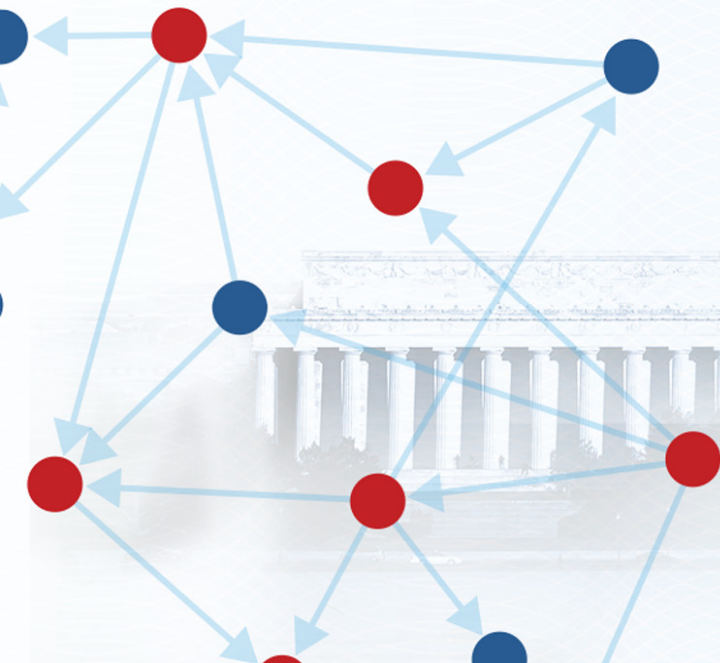




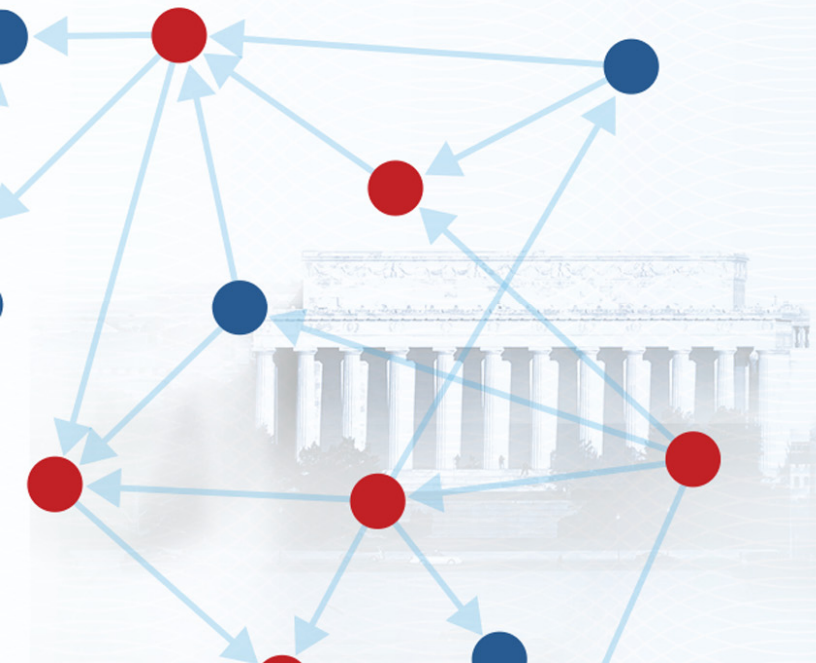
# Intelligence Analysis with Artificial Intelligence and Bayesian Networks





Hello  
my name is

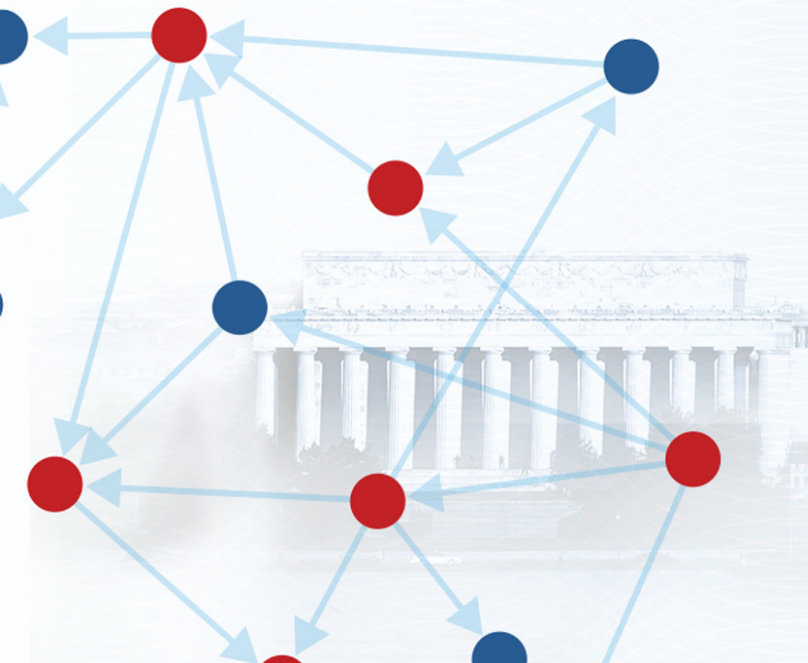
David  
Aebischer





Hello  
my name is

Stefan Conrady



# Part I: Introduction 60 min.

- Introduction: Our Company and Technology
- Motivations:
  - The Promise, the Peril, and the Limitations of Artificial Intelligence
  - Human Cognitive Limitations & Biases in Reasoning
- Objective:
  - Human-Machine Teaming
  - Practical Artificial Intelligence for Here & Now
- Dimensions of Reasoning
- Introducing Bayesian Networks as a Reasoning Framework





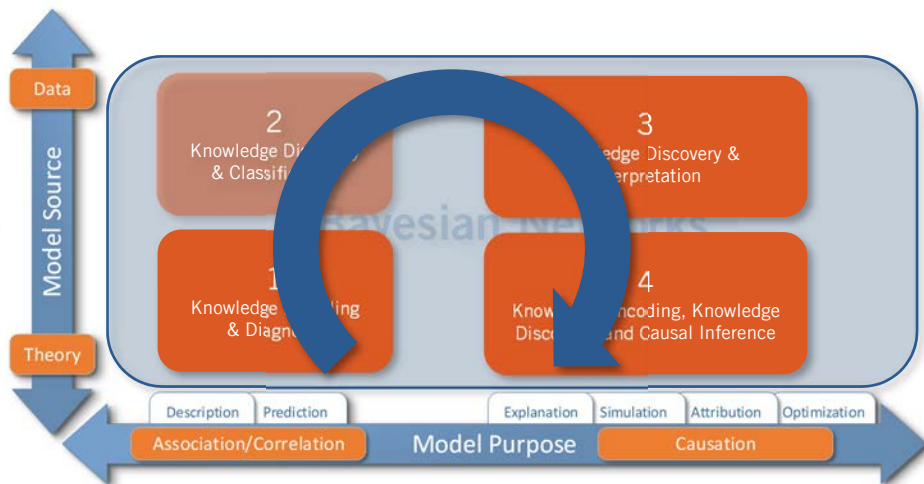
# Part II: Examples



120 min.

