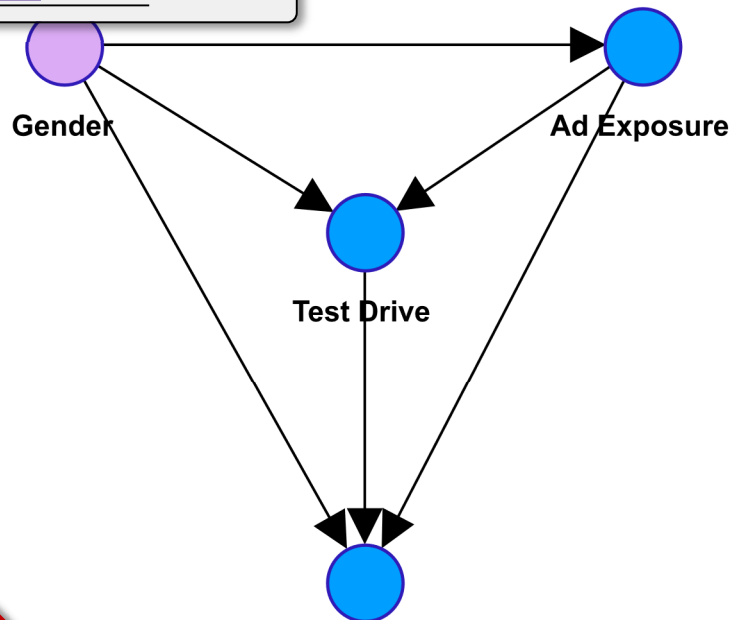
Introductory Example

Causal Inference: Simulating an

Fix Probabilities with
Likelihood Matching



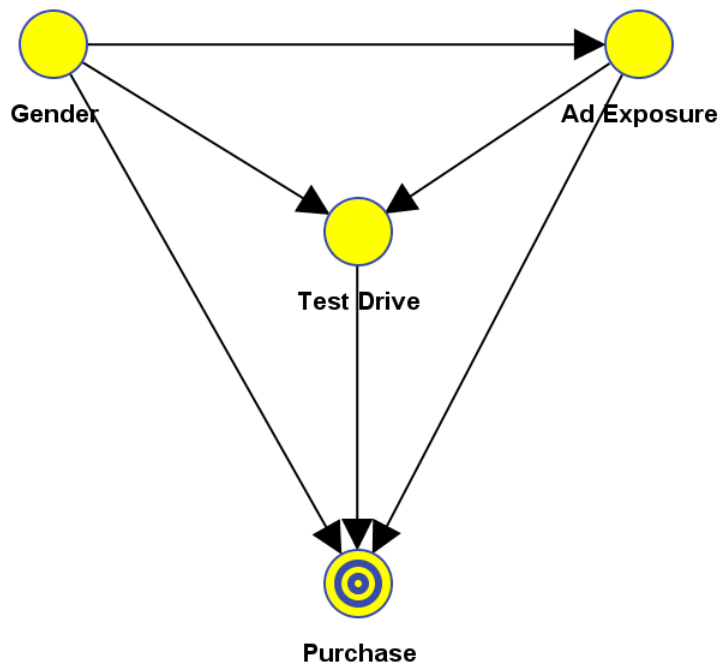
Causal Model



Intervention Model



DGP2.xbl *



Joint Probability: 100.00%
Log-Loss: 0
Cases: 100,000
Total Value: 1.525
Mean Value: 0.508

Gender

50.00%
50.00%



Intervention Node

Ad Exposure

Mean: 0.500 Dev: 0.500
Value: 0.500

50.00%
50.00%



Test Drive

Mean: 0.500 Dev: 0.500
Value: 0.500

50.00%
50.00%



Purchase

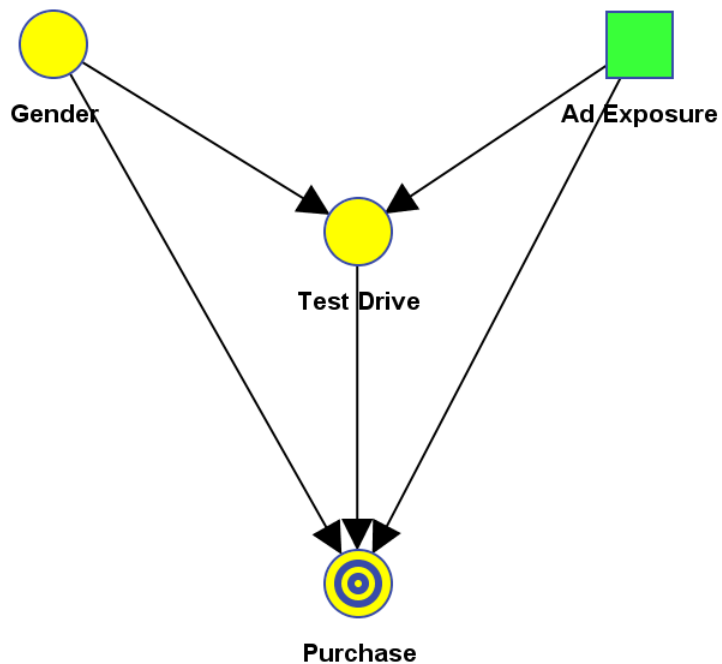
Mean: 0.525 Dev: 0.499
Value: 0.525

47.50%
52.50%





DGP2.xbl *



Joint Probability: 50.00%
Log-Loss: 1
Cases: 50,000
Total Value: 1.250
Mean Value: 0.417

Gender

50.00%
50.00%



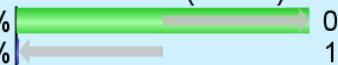
Female

Intervention

Ad Exposure

Mean: 0.000 Dev: 0.000
Value: 0.000 (-0.500)

100.00%
0.00%



0

1

Test Drive

Mean: 0.750 Dev: 0.433
Value: 0.750 (+0.250)

25.00%
75.00%



0

1

Purchase

Mean: 0.500 Dev: 0.500
Value: 0.500 (-0.025)

50.00%
50.00%

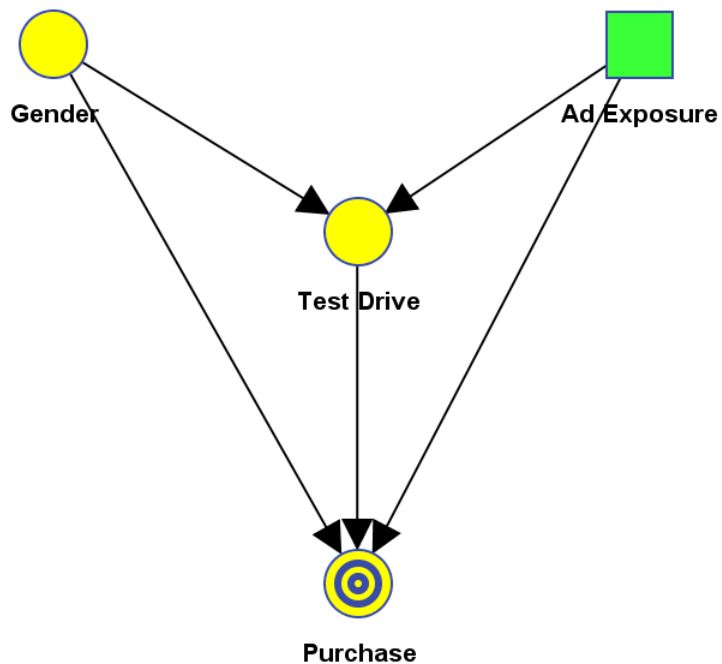


0

1



DGP2.xbl *



Joint Probability: 50.00%
Log-Loss: 1
Cases: 50,000
Total Value: 1.800
Mean Value: 0.600

Gender

50.00%
50.00%



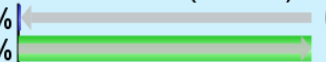
Female

Intervention

Ad Exposure

Mean: 1.000 Dev: 0.000
Value: 1.000 (+1.000)

0.00%
100.00%



0
1

Test Drive

Mean: 0.250 Dev: 0.433
Value: 0.250 (-0.500)

75.00%
25.00%



Effect

Purchase

Mean: 0.550 Dev: 0.497
Value: 0.550 (+0.050)

45.00%
55.00%



0
1

So, what's the advertising effect?

Test Drive	Gender	Ad Exposure	Purchase
No	Male	No	30%
		Yes	40%
	Female	No	70%
		Yes	80%
Yes	Male	No	30%
		Yes	20%
	Female	No	70%
		Yes	60%

≈ 0

Test Drive	Ad Exposure	Purchase
No	No	60%
	Yes	50%
Yes	No	60%
	Yes	30%

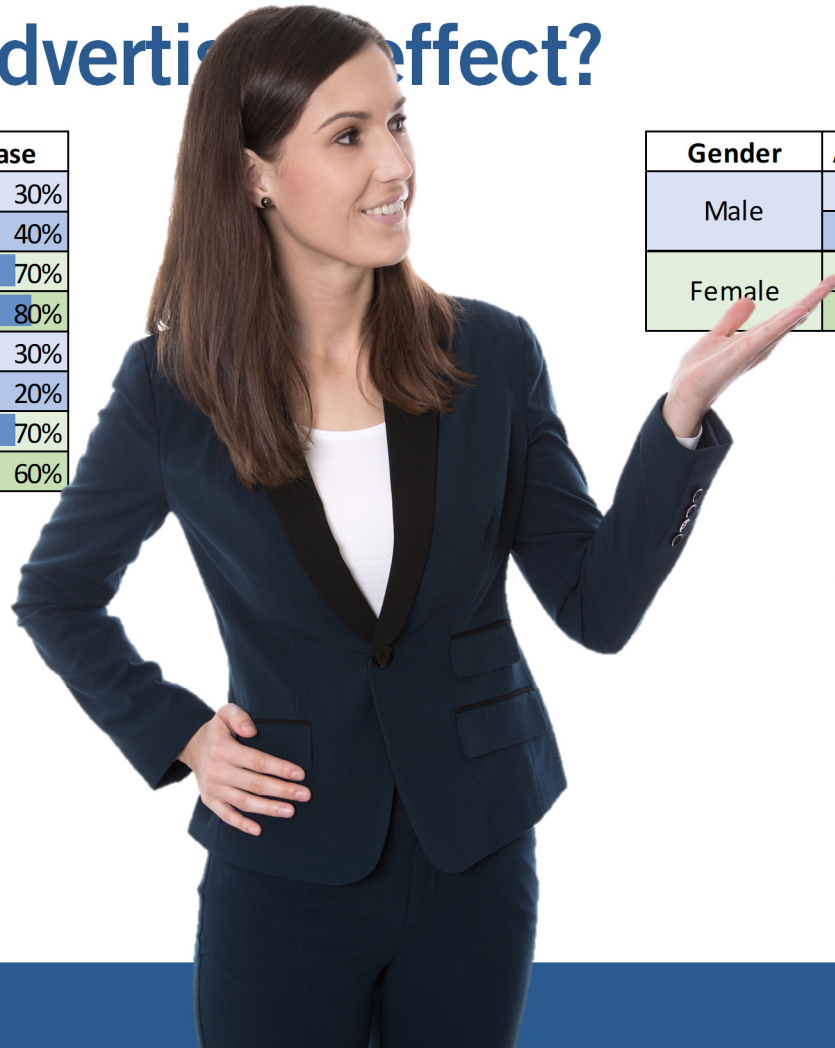
-0.2

Gender	Ad Exposure	Purchase
Male	No	30%
	Yes	35%
Female	No	70%
	Yes	75%

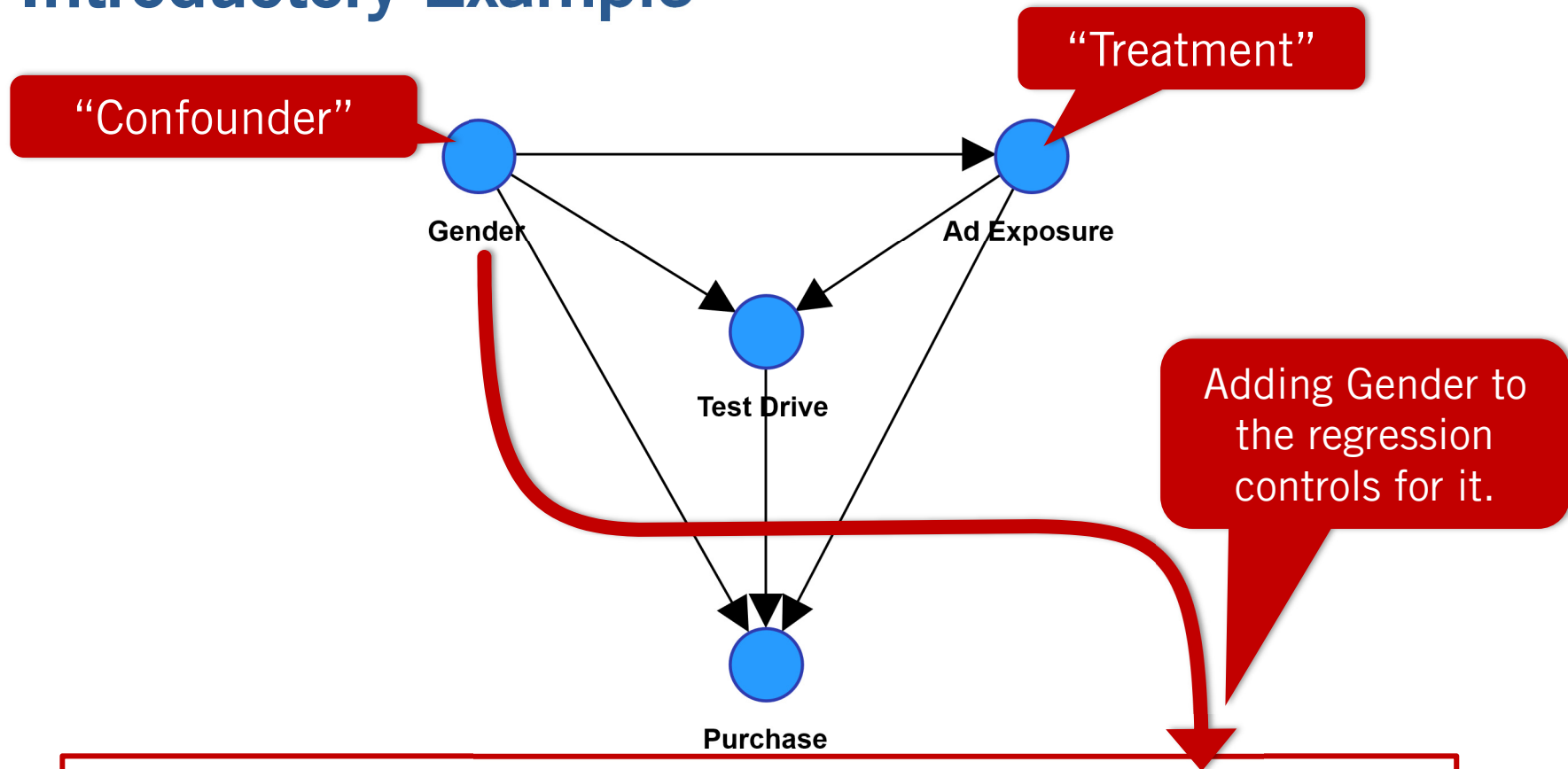
$+0.05$

Ad Exposure	Purchase
No	60%
Yes	45%

-0.15



Introductory Example



$$\text{Purchase} = 0.05 \cdot \text{Ad Exposure} + 0.4 \cdot \text{Gender} + 0.3$$

A row of cars, including a white sedan and several dark-colored SUVs, are parked in a lot. In the background is a large red wall with a yellow top section. The text 'ACME GENERIC' is written in large, stylized, italicized white letters, and 'AUTO CENTER' is written below it in smaller, italicized white letters.