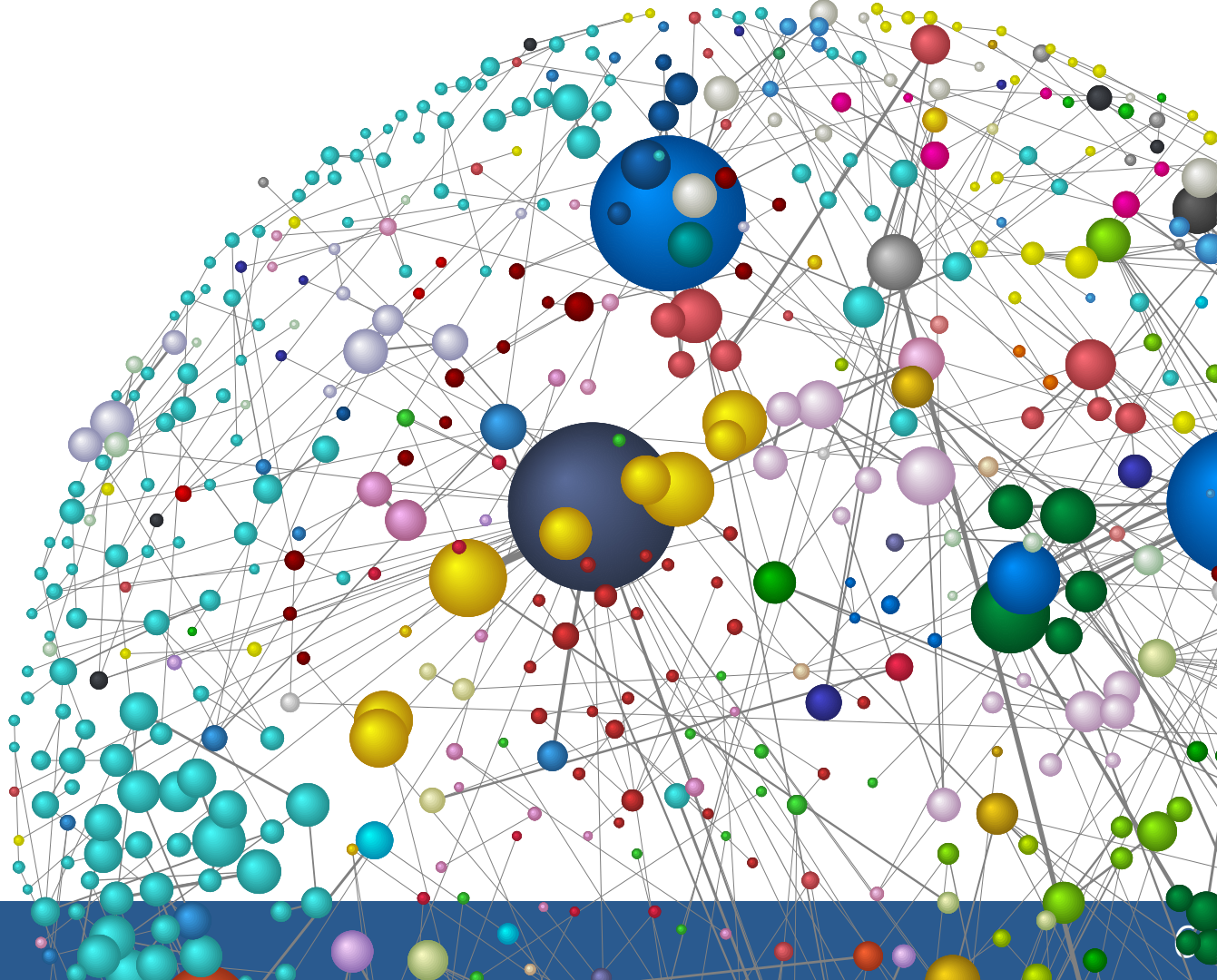
## Examples

- Knowledge Encoding & Reasoning
  - Friend or Foe?
  - Where is my Bag?
  - Monty Hall or Choose Your Battles Wisely!
  - Formal Knowledge Elicitation
- Knowledge Discovery
  - Interpretation
  - Anomaly Detection
- Causal Inference
  - Simpson's Paradox





Co-founded in 2001  
by Dr. Lionel Jouffe &  
Dr. Paul Munteanu



# Disambiguation



Our Company



Our Product

## The Paradigm

### BAYESIAN NETWORKS\*

**Judea Pearl**

Cognitive Systems Laboratory

Computer Science Department

University of California, Los Angeles, CA 90024

*judea@cs.ucla.edu*

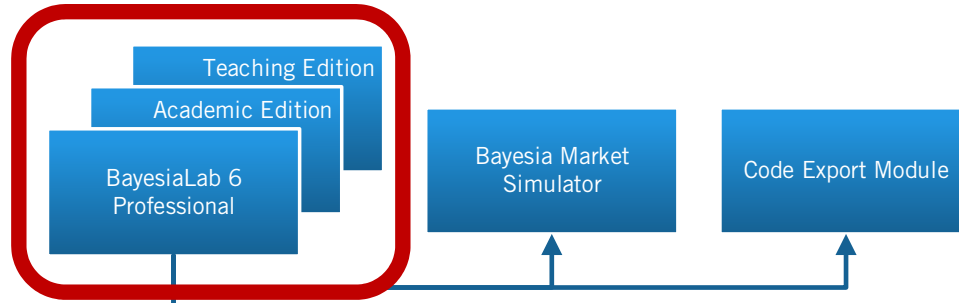
Bayesian networks were developed in the late 1970's to model distributed processing in reading comprehension, where both semantical expectations and perceptual evidence must be combined to form a coherent interpretation. The ability to coordinate bi-directional inferences filled a void in expert systems technology of the early 1980's, and Bayesian networks have emerged as a general representation scheme for uncertain knowledge [Pearl, 1988, Heckerman *et al.*, 1995, Jensen, 1996, Castillo *et al.*, 1997].

Bayesian networks are directed acyclic graphs (DAGs) in which the nodes represent vari-

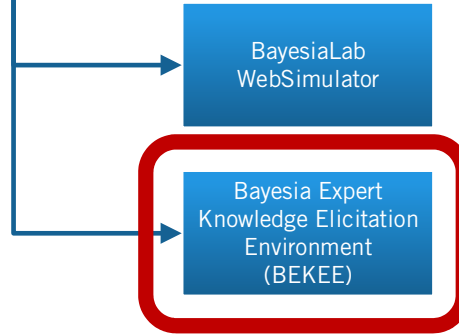




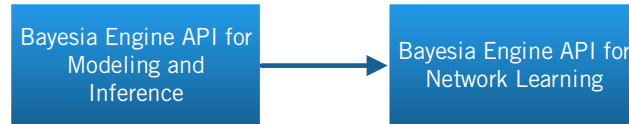
## Desktop Software



## Web Application



## API

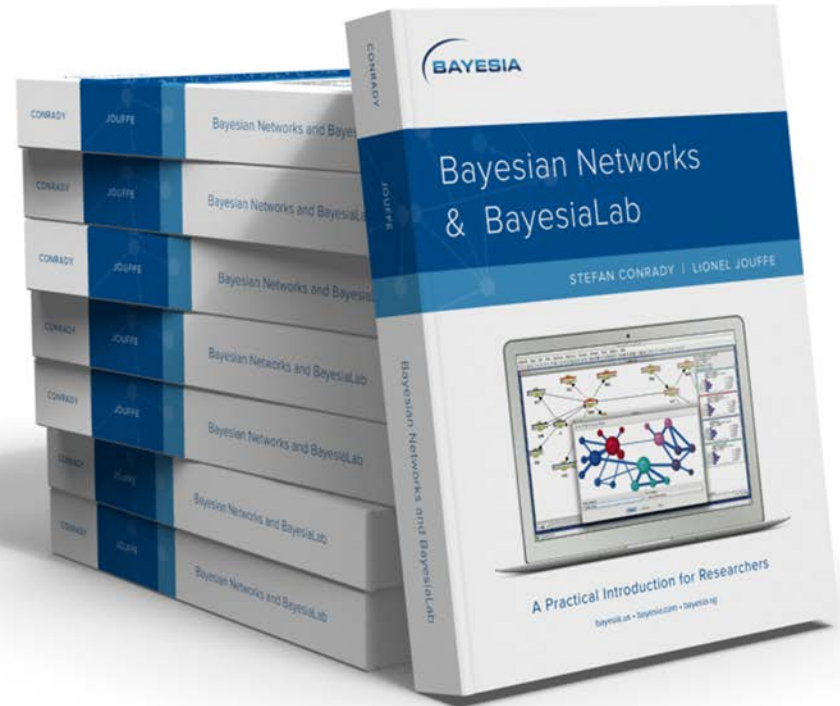




# Bayesian Networks & BayesiaLab

## A Practical Introduction for Researchers

- Free download:  
[www.bayesia.com/book](http://www.bayesia.com/book)
- Hardcopy available on Amazon:  
<http://amzn.com/0996533303>