ACME GENERIC

AUTO CENTER



NEWSPAPER

RADIO

TELEVISION

INTERNET

SUCCESS

METRICS



J. Wannamaker



H. Ford



J.C. Penney

I know I waste half of my advertising dollars; I just wish I knew which half.

Marketing Mix Optimization

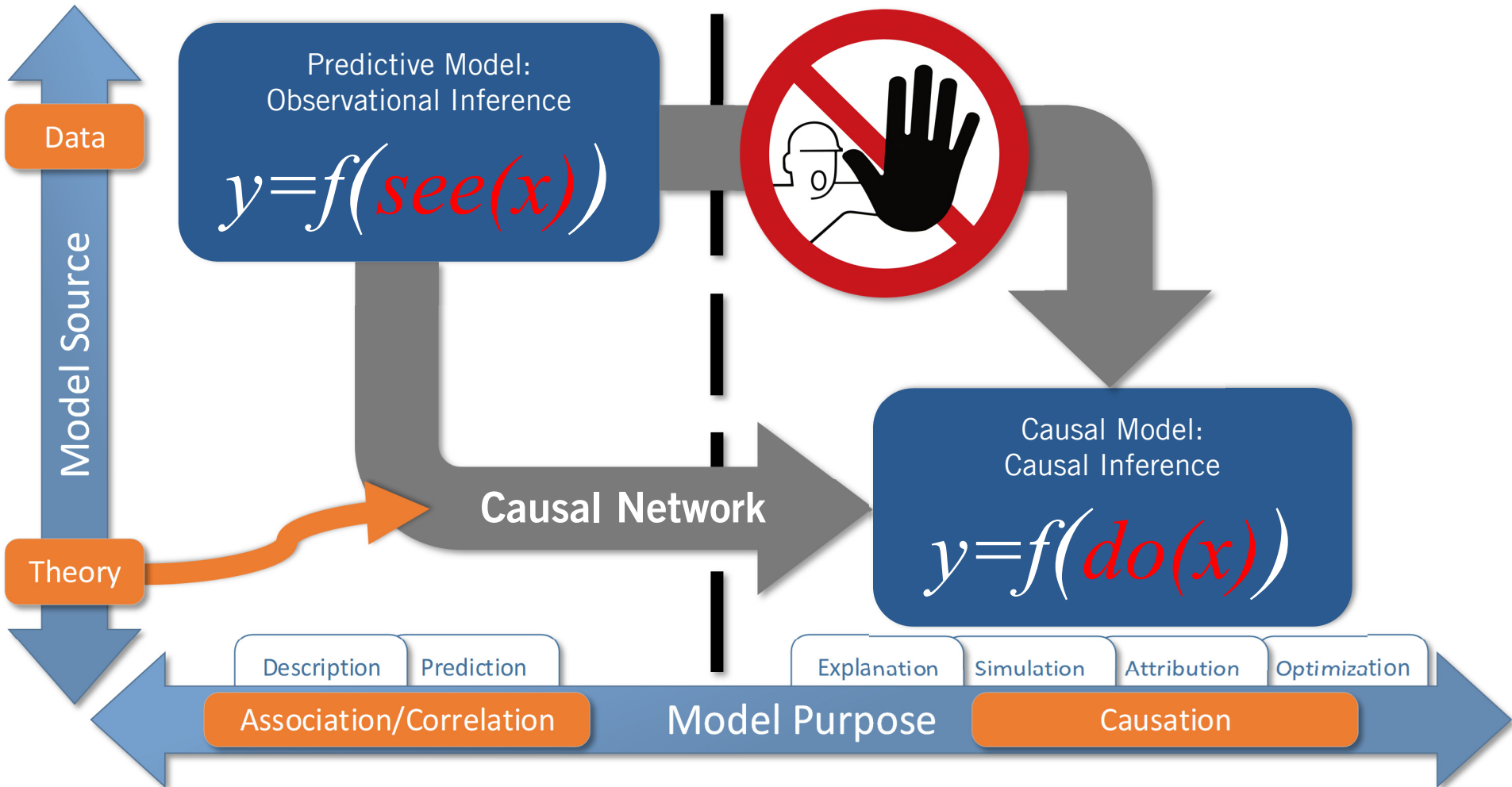


Objective

- Maximize sales within a given marketing budget.

Historical Sales & Media Data

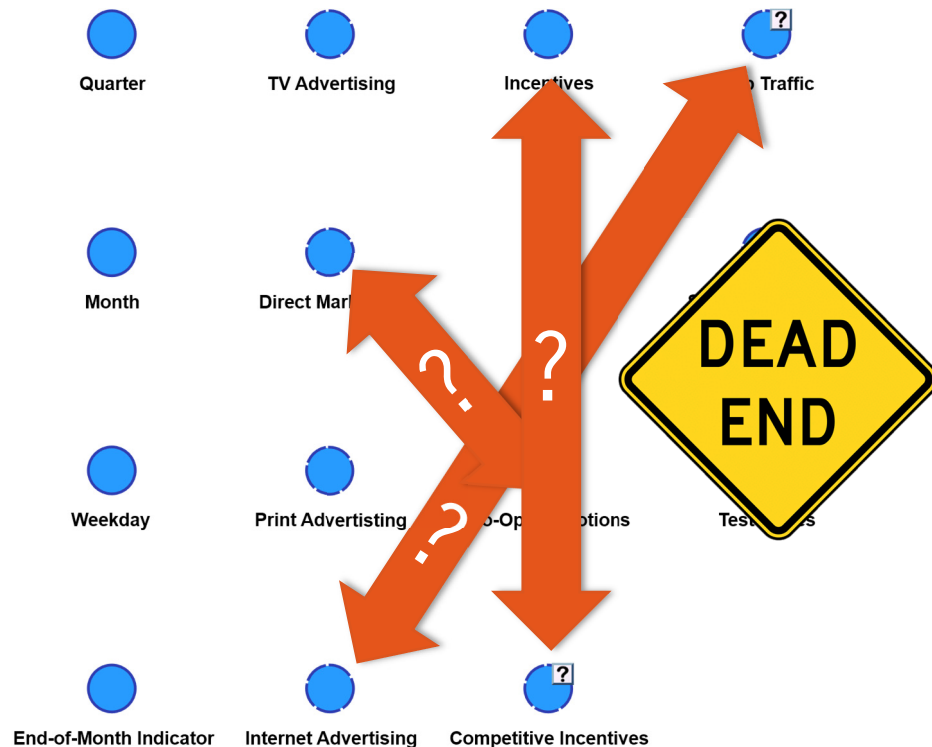
- Quarter
- Month
- Weekday
- End-of-Month Indicator
- TV Advertising
- Direct Marketing
- Print Advertising
- Internet Advertising
- Incentives
- Sales
- Co-Op Promotions
- Competitive Incentives
- Web Traffic
- Showroom Traffic
- Test Drives

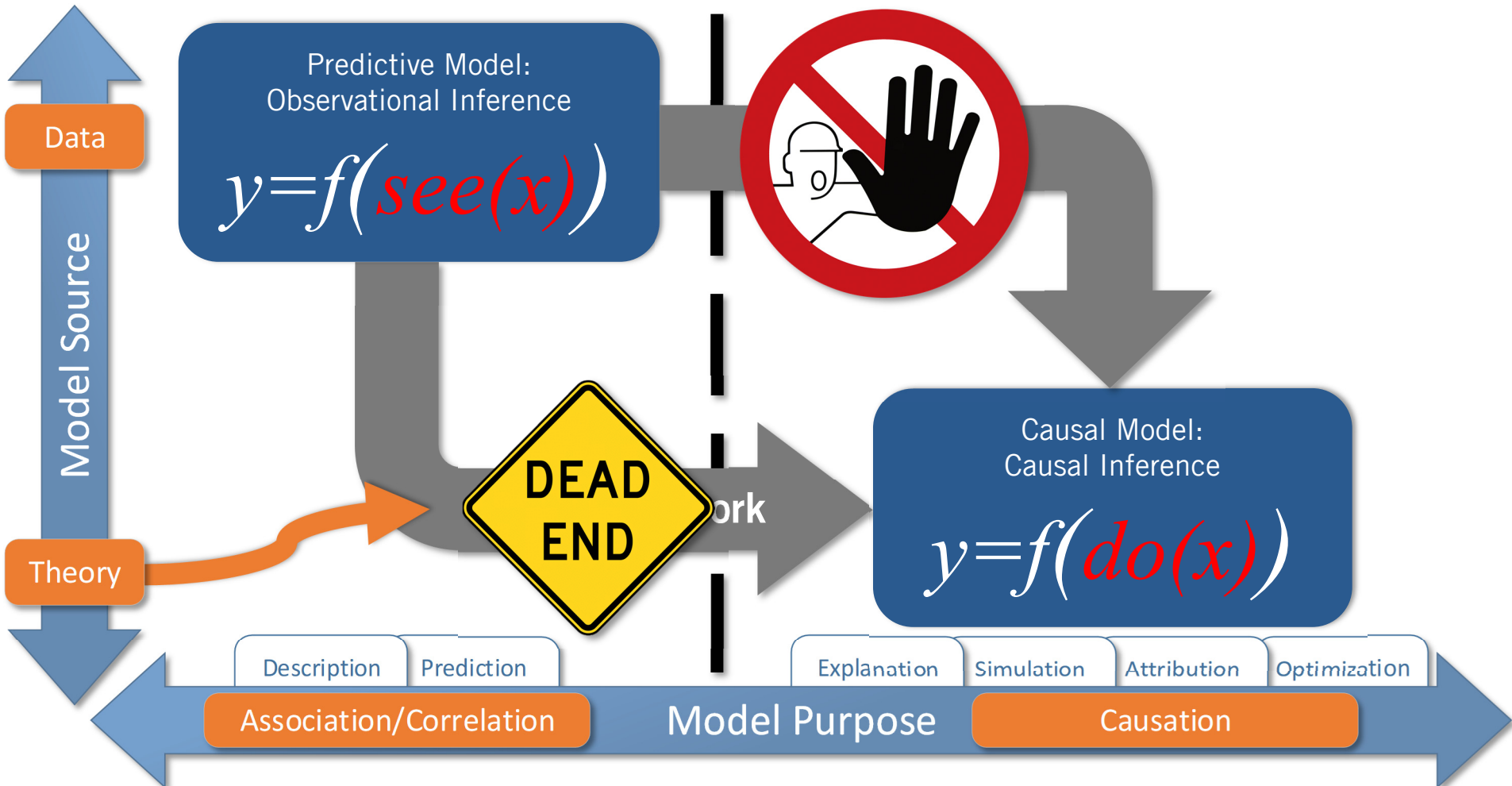


Marketing Mix Optimization


Causal Assumptions?

- Recall: Causal inference requires causal assumptions, e.g., a causal networks!
- But, given the number of variables, there are 2.38×10^{41} possible causal network graphs!
- Causal directions are not always obvious.





Now What?

**We need a different
kind of theory** 

Disjunctive Cause Criterion



NIH Public Access

Author Manuscript

Biometrics. Author manuscript; available in PMC 2012 December 1.

Published in final edited form as:

Biometrics. 2011 December ; 67(4): 1406–1413. doi:10.1111/j.1541-0420.2011.01619.x.

A new criterion for confounder selection

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Abstract

We propose a new criterion for confounder selection when the underlying causal structure is unknown and only limited knowledge is available. We assume all covariates being considered are pretreatment variables and that for each covariate it is known (i) whether the covariate is a cause of treatment, and (ii) whether the covariate is a cause of the outcome. The causal relationships the covariates have with one another is assumed unknown. We propose that control be made for any covariate that is either a cause of treatment or of the outcome or both. We show that irrespective of the actual underlying causal structure, if any subset of the observed covariates suffices to control

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Disjunctive Cause Criterion

VanderWeele and Shpitser (2011)

- “We propose that control be made for any [pre-treatment] **covariate** that is either a cause of **treatment** or of the **outcome** or both.”

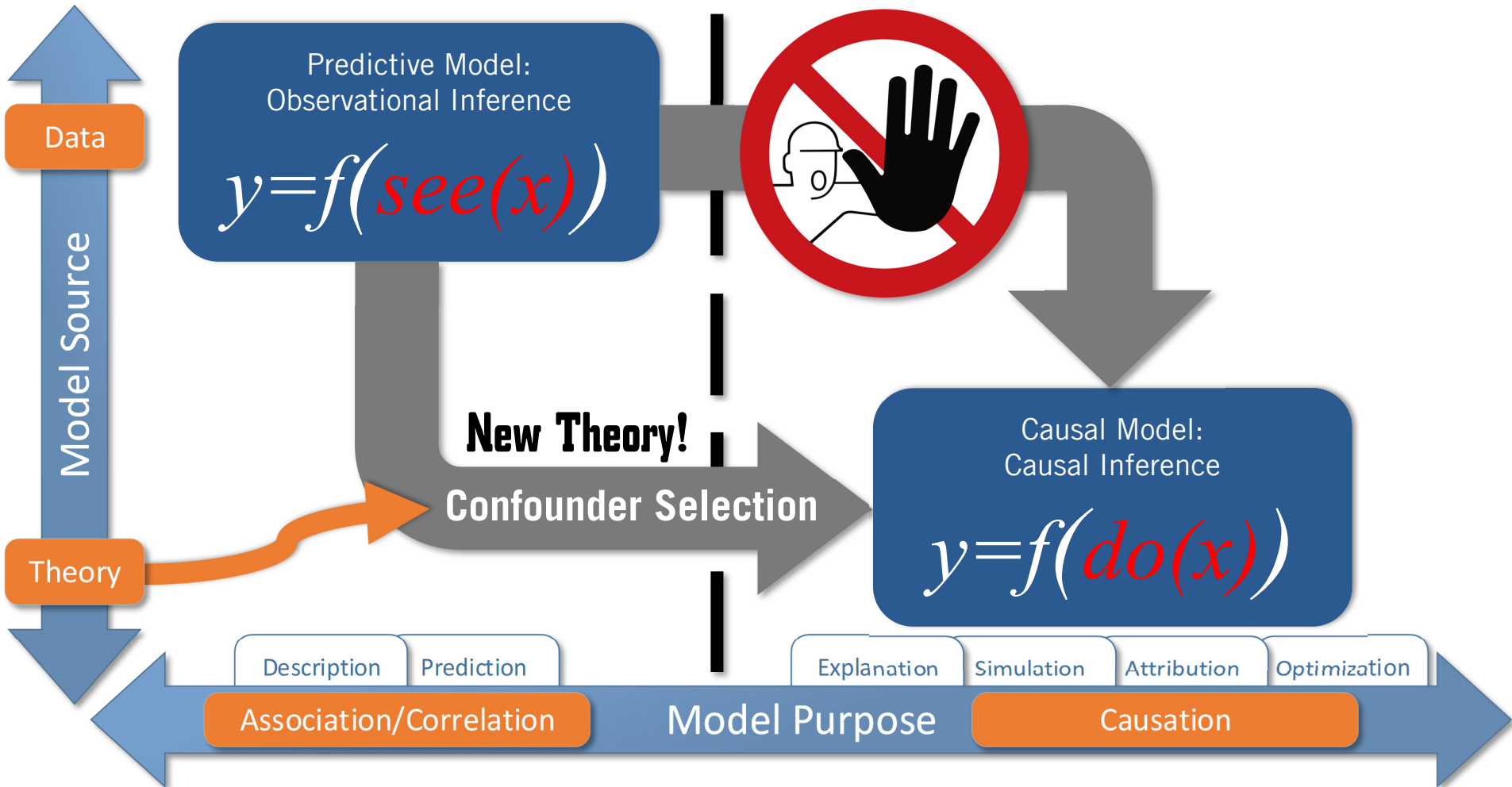
Confounder

Advertisement

Sales

Implementation in BayesiaLab:
Likelihood Matching on Confounders in
Direct Effects Analysis
→ Causal Effect, i.e., the Advertising Effect