# Seminar Credits

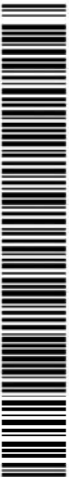






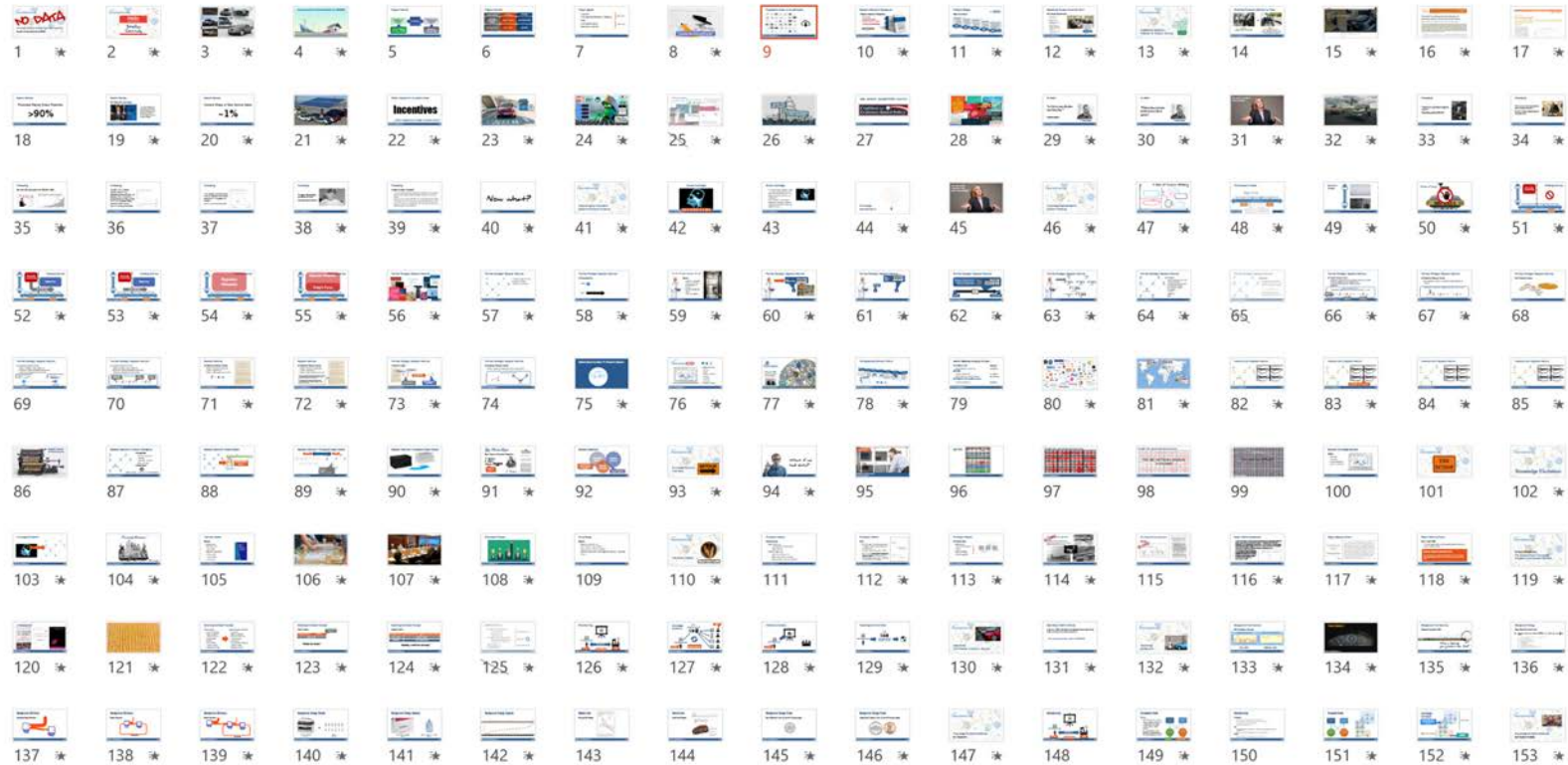
# Seminar Credits

Please check in!



|  |  |   |   |
|--|--|---|---|
| <br>718167964896578277001 | Event  |   | <br><br>Payment Status<br>Free Order |
|  | Free Seminar in Boston: Knowledge Discovery with Bayesian Networks and Virtual Reality |   |   |
|  | Date+Time  | Location  |   |
|  | Friday, January 19, 2018 from 1:00 PM to 4:00 PM (EST)                                 | CIC Boston—Lighthouse West<br>50 Milk Street<br>20th Floor<br>Boston, MA 02109      |   |
|  | Order Info<br>Order # 11111111. Ordered by Maria Singh on January 17, 2018 1:00 PM     |   |   |
| Type<br>Seminar: Knowledge Discovery with Bayesian Networks and Virtual Reality                            |  |  |   |

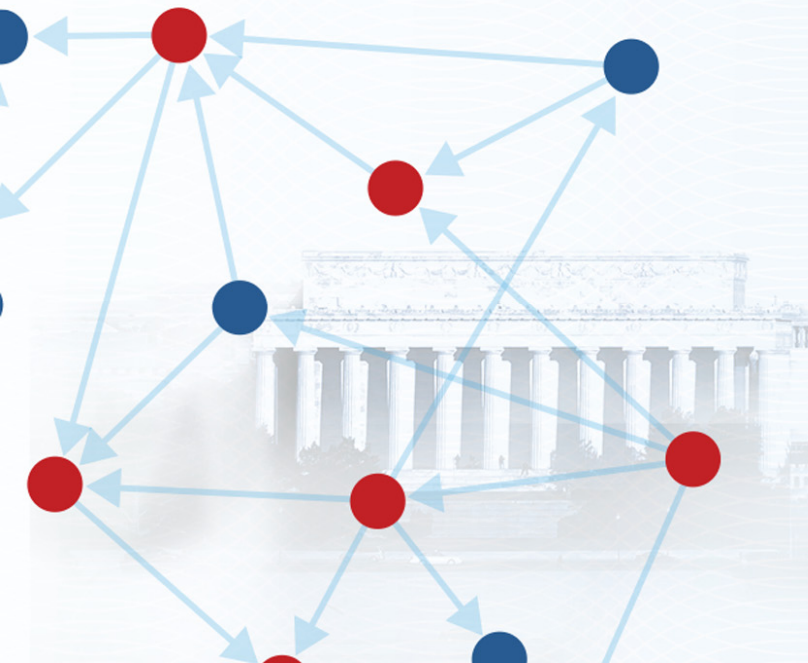
# Presentation slides will be available





# Motivation

## The Promise, the Peril, and the Limits of Artificial Intelligence



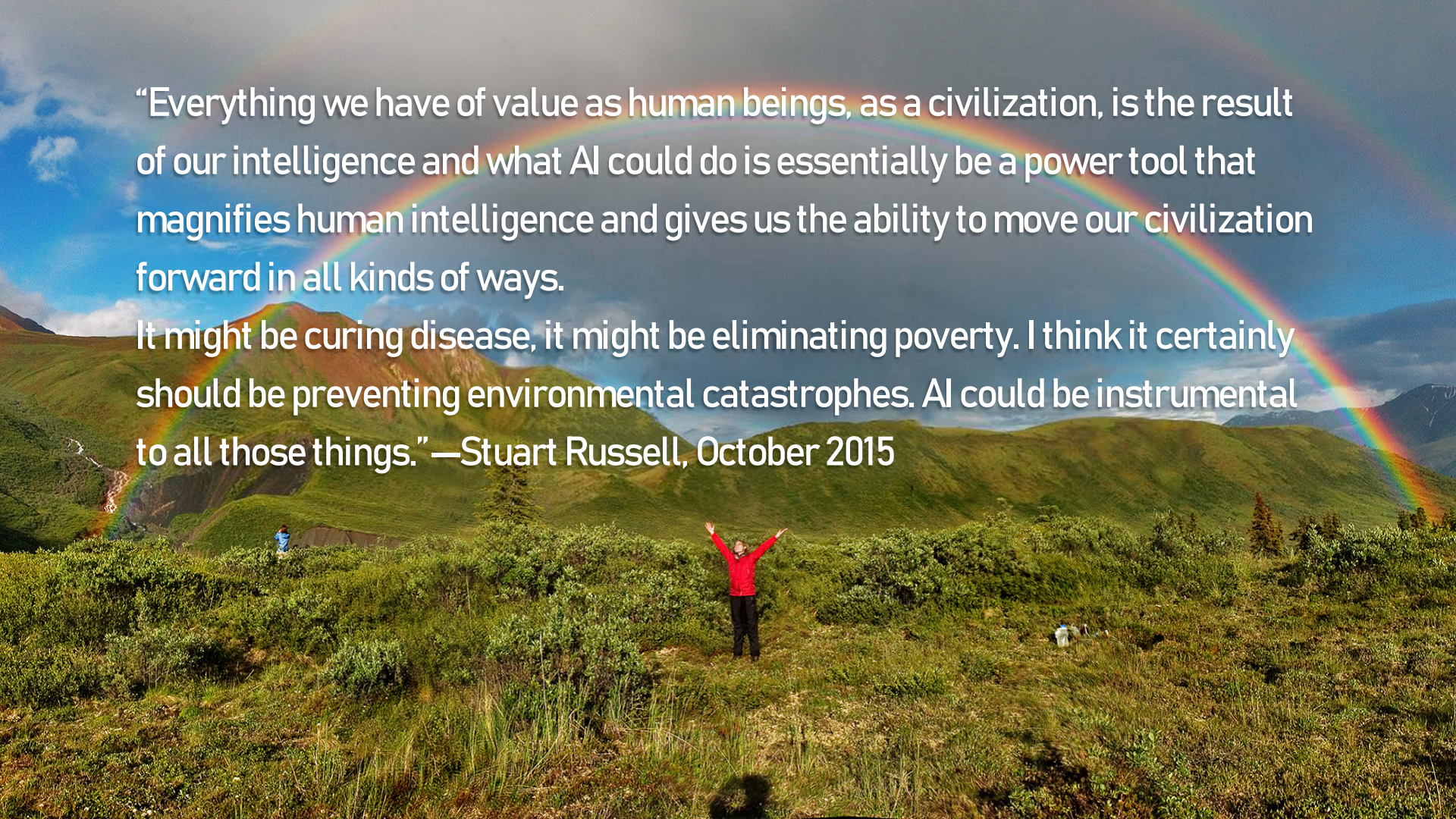


I WANT TO SAY TWO WORDS TO YOU:



ARTIFICIAL INTELLIGENCE



A vibrant landscape featuring rolling green hills under a blue sky with scattered clouds. A bright, multi-colored rainbow arches across the sky, starting from the left and ending on the right. In the foreground, a person wearing a red jacket and dark pants stands with their arms raised in a celebratory gesture. The terrain is covered in lush green grass and shrubs. In the distance, more hills and a small waterfall are visible.

“Everything we have of value as human beings, as a civilization, is the result of our intelligence and what AI could do is essentially be a power tool that magnifies human intelligence and gives us the ability to move our civilization forward in all kinds of ways.

It might be curing disease, it might be eliminating poverty. I think it certainly should be preventing environmental catastrophes. AI could be instrumental to all those things.” —Stuart Russell, October 2015





**ARTIFICIAL INTELLIGENCE**



THE DEVELOPMENT OF FULL ARTIFICIAL INTELLIGENCE  
COULD SPELL THE END OF THE HUMAN RACE.  
STEPHEN HAWKING, DECEMBER 2014



# Artificial Intelligence — A Threat?



**Elon Musk**   
@elonmusk



If you're not concerned about AI safety, you should be. Vastly more risk than North Korea.

8:29 PM - Aug 11, 2017

 2,429  13,681  37,782





## News | Science

[Home](#) > [News](#) > [Science](#)

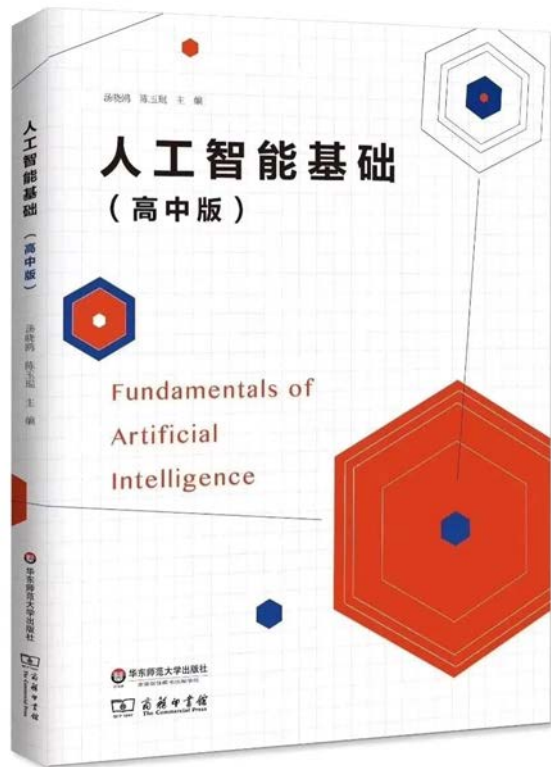
# Artificial Intelligence is greater concern than climate change or terrorism, says new head of British Science Association



## MORE STORIES

- 1** Anything could now happen on Brexit as Barnier bluff goes wrong
- 2** Almost \$40bn wiped off cryptocurrency market as Bitcoin rout intensifies
- 3** My daughter was seen by the NHS 47 times but no one realised her condition was fatal
- 4** Sixty Conservative MPs to launch plan to take down Theresa May's Chequers deal this weekend
- 5** Royal Navy warship 'confronted by Chinese military' in South China Sea

# Artificial Intelligence an Adversarial Threat?



# 中国人工智能

# The Washington Post



The Pentagon. (Photo/Charles Dharapak/AP file photo)

By **Drew Harwell**

September 7 at 10:39 AM

## The Switch

# Defense Department pledges billions toward artificial intelligence research

The military's research arm said Friday it will invest up to \$2 billion over the next five years toward new programs advancing artificial intelligence, stepping up both a technological arms race with China and an ideological clash with Silicon Valley over the future of powerful machines.



Big Data  
Is the New Oil

Forbes

FUTURE OF  
A-DRIVEN  
OVATION

ARTIFICIAL  
INTELLIGENCE

MACHINE  
LEARNING

Harvard  
Business  
Review

GETTING  
CONTROL OF  
BIG DATA

Data  
Models

AI

Big

We need to find it,  
Extract it, Refine it, Distill  
use it to drive Economic

AI:  
The Killer App for  
Your Business

How connected artificial  
intelligence will reshape  
21st century businesses.

NO HYPE  
ZONE

INSIDE: A 14-PAGE SPECIAL REPORT ON FINANCIAL TECHNOLOGY

The  
Economist

How to fix America's inner cities  
The self-service economy  
Time to open up Indonesia  
Inside the anti-bribery business  
Why humans cause heatwaves