**IMPORTANT ASSUMPTION:
NO UNOBSERVED CONFOUNDERS**



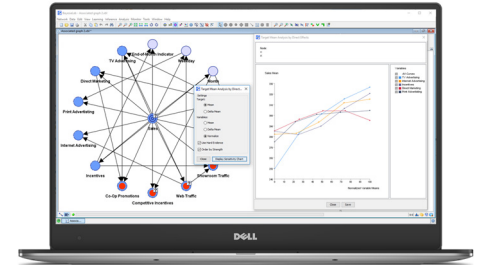
Marketing Mix Optimization

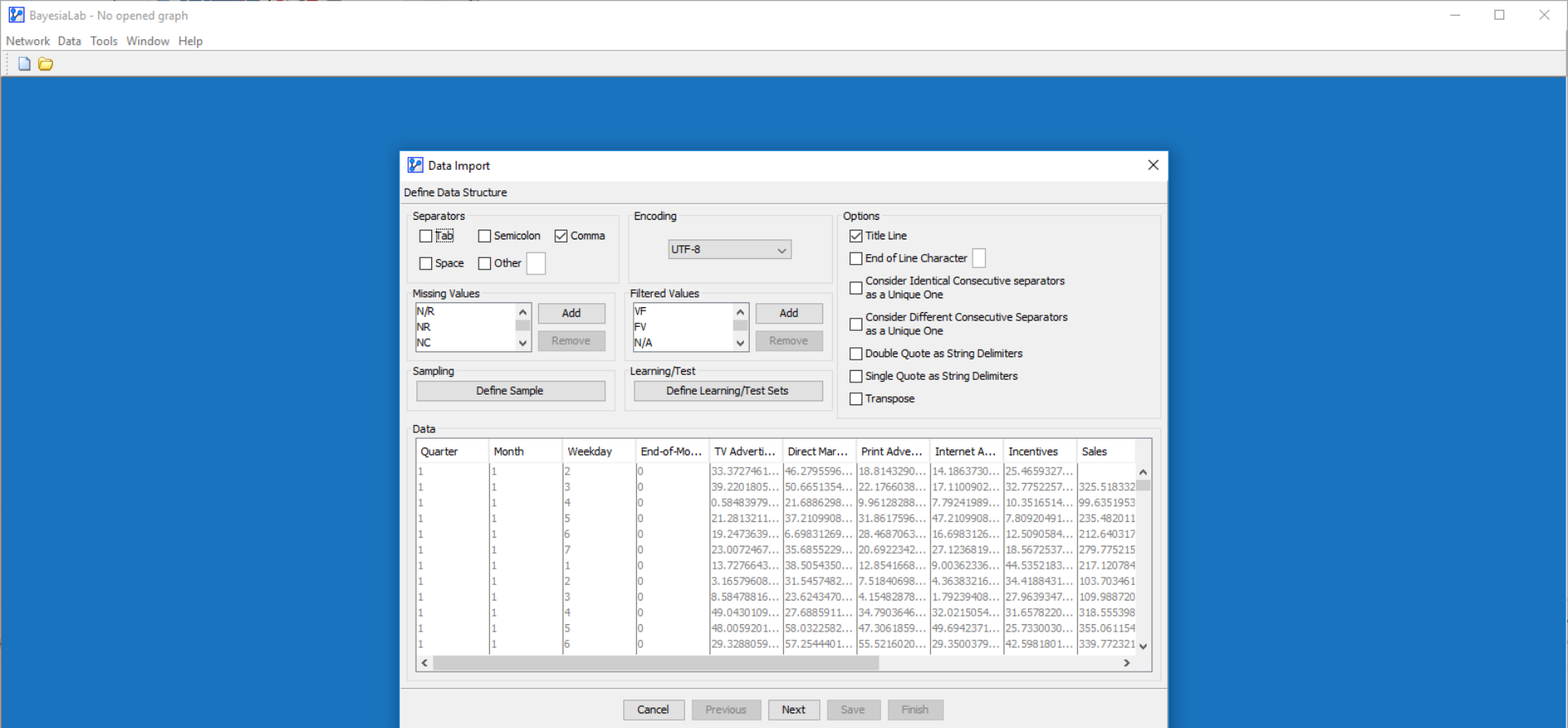


All Data is Synthetic

Proposed Workflow

- Import historical sales and marketing data.
- Machine-learn a predictive model with BayesiaLab.
- Determine **Confounders** vs. **Non-Confounders**, using the **Disjunctive Cause Criterion**.
- Estimate and evaluate **Direct Effects** response curves.
- Introduce **Function Node** and assign media costs.
- Perform **Genetic Target Optimization**.
- Apply **Network Temporalization**.
- Add **Constraint Nodes** between t and $t-1$ marketing variables.
- Perform **Genetic Target Optimization** on dynamic network.





Data Import Wizard



☐ Not Distributed
 ☒ Discrete
 ☐ Continuous
 ☐ Weight
 ☐ Learning/Test
 ☐ Row Identifier

Columns with Missing Values

All not Distributed

All Discrete

All Continuous

Number of Rows

16801

100.00%

Not Distributed

0

0.00%

Discrete

4

26.67%

Continuous

11

73.33%

Others

0

0.00%

Missing Values

6

0.00%

Filtered Values

0

0.00%

Quarter

Month

Weekday

End-of-Mo...

TV Adverti...

Direct Mar...

Print Adve...

Internet A...

Incentives

Sales

1	1	2	0	33.3727461...	46.2795596...	18.8143290...	14.1863730...	25.4659327...	325.518332
1	1	3	0	39.2201805...	50.6651354...	22.1766038...	17.1100902...	32.7752257...	99.6351953
1	1	4	0	0.58483979...	21.6886298...	9.96128288...	7.79241989...	10.3516514...	235.482011
1	1	5	0	21.2813211...	37.2109908...	31.8617596...	47.2109908...	7.80920491...	1212.640317
1	1	6	0	19.2473639...	6.69831269...	28.4687063...	16.6983126...	12.5090584...	279.775215
1	1	7	0	23.0072467...	35.6855229...	20.6922342...	27.1236819...	18.5672537...	217.120784
1	1	1	0	13.7276643...	38.5054350...	12.8541668...	9.00362336...	44.5352183...	103.703461
1	1	2	0	3.16579608...	31.5457482...	7.51840698...	4.36383216...	34.4188431...	27.9639347...
1	1	3	0	8.58478816...	23.6243470...	4.15482878...	1.79239408...	31.6578220...	318.555398
1	1	4	0	49.0430109...	27.6885911...	34.7903646...	32.0215054...	25.7330030...	355.061154
1	1	5	0	48.0059201...	58.0322582...	47.3061859...	49.6942371...	42.5981801...	339.772321
1	1	6	0	29.3288059...	57.2544401...	55.5216020...	29.3500379...	32.0630377...	48.8700524...
1	1	7	0	44.4346604...	43.2466044...	10.5580191...	32.0630377...	36.6784392...	287.837859
1	1	1	0	29.1636534...	54.5759953...	17.5206372...	12.6097153...		

Cancel

Previous

Next

Save

Finish

Variable Type Definition

Data Import

Data Selection and Filtering

Missing Value Processing

☐ Filter

☒ OR

☐ AND

☐ Replace by :

☐ Value

☐ Mean/Modal

☐ Infer

☐ Static Imputation

☐ Dynamic Imputation

☒ Structural EM

☐ Entropy-Based Static Imputation

☐ Entropy-Based Dynamic Imputation

Information

Number of Rows	16801	100.00%
Not Distributed	0	0.00%
Discrete	4	26.67%
Continuous	11	73.33%
Others	0	0.00%
Missing Values	6	0.00%
Filtered Values	0	0.00%

Select Values

☐ OR

☒ AND

Delete Selections

Display Selections

Data

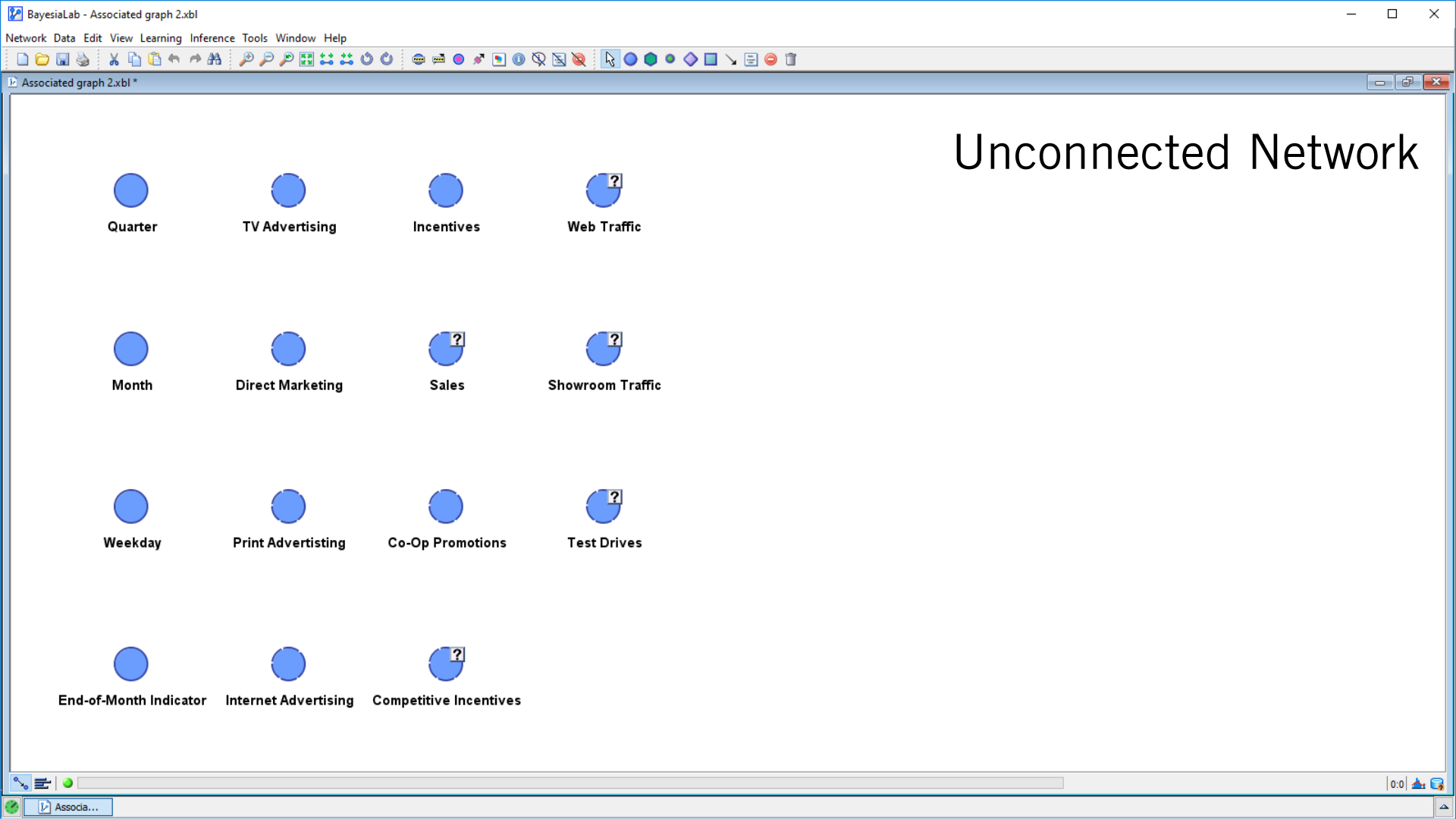
Quarter	Month	Weekday	End-of...	TV Adv...	Direct M...	Print Ad...	Interne...	Incentives	Sales
1	1	2	0	33.3727461...	46.2795596...	18.8143290...	14.1863730...	25.4659327...	
1	1	3	0	39.2201805...	50.6651354...	22.1766038...	17.1100902...	32.7752257...	325.518332
1	1	4	0	0.58483979...	21.6886298...	9.96128288...	7.79241989...	10.3516514...	99.6351953
1	1	5	0	21.2813211...	37.2109908...	31.8617596...	47.2109908...	7.80920491...	235.482011
1	1	6	0	19.2473639...	6.69831269...	28.4687063...	16.6983126...	12.5090584...	212.640317