Artificial Intelligence

The promise and the peril

ARTIFICIAL INTELLIGENCE  
AND THE END  
OF THE HUMAN ERA

OUR FINAL  
INVENTION

JAMES BARRAT

DATA-  
DRIVEN  
BUSINESS

USE REAL-LIFE NUMBERS TO  
IMPROVE YOUR BUSINESS BY 352%

Stage-1  
Machine  
Consciousness

Stage-2  
Machine  
Intelligence

Stage-3  
Machine  
Learning

Stages of Artificial Intelligence

NEXT 200 SLIDES

Gartner Analytic Ascendancy



Artificial  
for A Better Future

BIG  
DATA

www.oddesttechnologies.com

BayesiaLab.com





DAVID WEINBERGER [BACKCHANNEL](#) 04.18.17 08:22 PM

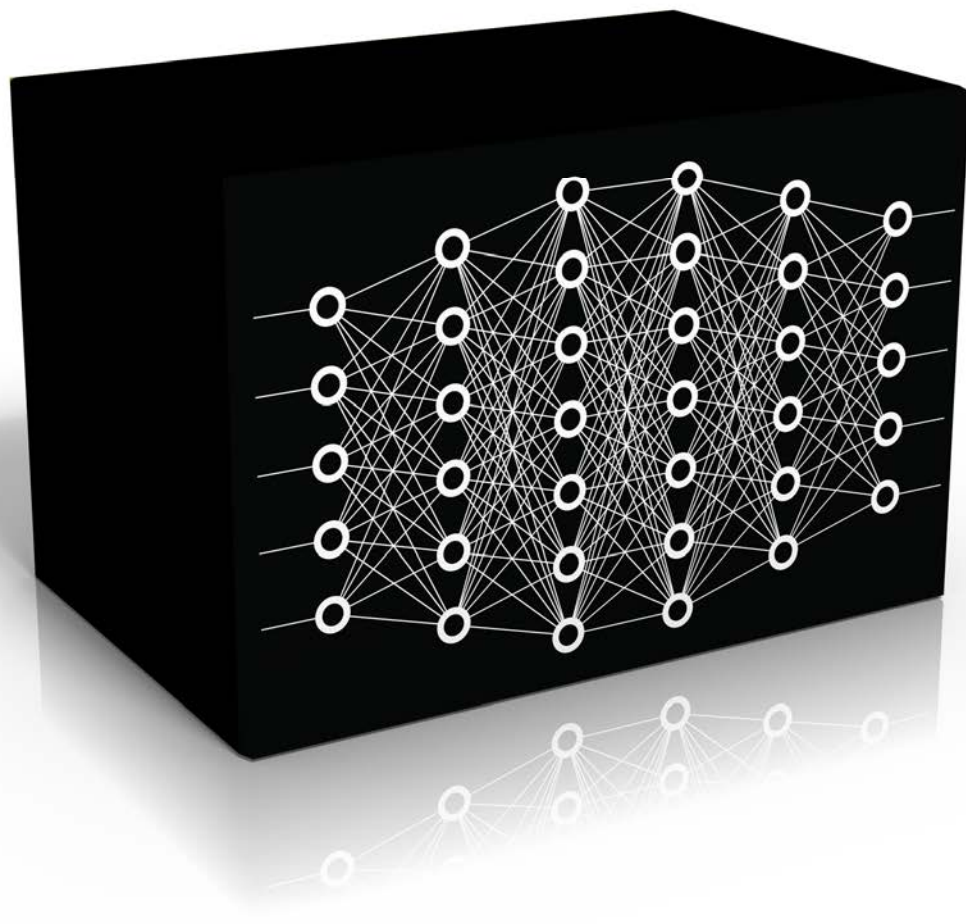
# OUR MACHINES NOW HAVE KNOWLEDGE WE'LL NEVER UNDERSTAND



**WIRED**

# ALIEN KNOWLEDGE

WHEN MACHINES JUSTIFY KNOWLEDGE



# Motivation

Small Brain







**COGNITIVE  
LIMIT**

**3**

**DIMENSIONS**

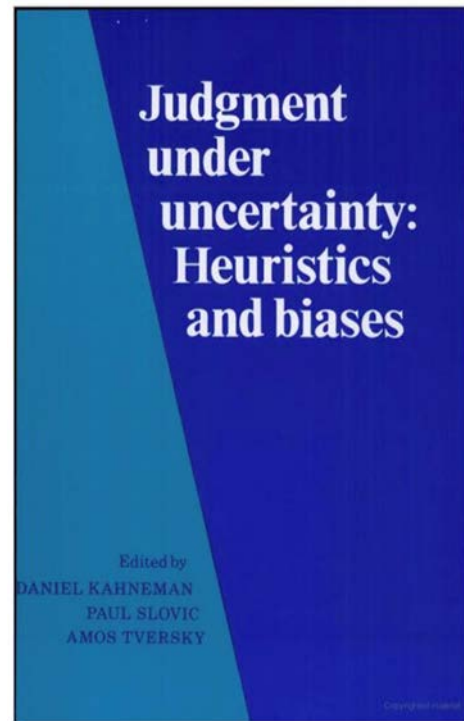
**HUMANS ONLY**

# Motivation

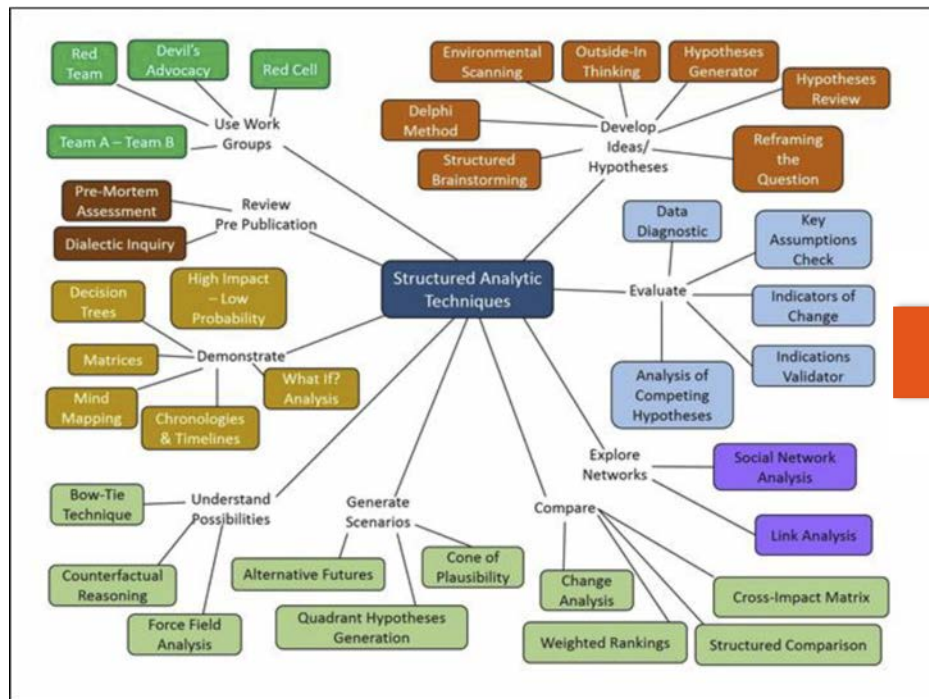
## Fundamental Challenges in Human Reasoning

- Cognitive Biases
- Comprehending High-Dimensional Domains
- Dealing with Uncertainty
- Combining Data and Theory
- Distinguishing Observation and Causation

Human reasoning is flawed!



# Motivation

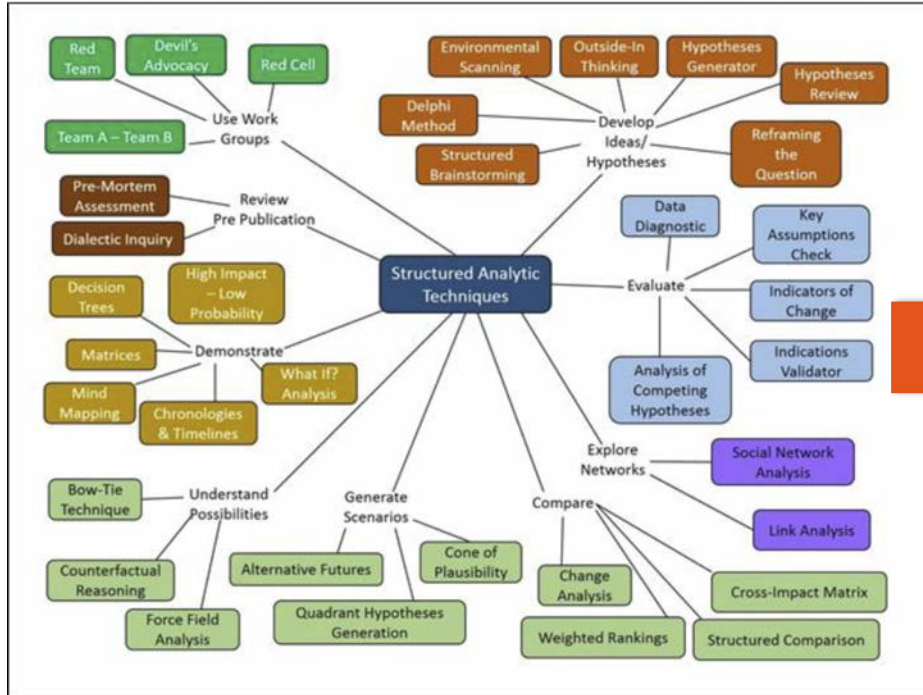


Inference must still happen  
in the human brain

*Structured Analytics Techniques*

*Source: AFH14-133 27 SEPTEMBER 2017 31*

# Motivation



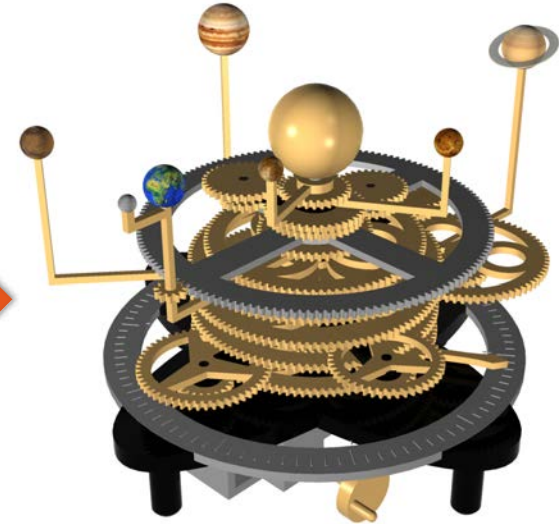
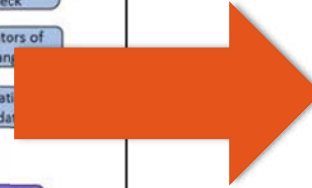
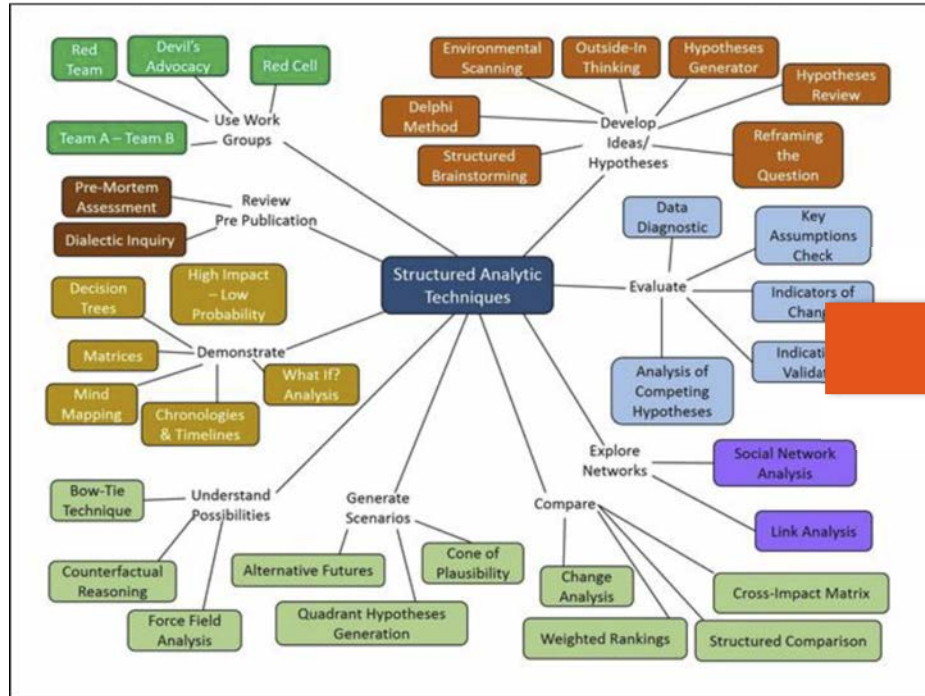
Decision Maker

*Structured Analytics Techniques*

*Source: AFH14-133 27 SEPTEMBER 2017 31*

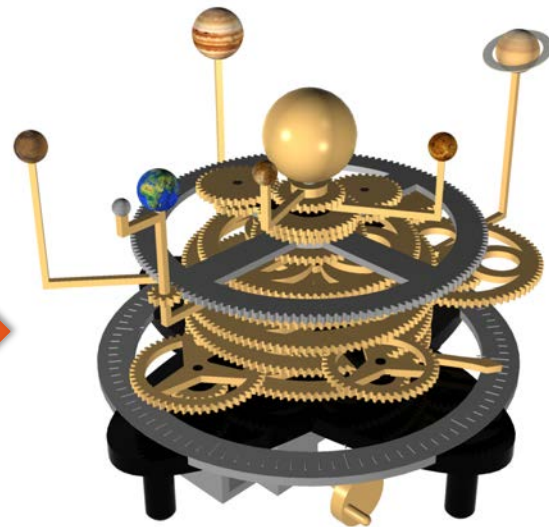


# Objective: Explicit Inference & Reasoning



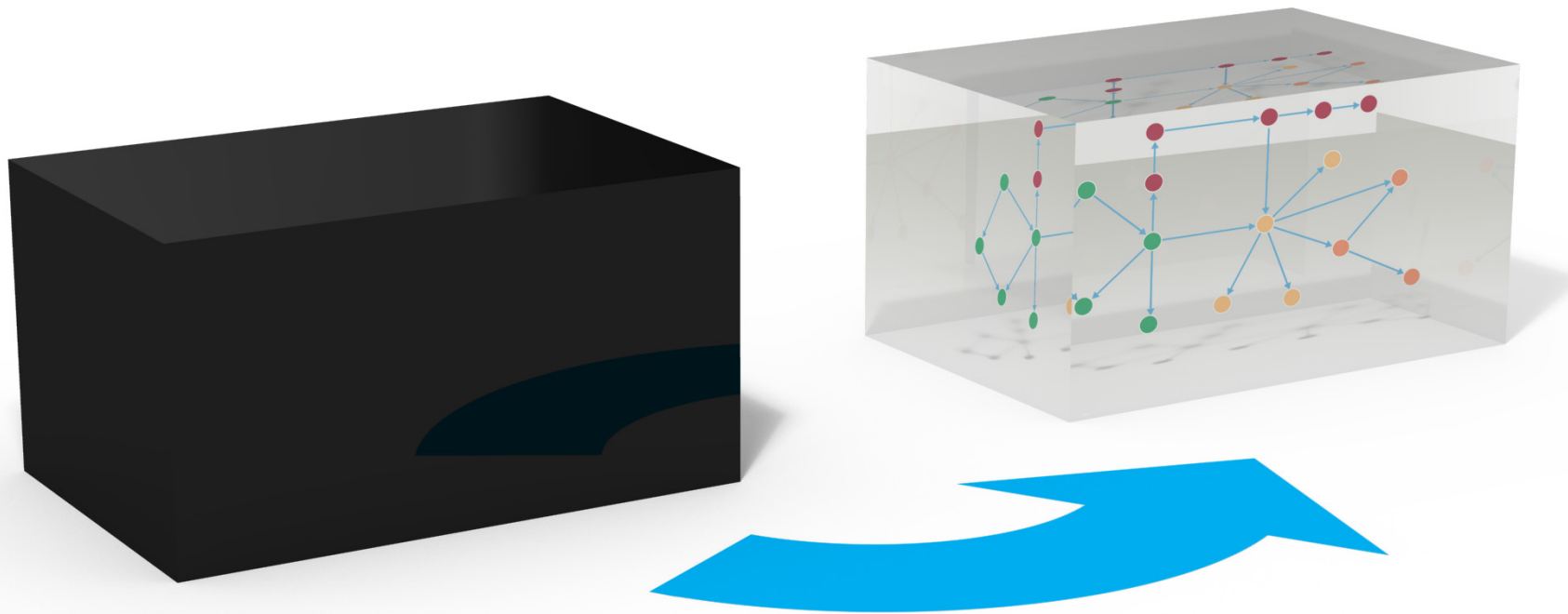
A modeling framework that can help you understand, think, and reason explicitly.

# Objective: Explicit Inference & Reasoning



A modeling framework that can help you understand, think, and reason explicitly.