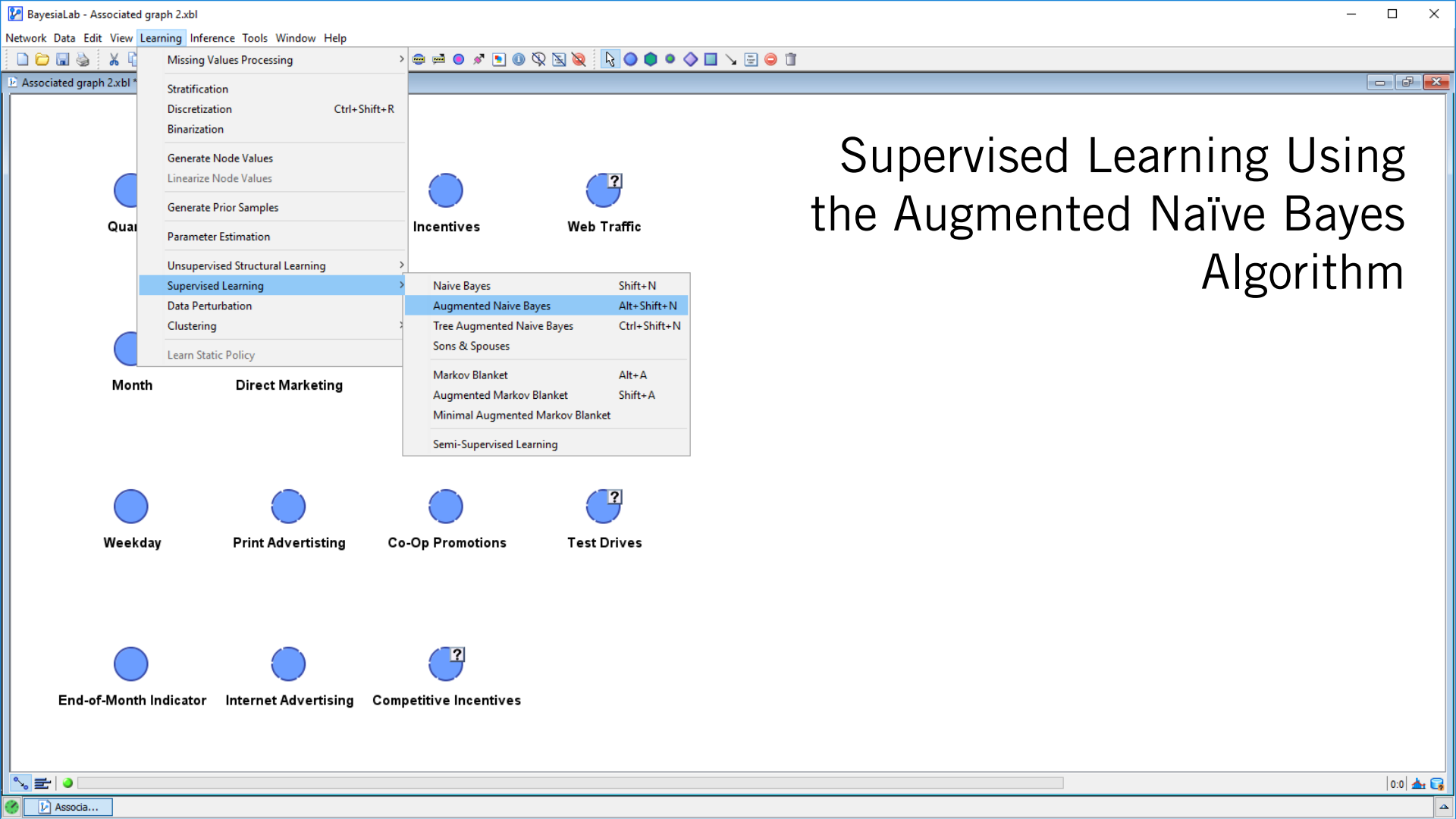
Select All Continuous Select All Discrete

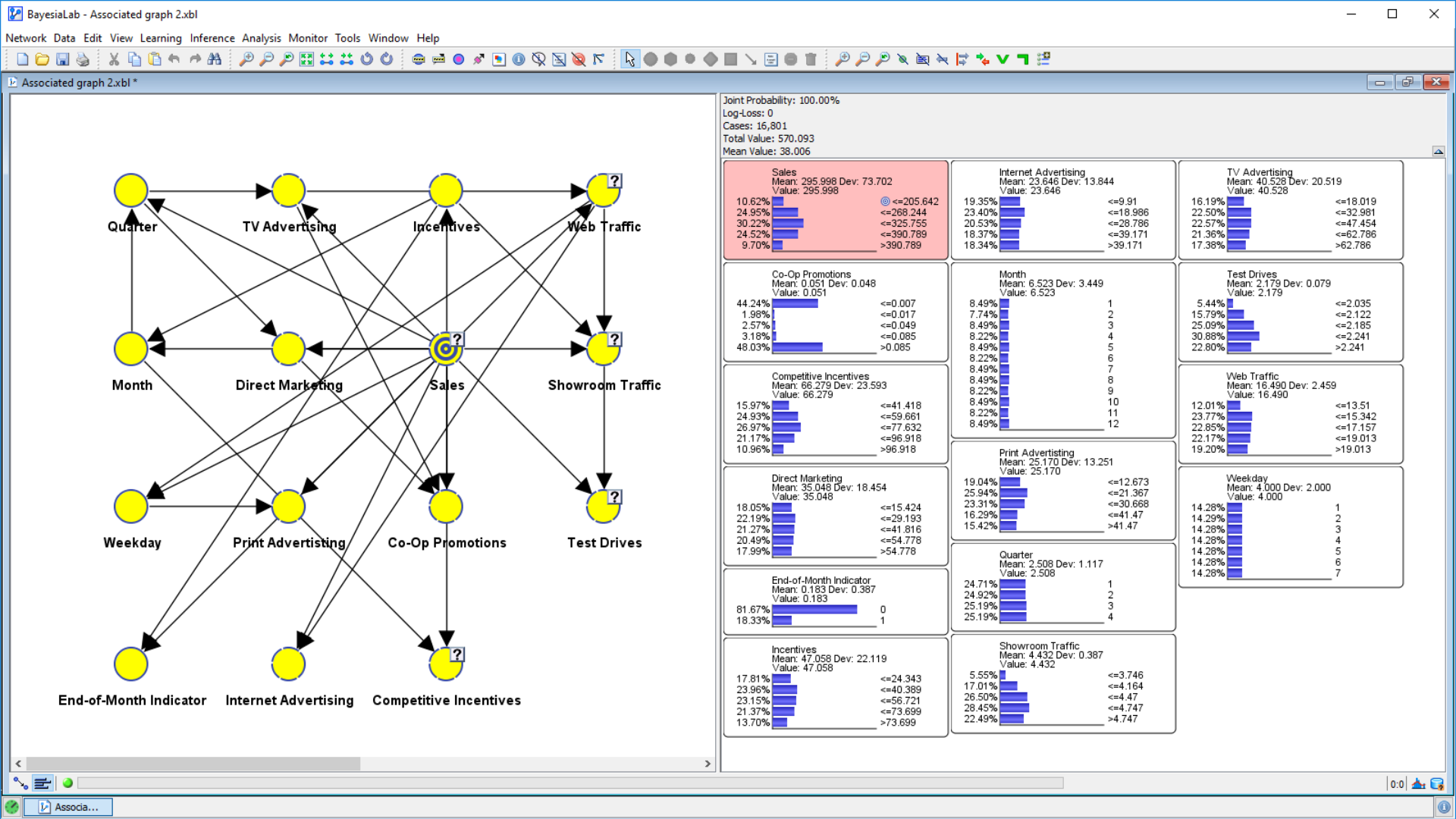
Cancel Previous **Next** Save Finish

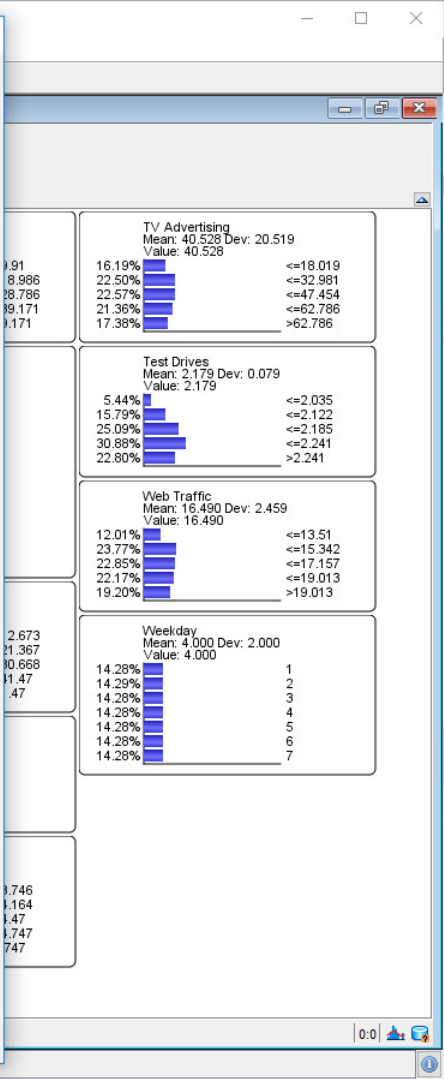
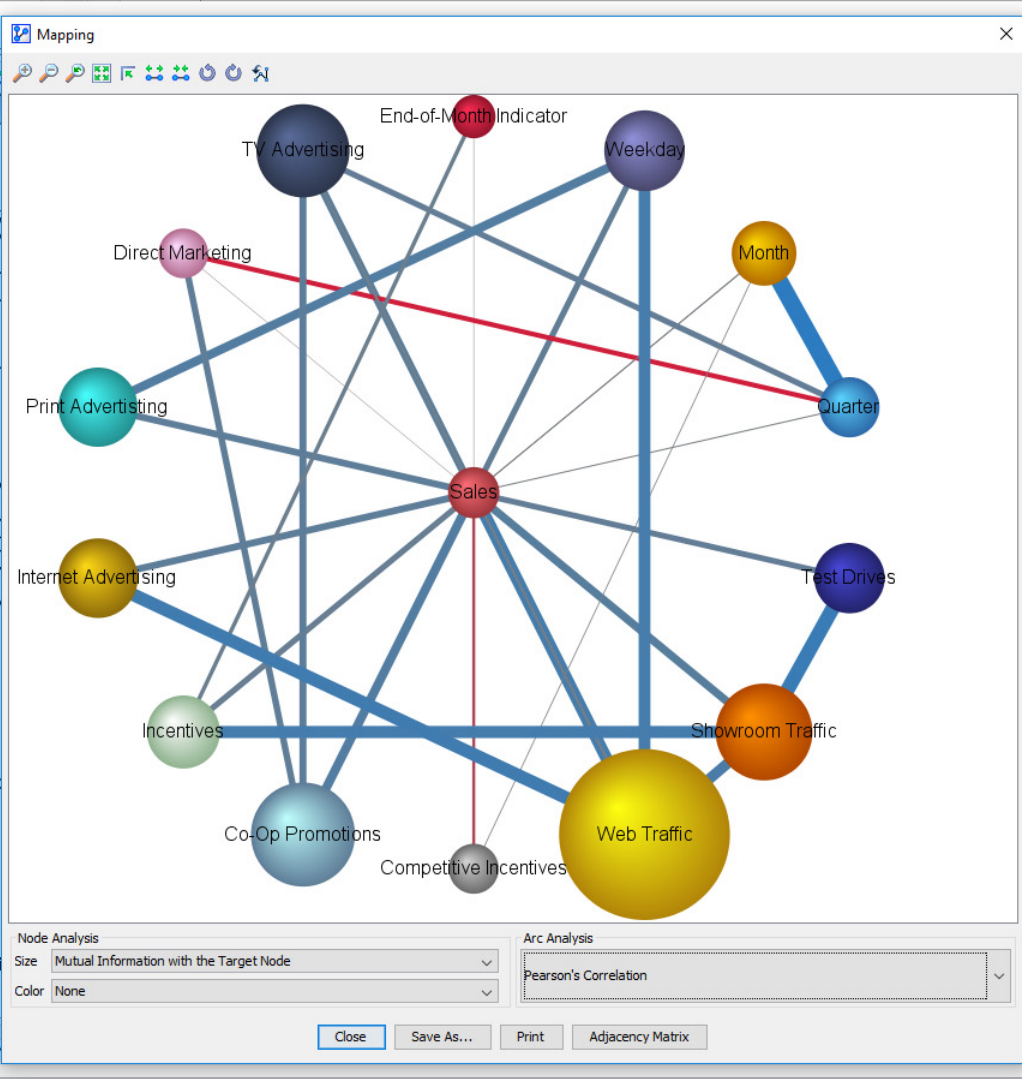
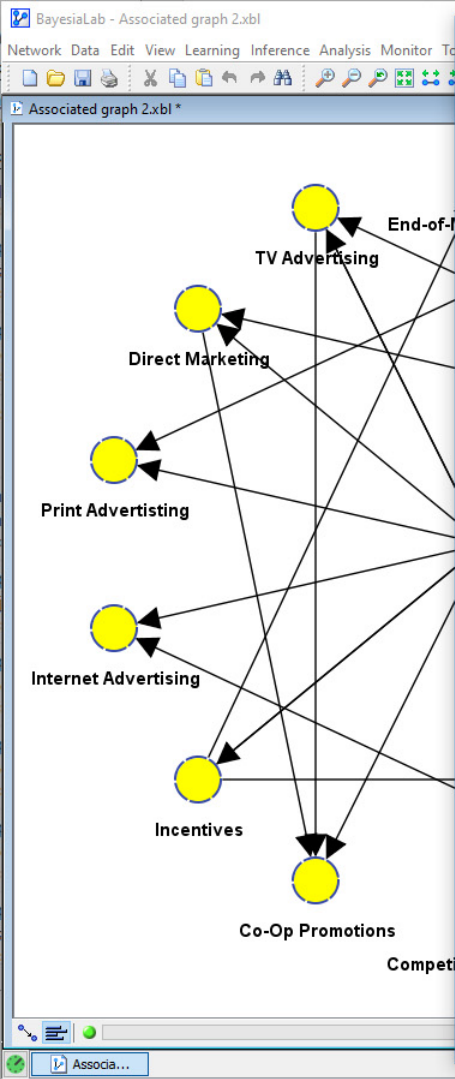
Missing Values Processing