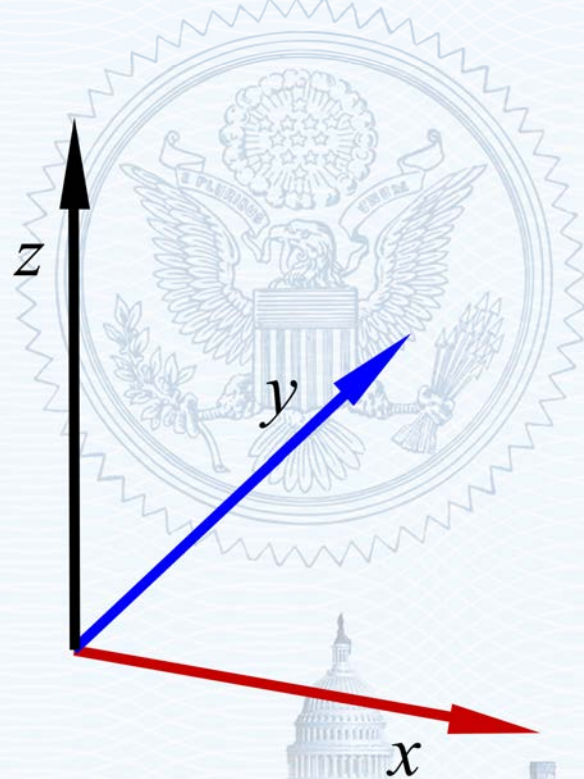
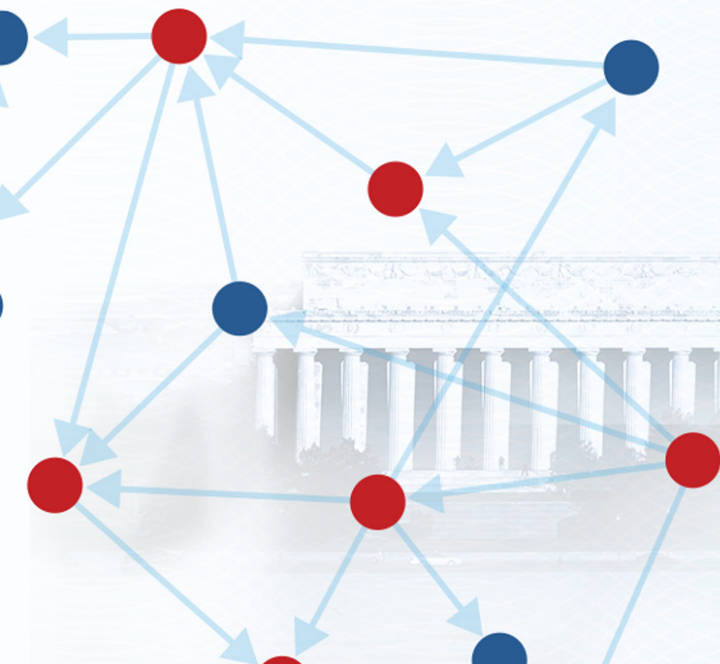
# Objective: Explicit Inference & Reasoning





# Objective: Human-Machine Teaming for Reasoning



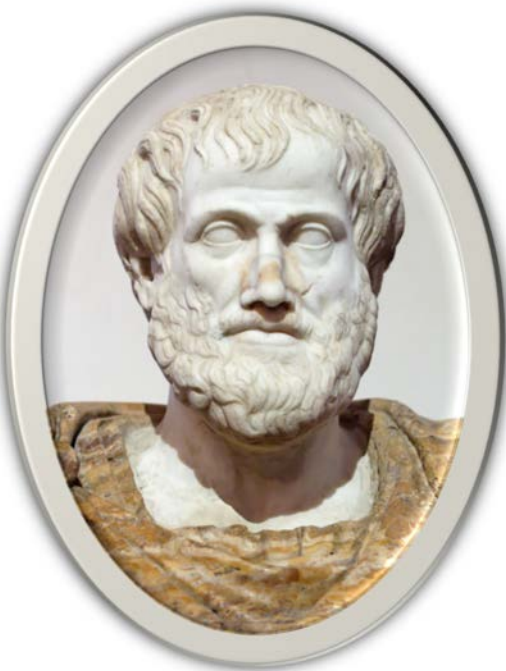


Dimensions of Reasoning



# Deductive Logic

Aristotle (384-322 BC)



ΑΡΙΣΤΟΤΕΛΟΥΣ ΑΝΑΛΥΤΙΚΩΝ ὙΣΤΕ  
ΡΩΝ ΗΤΟΙ ΤΗΣ ΑΠΟΔΕΙΚΤΙΚΗΣ  
ΠΡΩΤΟΝ.



Α Σ Α Διδασκαλία καὶ πᾶς μά  
θησις διαφορετικὴ ἐκ προῦ παρρησίας  
γίνεται γνώσεως. Φανερὸν δὲ τῷ ἰσχυρῶς  
ροῦσιν ἐπὶ πασῶν. Αἵτις γὰρ μαθημα  
τικαὶ τῇ ἐπιστημῇ διὰ τοῦτο τὸ  
ποῦ περαινόνται καὶ τῇ αἰσθύνῃ ἐκαστῇ  
τεχνῇ ὁμοίως δὲ ἐπεὶ τοῦτο λόγος,  
οἷον διὰ συλλογισμῶν καὶ οἷον παρὰ τῆς ἀμφοτέρωθεν προ  
τιρωσ κομῶντων ποιοῦνται τὴν διδασκαλίαν. Οἱ μὲν λαμ  
βάνοντες οὕτως παρὰ ξυμμετρῶν οἱ δὲ διὰ κινῶν τῶν ἀποδόχων διὰ  
τῆς ἀλλοτρίου καὶ ἀποδοχῆς. Ὡς οὖν τῶν οἱ ξυμμετρικοὶ συμπερί  
σῃν καὶ διὰ παρὰ τοῦτο οὕτως ἐπὶ τῇ διένευσί μιν καὶ  
ὁ παρὰ τοῦτο συλλογισμὸς διὰ τῆς ἀποδοχῆς προσηγορεύεται. Ταῦτα μὲν  
ἴσως οἱ πρὸ τῆς λαμβάνου ἀποδοχῆς καὶ τῆς ἀποδοχῆς καὶ τῆς ἀποδοχῆς  
ξυμμετρίας εἶναι. καὶ οἱ μὲν ἀποδοχῆς καὶ τῆς ἀποδοχῆς καὶ τῆς ἀποδοχῆς  
φῶσαι ἀληθείας, οἱ δὲ τῆς ἀποδοχῆς καὶ τῆς ἀποδοχῆς καὶ τῆς ἀποδοχῆς  
ἀμφοτέρωθεν. Τῶν μὲν οὖν οἱ ἀποδοχῆς καὶ τῆς ἀποδοχῆς καὶ τῆς ἀποδοχῆς  
λαμβάνοντες. Ἐστὶ δὲ γνωρίζοντα μὲν πρότερον γνωρίζοντα. τὰ δὲ καὶ  
ἀμφοτέρωθεν. ὡς ἐπὶ τῶν γνωρίζοντων οἷον ὅσα τῶν ἀποδοχῆς καὶ τῆς ἀποδοχῆς  
καθόλου, ὡς ἐπὶ τῶν γνωρίζοντων οἷον ὅσα τῶν ἀποδοχῆς καὶ τῆς ἀποδοχῆς  
οἰσθῆναι, προσηγορεύεται. ὡς ἐπὶ τῶν ἀποδοχῆς καὶ τῆς ἀποδοχῆς καὶ τῆς ἀποδοχῆς  
ἀμφοτέρωθεν. ὡς ἐπὶ τῶν ἀποδοχῆς καὶ τῆς ἀποδοχῆς καὶ τῆς ἀποδοχῆς  
οἰσθῆναι, προσηγορεύεται. ὡς ἐπὶ τῶν ἀποδοχῆς καὶ τῆς ἀποδοχῆς καὶ τῆς ἀποδοχῆς



# Deductive Logic

## Limitations of Logic

“Classical logic has no explicit mechanism for representing the degree of certainty of premises in an argument, nor the degree of certainty in a conclusion, given those premises.”

*J. Williamson, Handbook of the Logic of Argument and Inference.*

*The Turn Toward the Practical*

Logic is not enough!