Discretization



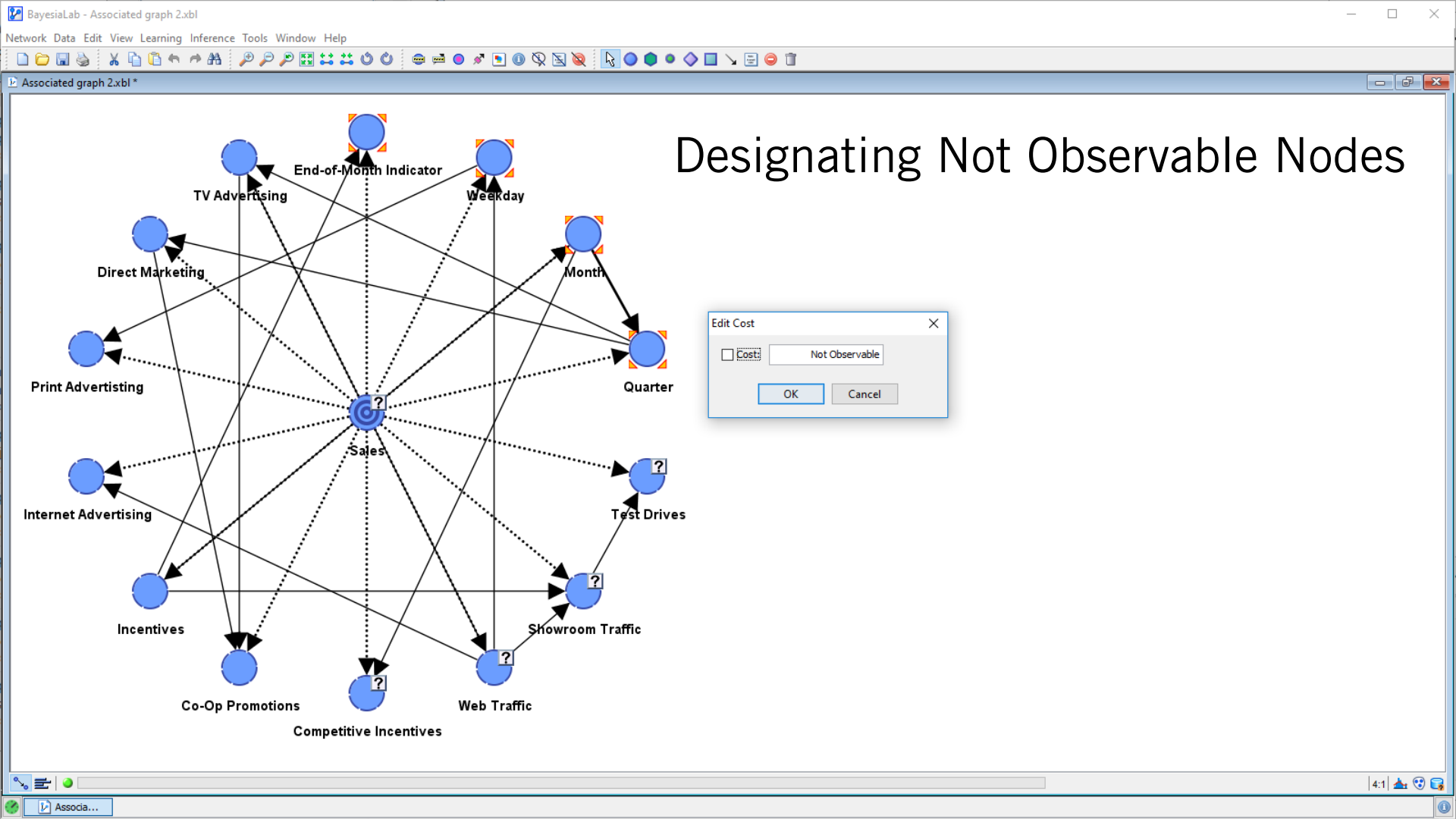


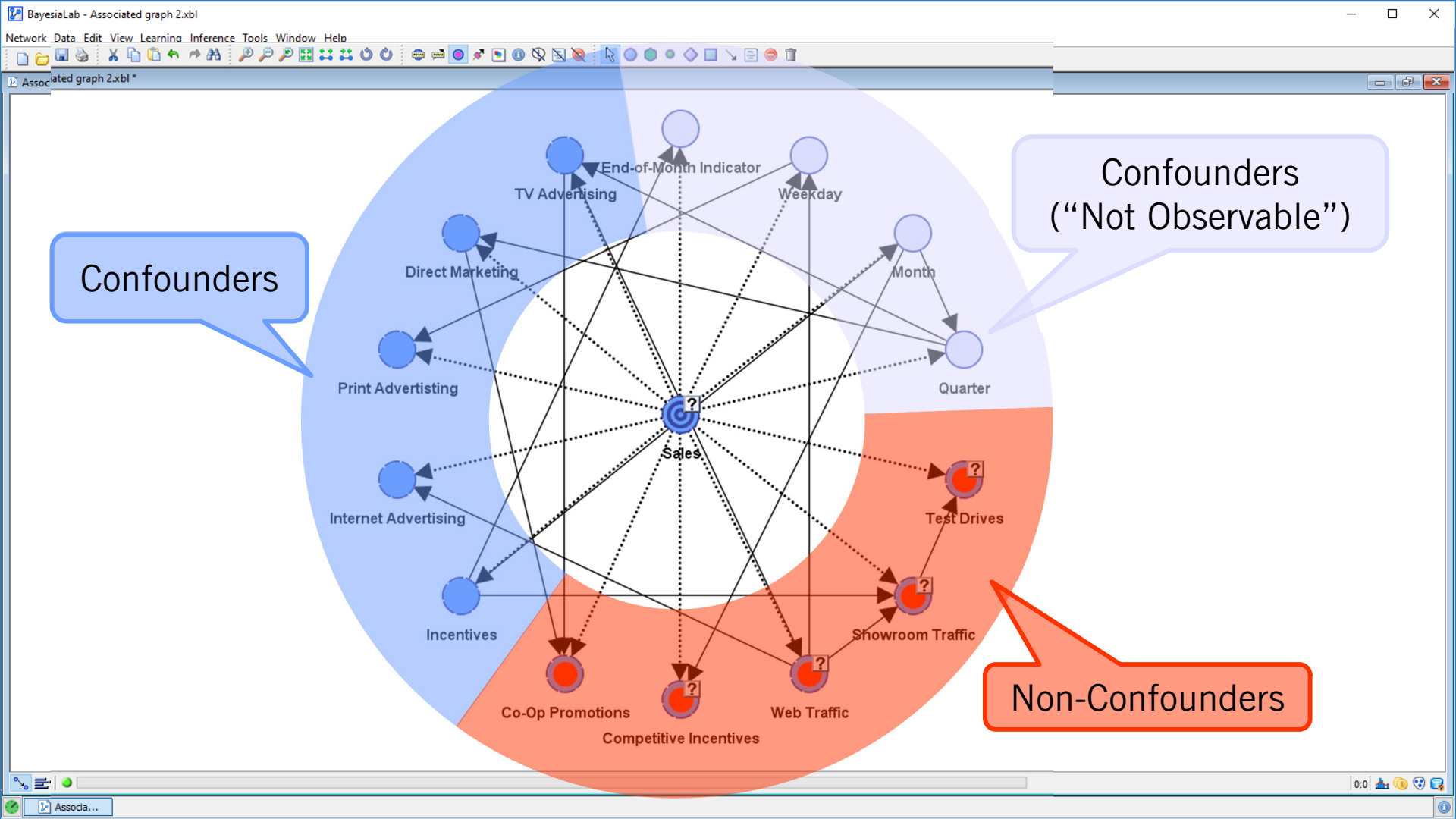




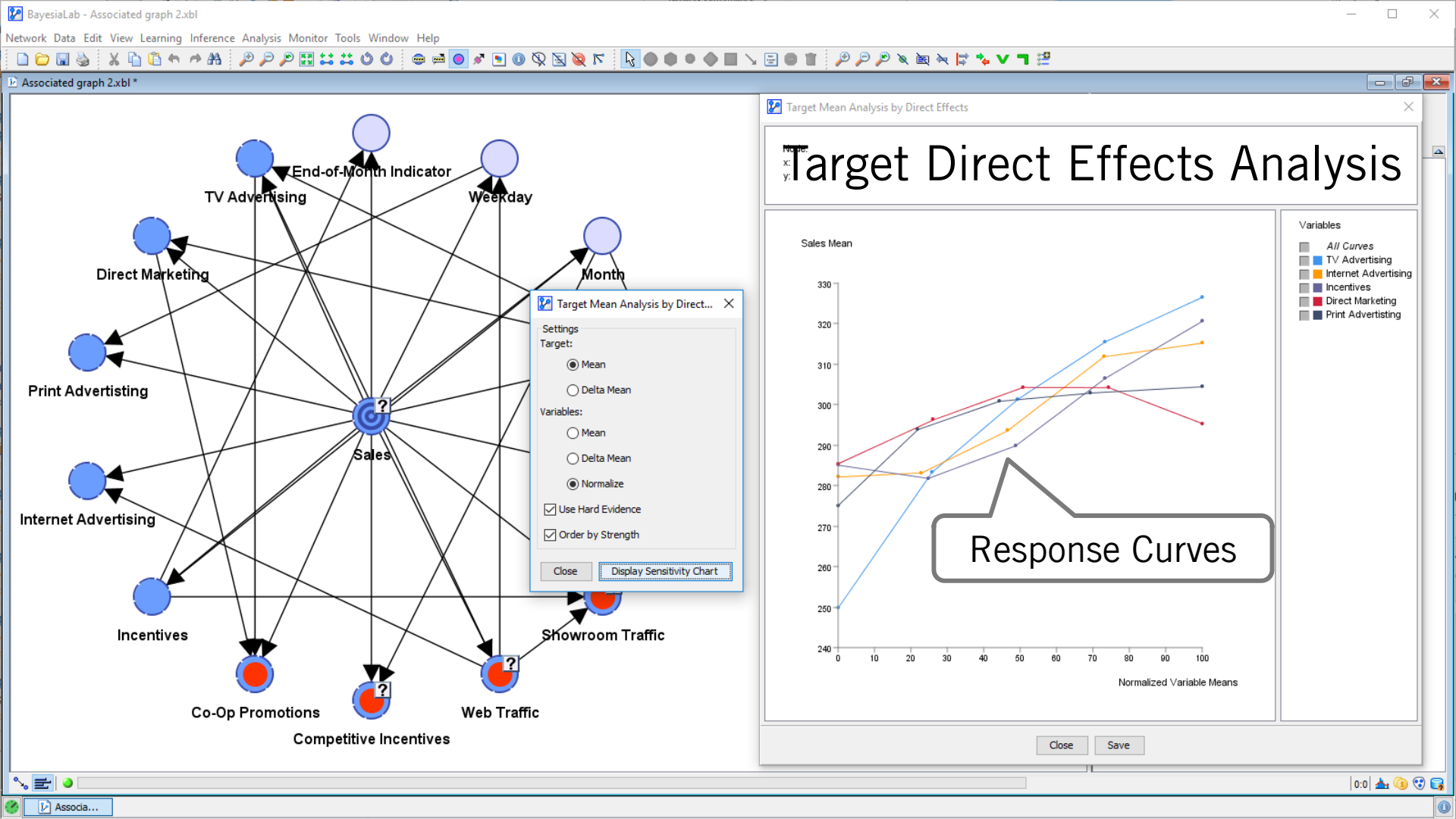


5:2



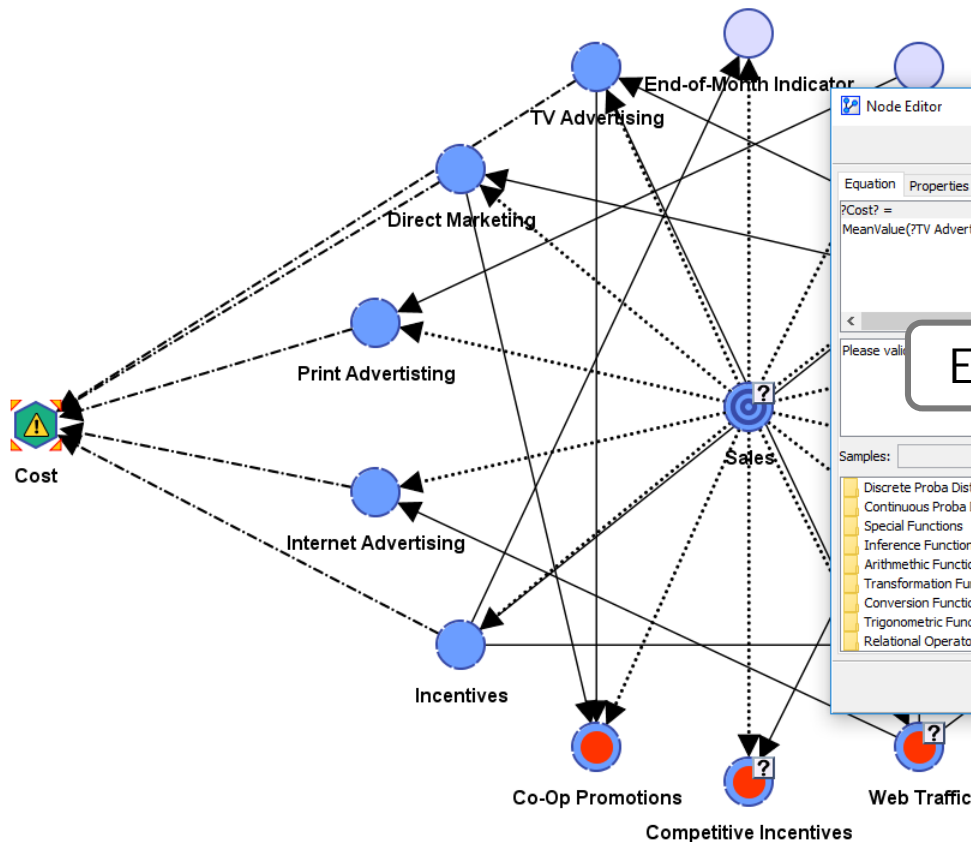








Associated graph 2.xbl *



Defining Media Costs

Node Editor

Node Selection: Cost Rename

Equation Properties Classes Comment

?Cost? =
 MeanValue(?TV Advertising?) + MeanValue(?Direct Marketing?) + MeanValue(?Print Advertising?) + MeanValue(?Internet Advertising?) + MeanValue(?Incentives?)

Please validate

Excel-style formula

Samples: 1 ☒ Fixed Seed: 31 Validate

- Discrete Proba Distributions
- Continuous Proba Distributions
- Special Functions
- Inference Functions
- Arithmetic Functions
- Transformation Functions
- Conversion Functions
- Trigonometric Functions
- Relational Operators

TV Advertising
 Direct Marketing
 Print Advertising
 Internet Advertising
Incentives

Domain: [0.2759110152971571, 104.231996355]

OK Cancel

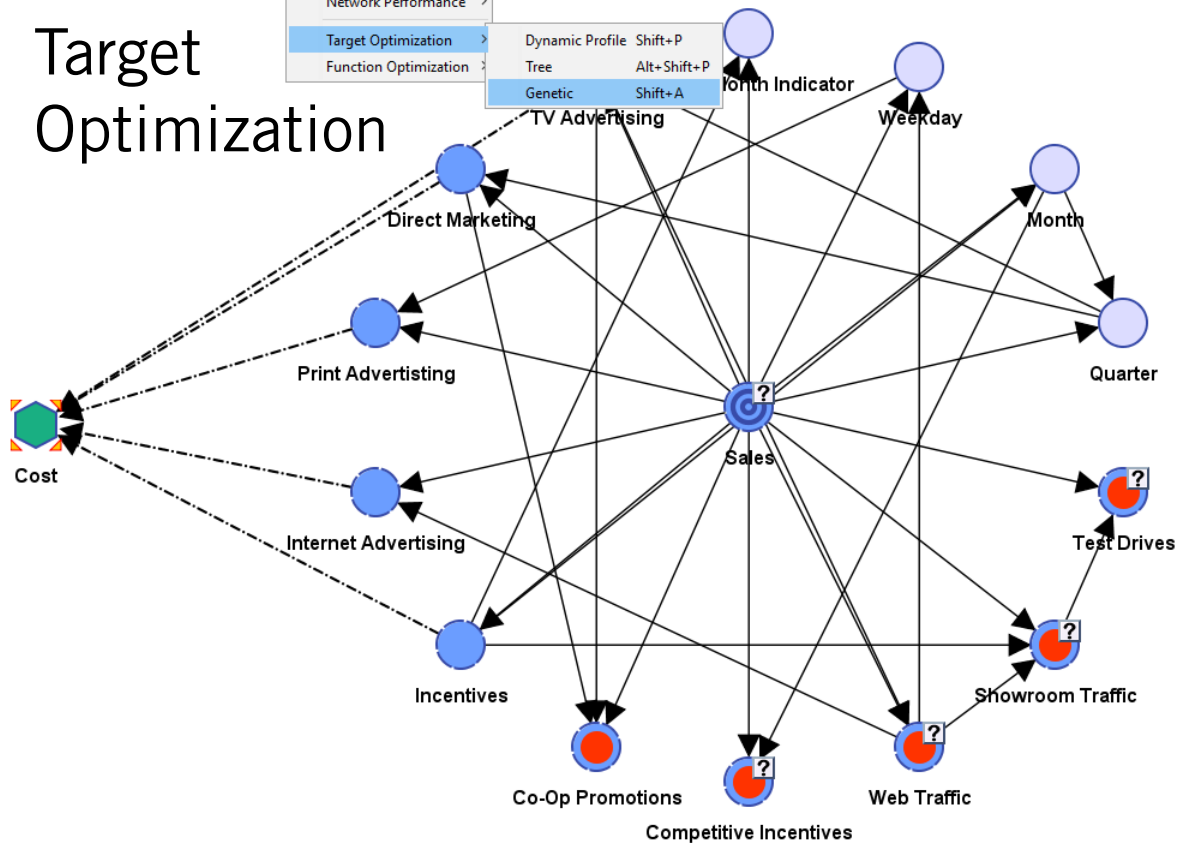


Associated graph 2.xbl

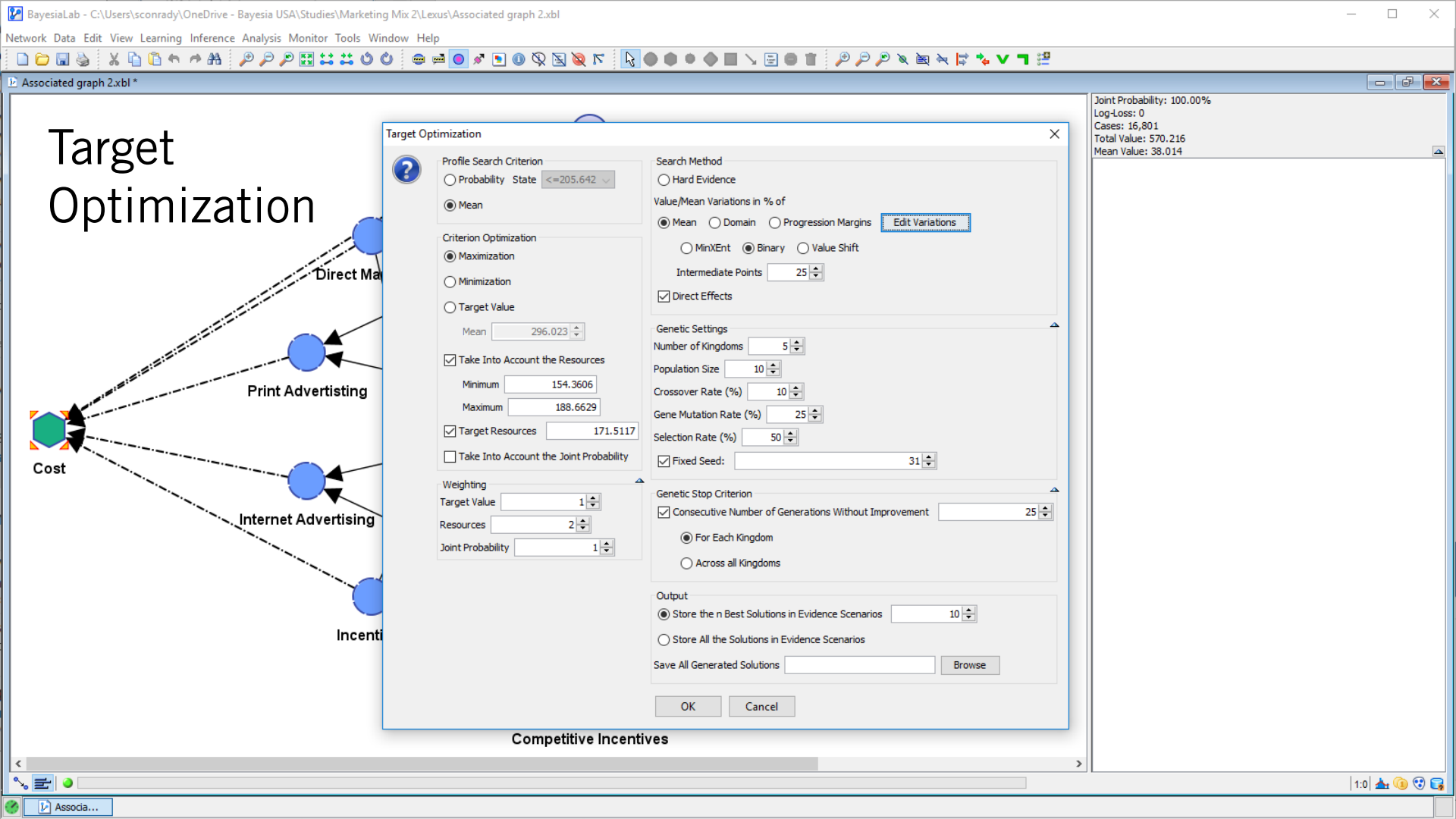
Target Optimization

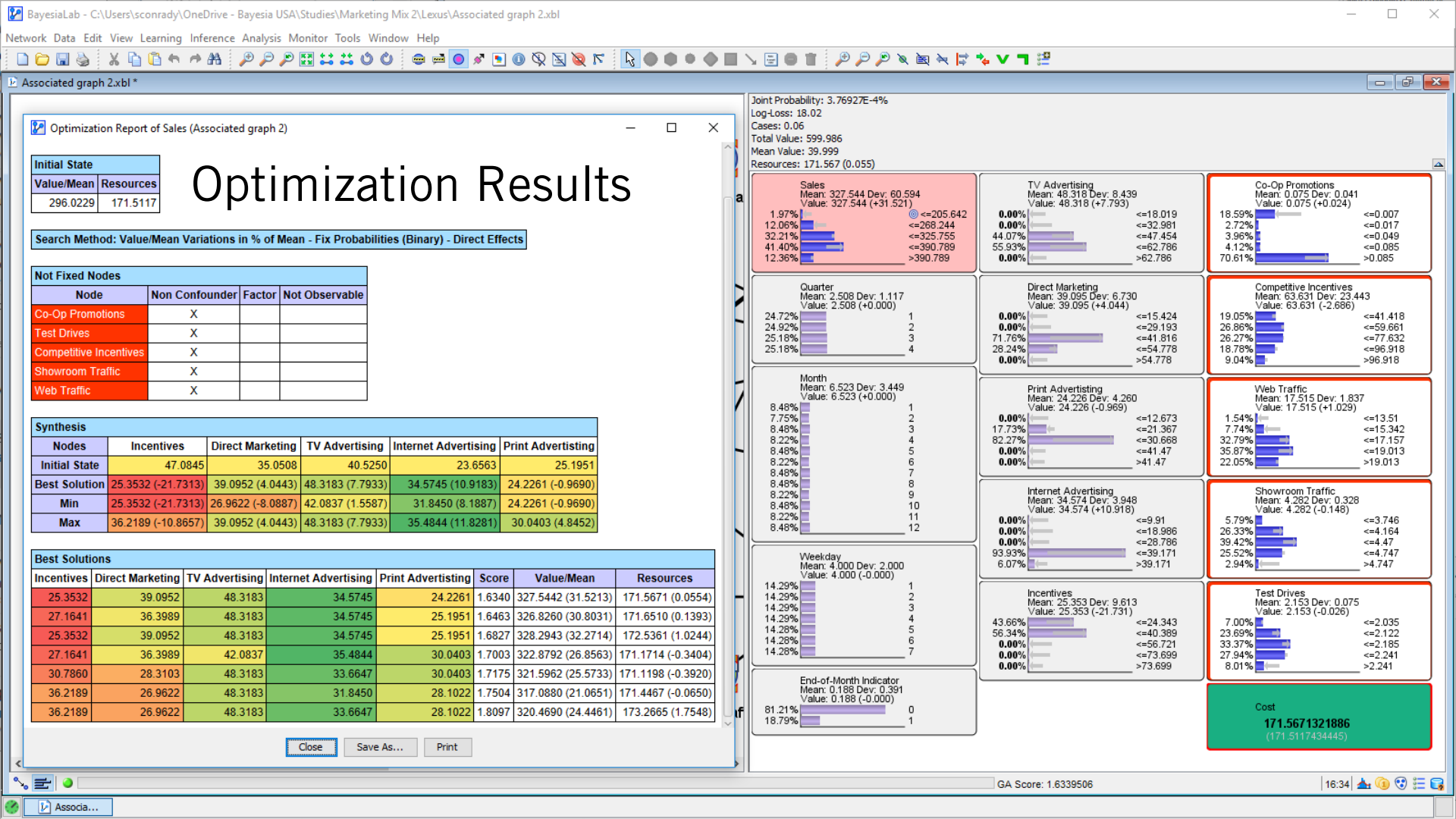
- Visual
- Report
- Network Performance
- Target Optimization
- Function Optimization

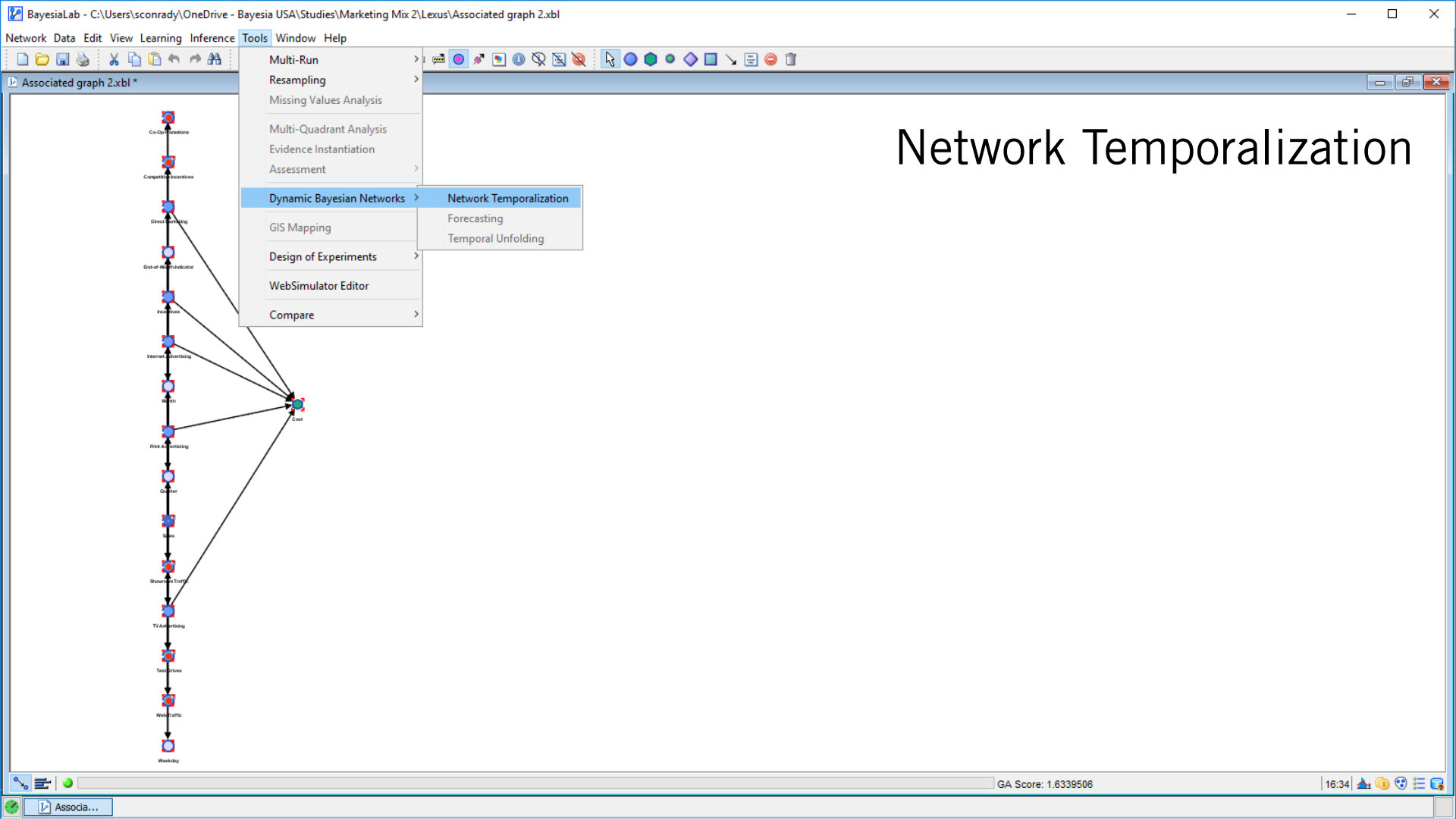
- Dynamic Profile Shift+P
- Tree Alt+Shift+P
- Genetic Shift+A

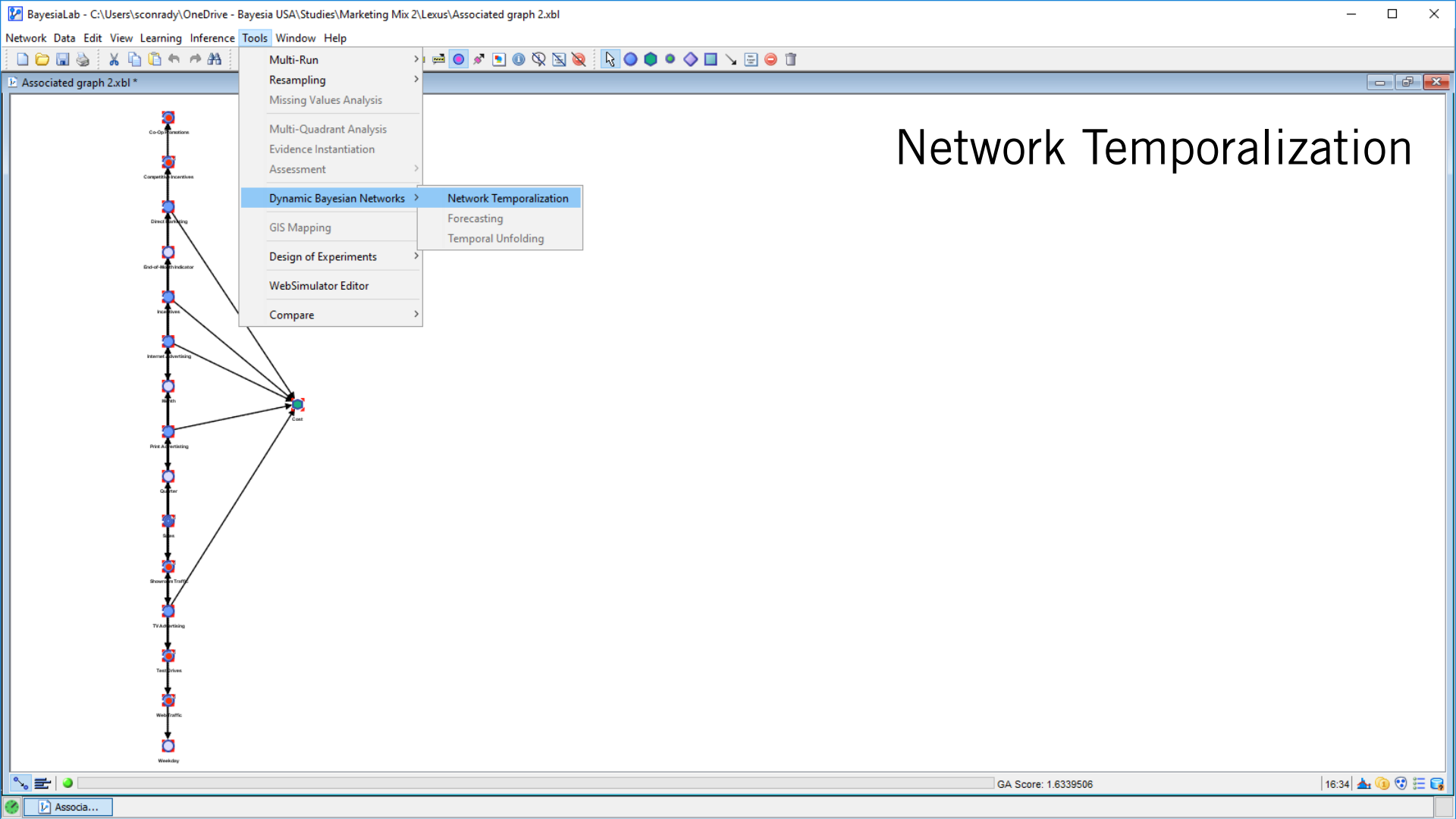


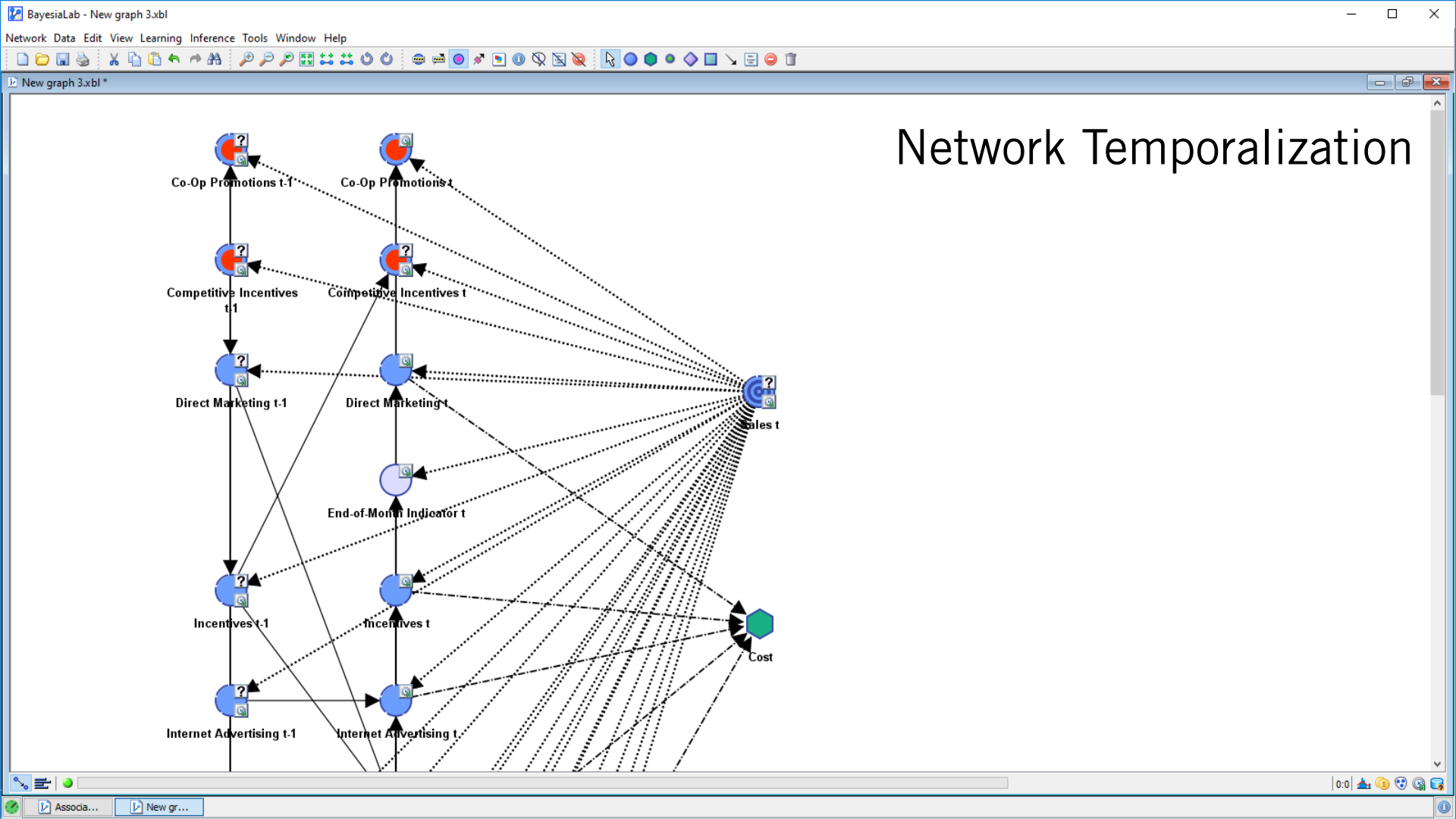
Joint Probability: 100.00%
Log-Loss: 0
Cases: 16,801
Total Value: 570.216
Mean Value: 38.014





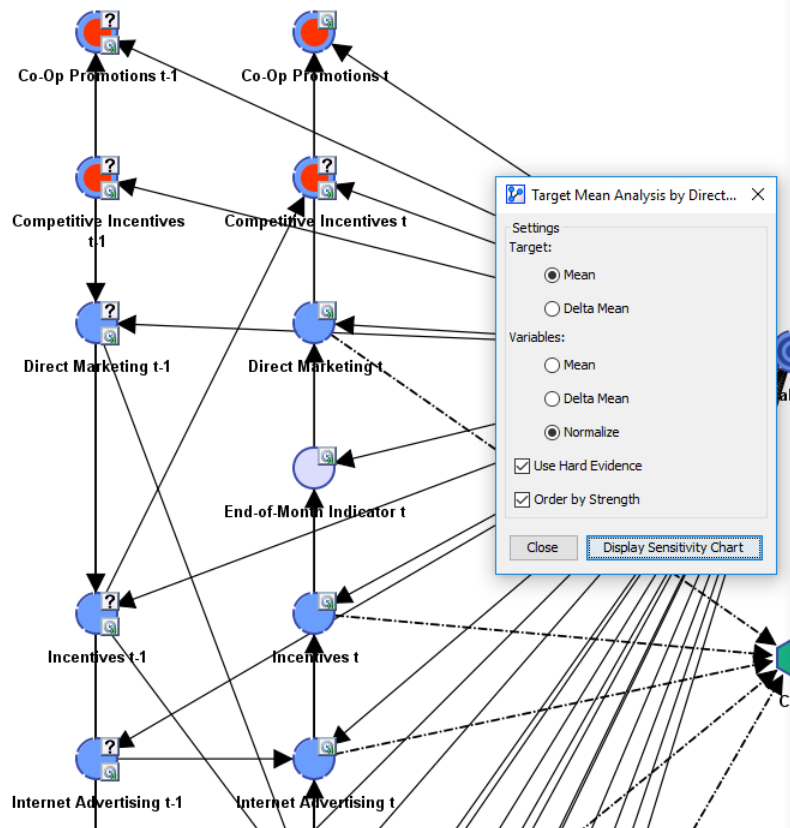








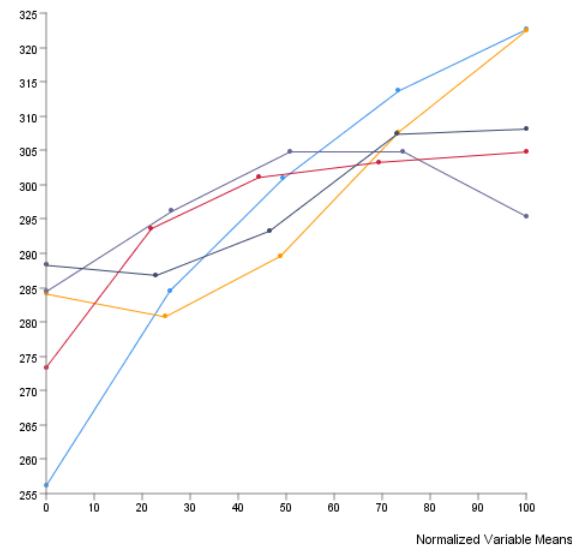
New graph 3.x.bl *



Target Mean Analysis by Direct Effects

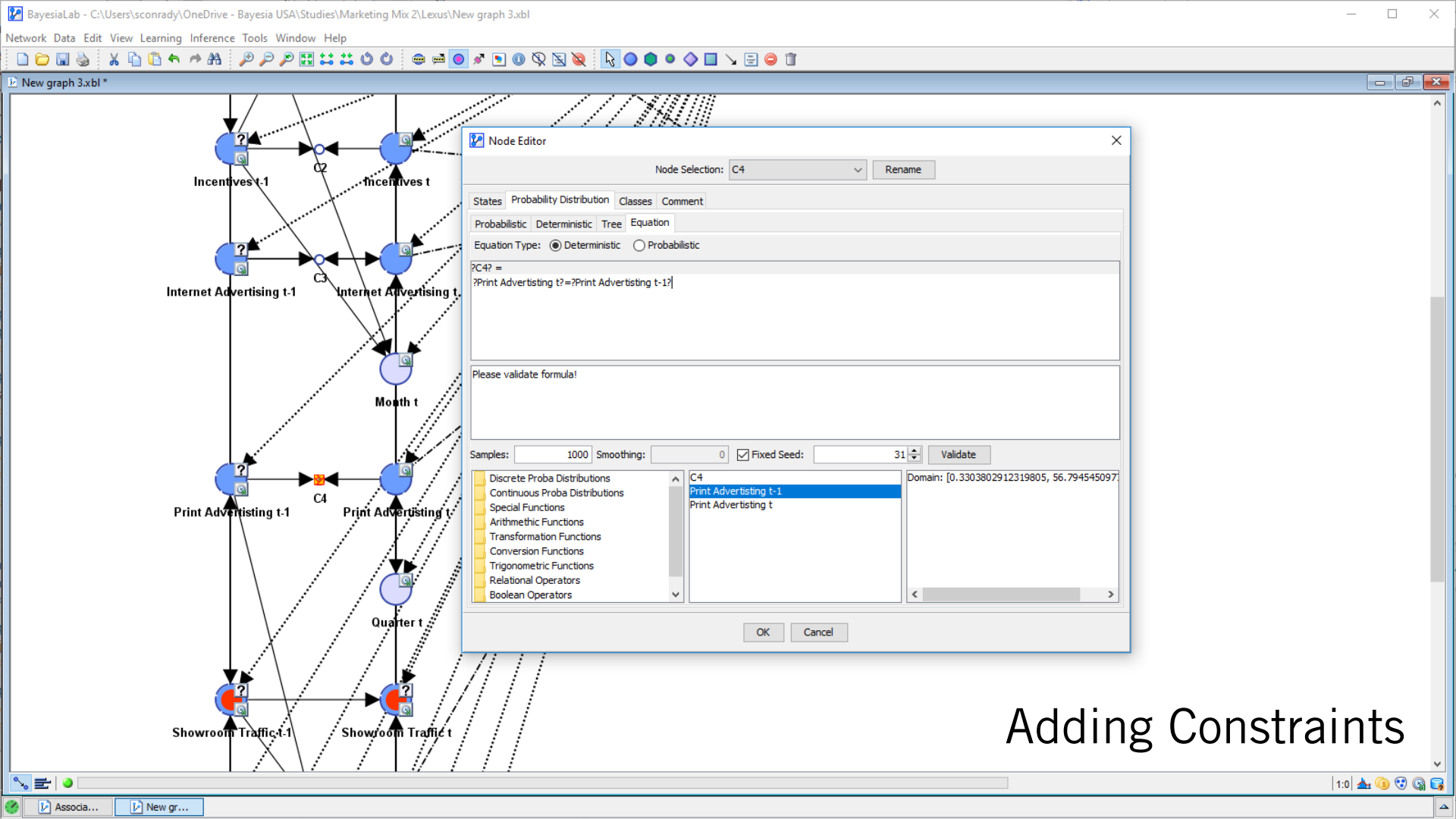
Target Direct Effects Analysis

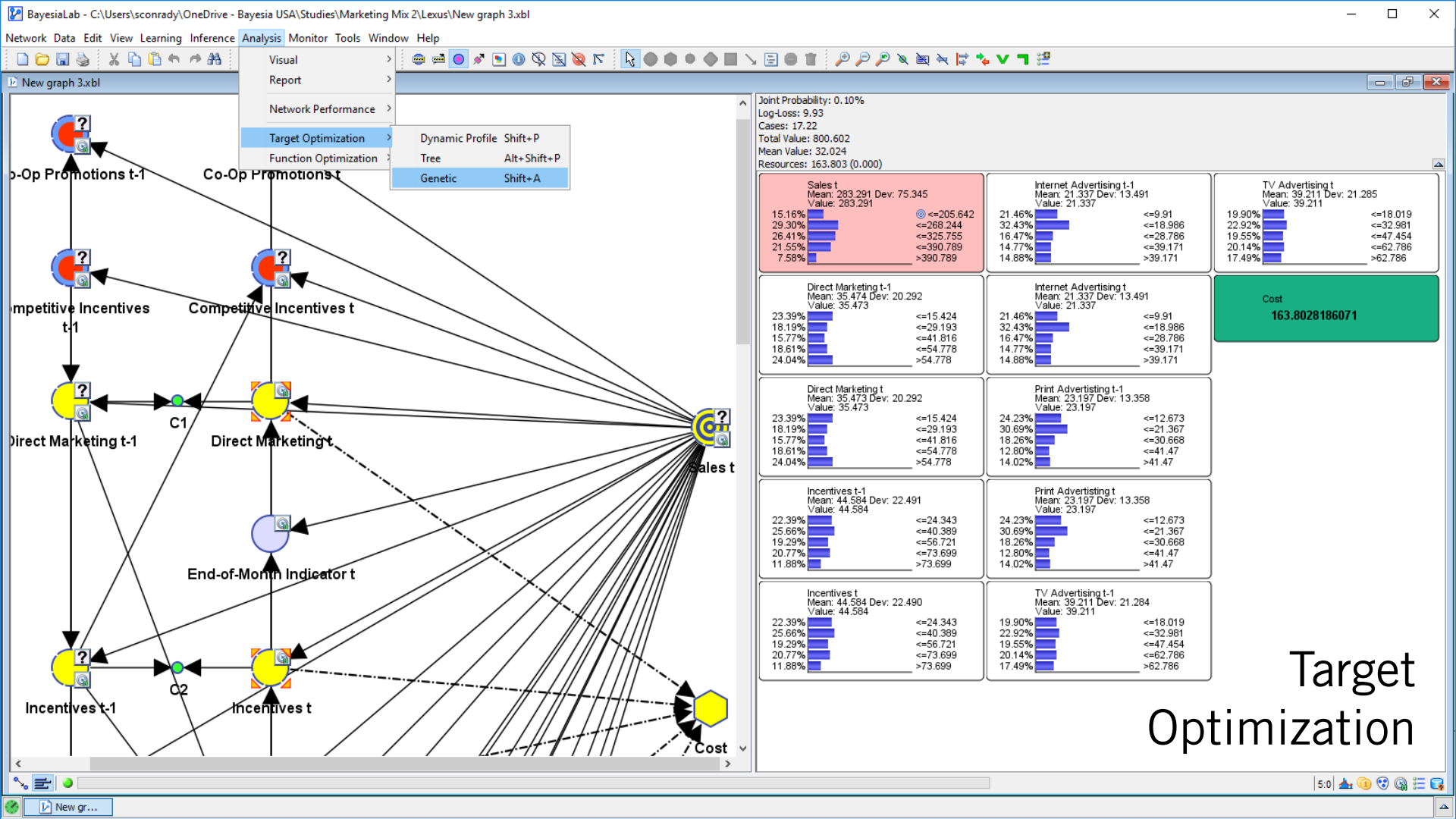
Sales t Mean

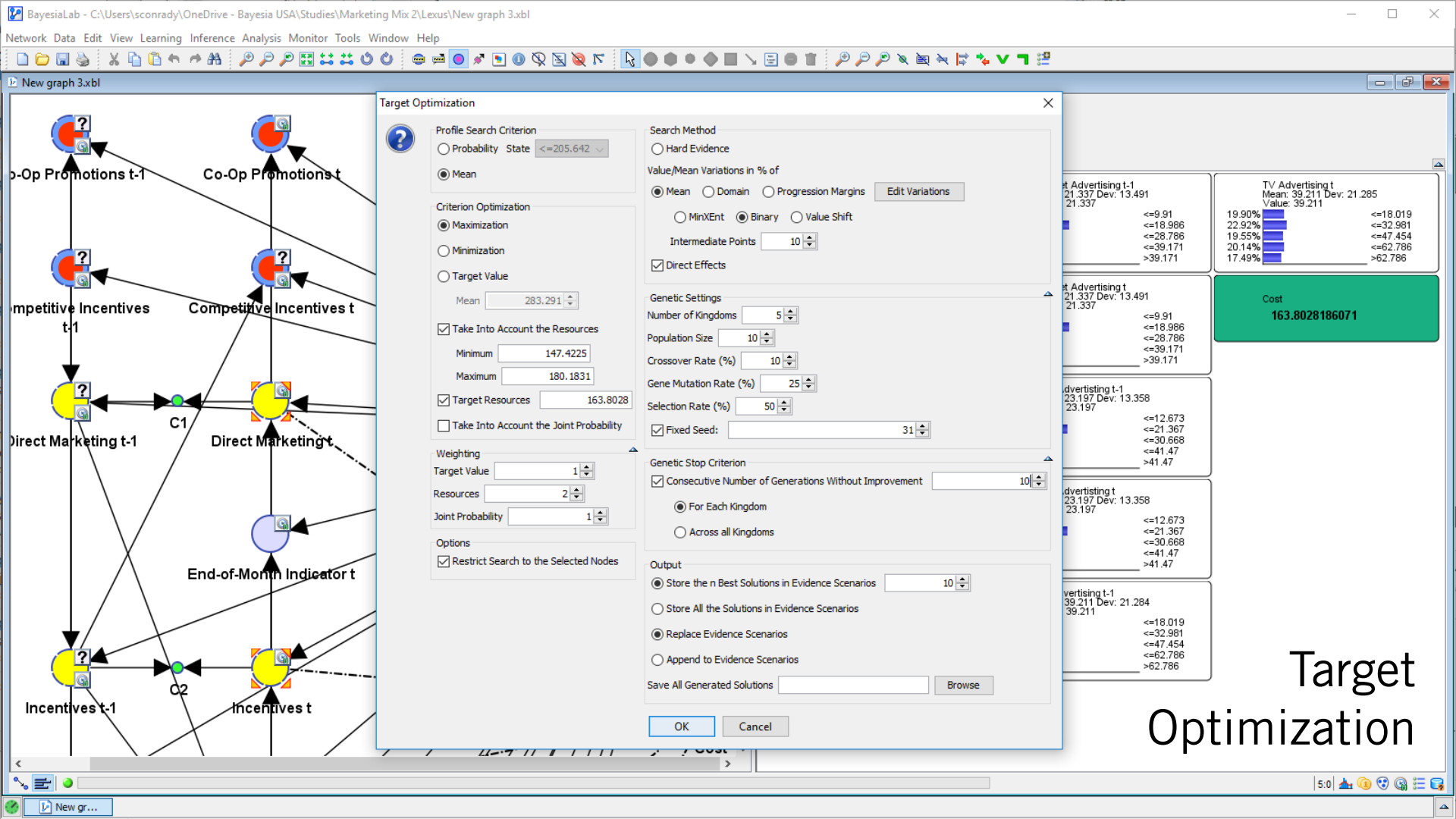


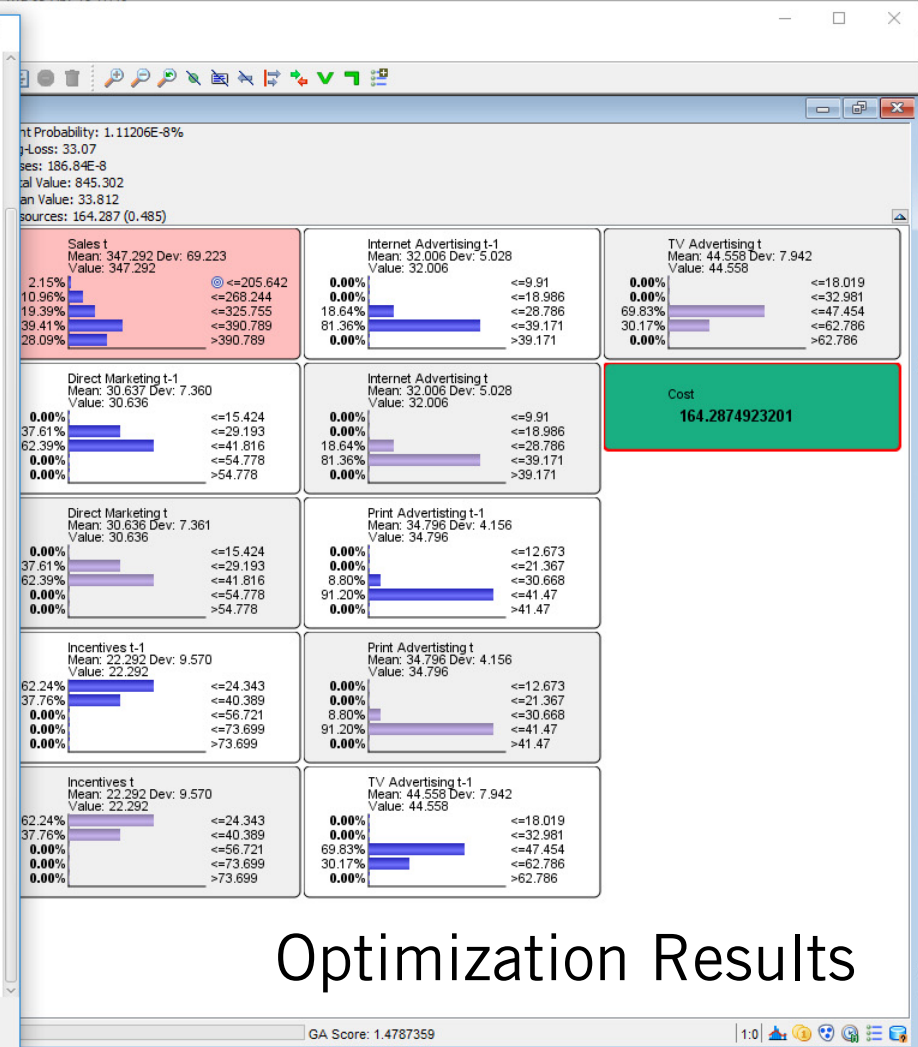
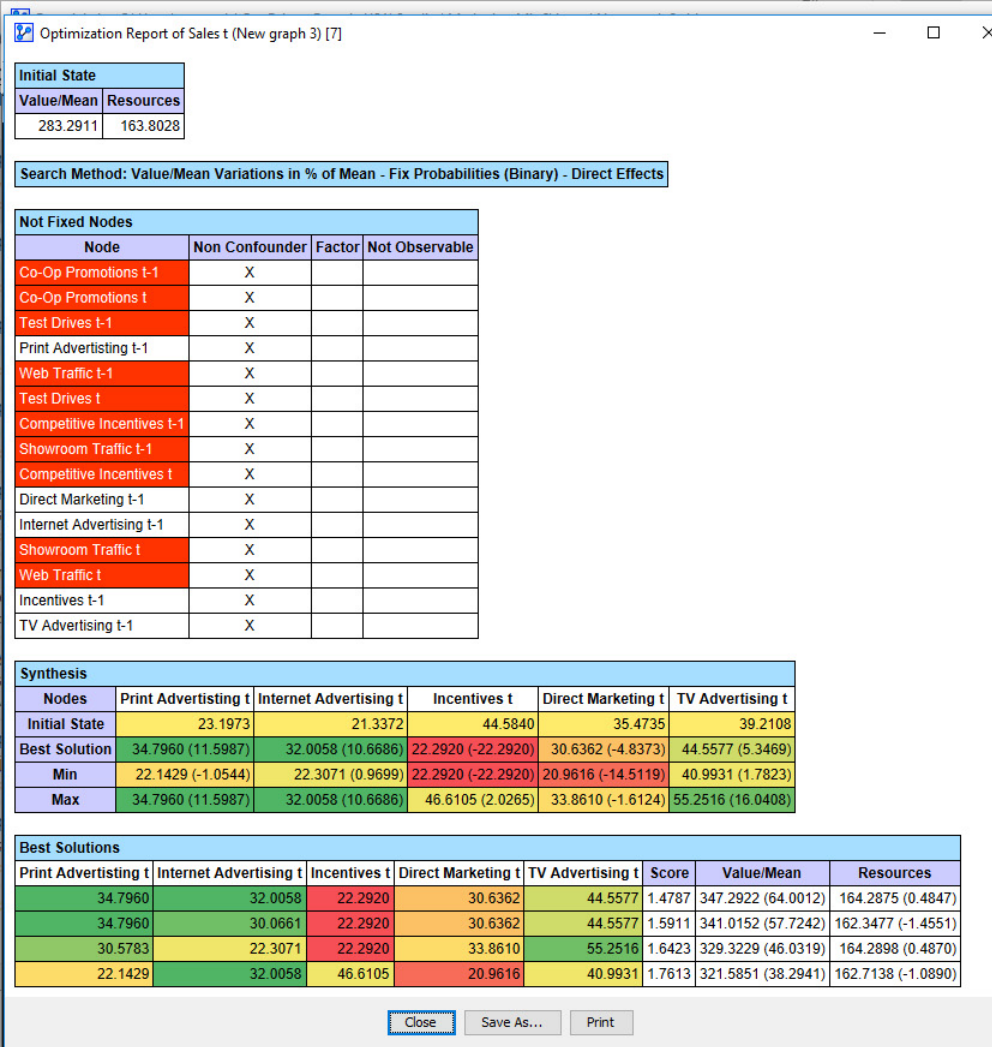
Close

Save











In Conclusion...

Webinar Series: Friday at 1 p.m. (Central)

Upcoming Webinars:

- April 13 Analyzing Capital Flows of Exchange-Traded Funds
- April 20 GIS Mapping with BayesiaLab

Register here: bayesia.com/events

2018 Event Calendar

Webinar Series >

Professional Courses >

6th Annual BayesiaLab Conference in Chicago >

**April 11–13, 2018: Sydney
Introductory BayesiaLab Course**May 16–18, 2018: Seattle
Introductory BayesiaLab CourseMay 21–23, 2018: Seattle
Advanced BayesiaLab CourseJune 5–7, 2018: Paris, France
Introductory BayesiaLab CourseJune 26–28, 2018: Boston
Introductory BayesiaLab CourseJuly 23–25, 2018: San Francisco
Introductory BayesiaLab CourseSeptember 26–28, 2018: New Delhi
Introductory BayesiaLab CourseOctober 29–31, 2018: Chicago
Introductory BayesiaLab CourseNovember 5–7, 2018: Chicago
Advanced BayesiaLab Course

BayesiaLab 7

Artificial Intelligence for Research, Analytics, and Reasoning

User Forum: bayesia.com/community

The screenshot shows the BayesiaLab User Forum interface. At the top is the BayesiaLab logo. Below it is a navigation bar with links: BayesiaLab Software, Bayesian Networks, User Guide & Library, User Forum (which is underlined), BayesiaLab Store, Courses & Events, Learning Resources, News Feed, and About. Below the navigation bar is a dark blue header with a search bar on the left (containing 'This Category' and a search icon) and 'Log In' and 'Register' links on the right. Below the header is a breadcrumb trail: 'BayesiaLab Seminars' with a back arrow. To the right of the breadcrumb is a 'START NEW TOPIC' button. Below the breadcrumb is a forum post. The post has a title 'Webinar on Diagnostic Decision Support with Bayesian Networks' and a description 'a minute ago by stefanconrady: The answers to all webinar questions will be posted here.' To the right of the description are icons for replies (0), likes (0), and views (0). Below the description is a line 'Started by stefanconrady a minute ago'. At the bottom of the forum post is a language selector showing 'English' with a dropdown arrow.


BAYESIALAB

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← BayesiaLab Seminars **START NEW TOPIC**

Latest New Top

 **Webinar on Diagnostic Decision Support with Bayesian Networks**
a minute ago by [stefanconrady](#): The answers to all webinar questions will be posted here. 0 0 0

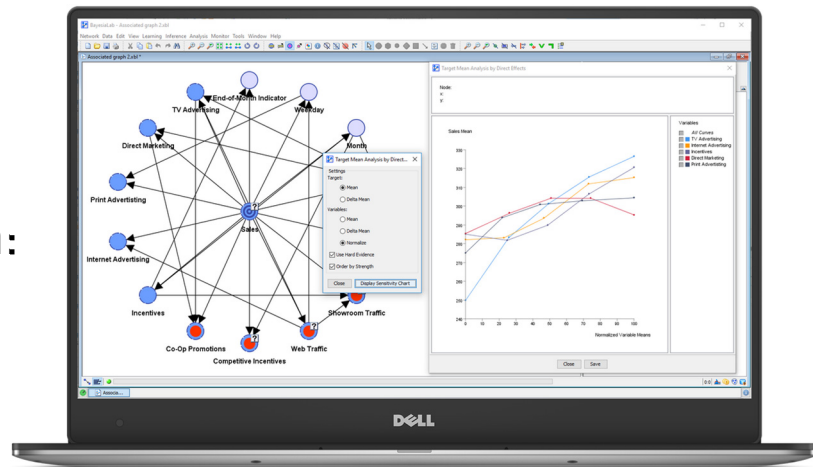
Started by [stefanconrady](#) a minute ago

English

BayesiaLab Trial

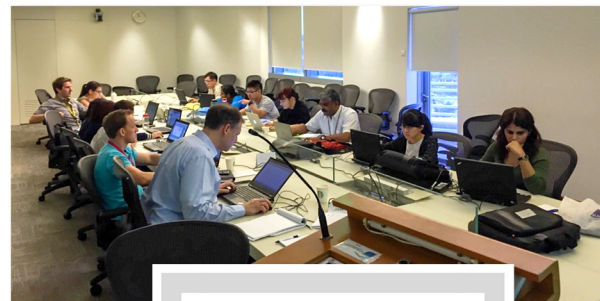
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- July 23–25
San Francisco, CA
- August 29–31
London, UK
- September 26–28
New Delhi, India
- October 29–31
Chicago, IL
- December 4–6
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6th Annual BayesiaLab Conference in Chicago

November 1–2, 2018



Thank You!



stefan.conrady@bayesia.us



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