# Inductive vs. Deductive Logic

Formal Deductive Logic



# 2000 YEARS LATER...

## Bayes' Theorem for Conditional Probabilities

$H$ : Hypothesis

$E$ : Evidence

$$P(H | E) = \frac{P(E | H)P(H)}{P(E)}$$

“Probability of  
H given E”



*T. Bayes.*

## 1763 PHILOSOPHICAL TRANSACTIONS

[ 370 ]

quodque solum, certa nitri signa præbere, sed plura  
concurrere debere, ut de vero nitro producto dubium  
non relinquatur.

LII. *An Essay towards solving a Problem in  
the Doctrine of Chances. By the late Rev.  
Mr. Bayes, F. R. S. communicated by Mr.  
Price, in a Letter to John Canton, A. M.  
F. R. S.*

Dear Sir,

Read Dec. 23, 1763. I Now send you an essay which I have

found among the papers of our deceased friend Mr. Bayes, and which, in my opinion, has great merit, and well deserves to be preserved. Experimental philosophy, you will find, is nearly interested in the subject of it; and on this account there seems to be particular reason for thinking that a communication of it to the Royal Society cannot be improper.

He had, you know, the honour of being a member of that illustrious Society, and was much esteemed by many in it as a very able mathematician. In an introduction which he has writ to this Essay, he says, that his design at first in thinking on the subject of it was, to find out a method by which we might judge concerning the probability that an event has to happen, in given circumstances, upon supposition that we know nothing concerning it but that, under the same circum-



# Probabilistic Reasoning

## Mathematical Formulation of Probabilistic Reasoning

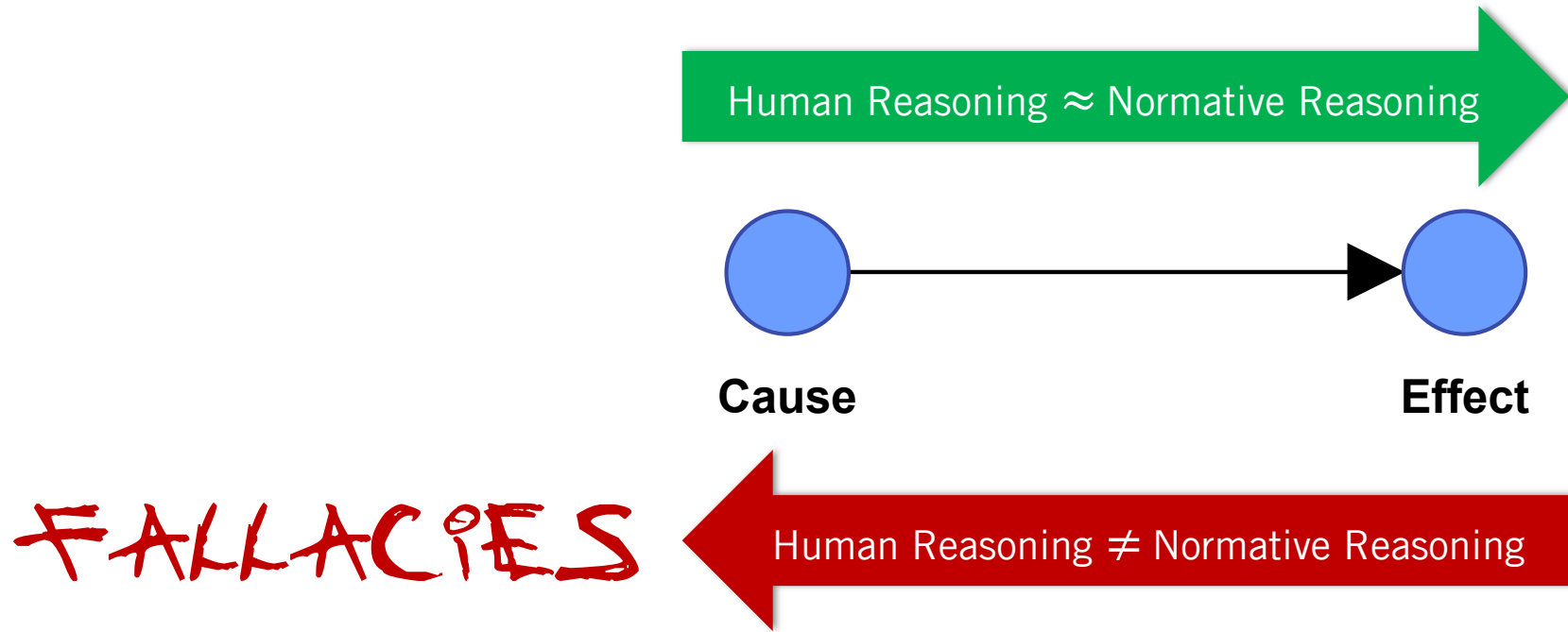
“Bayesian inference is important because it provides a normative and general-purpose procedure for reasoning under uncertainty.”

*Inductive Reasoning: Experimental, Developmental, and Computational Approaches, edited by Aidan Feeney and Evan Heit*

*This is it!*

# Why is this so important?

## Human Cognitive Limitations and Biases Under Uncertainty



# 250 Years Later...

- “...despite the mathematization of probability in the Enlightenment, mathematical probability theory remains, to this very day, **entirely unused** in criminal courtrooms, when evaluating the ‘probability’ of the guilt of a suspected criminal.”

*James Franklin, The Science of Conjecture:  
Evidence and Probability before Pascal,  
2001 The Johns Hopkins Press*

THE  
DOCTRINE  
OF  
CHANCES:  
OR,

A METHOD of Calculating the Probabilities  
of Events in PLAY.

---

THE THIRD EDITION,  
Fuller, Clearer, and more Correct than the Former.

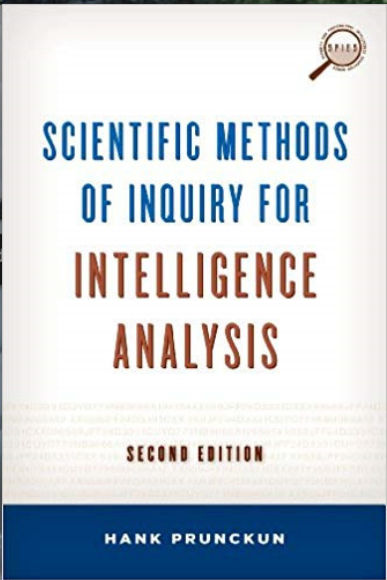
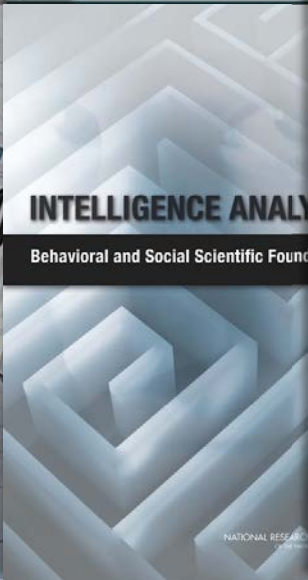
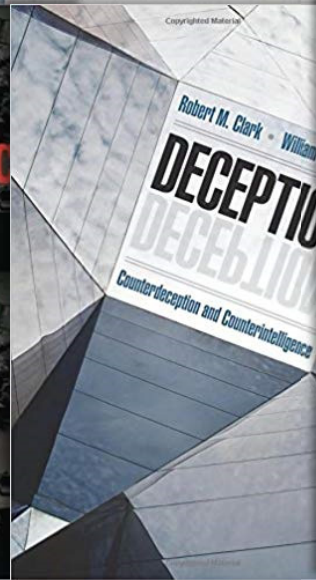
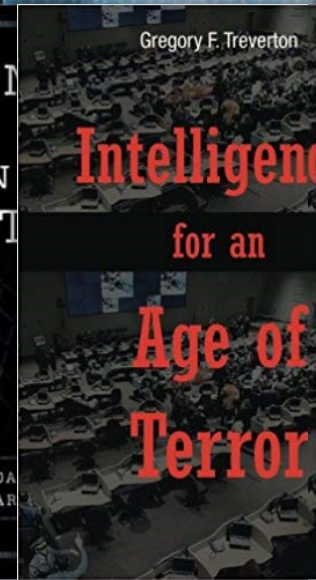
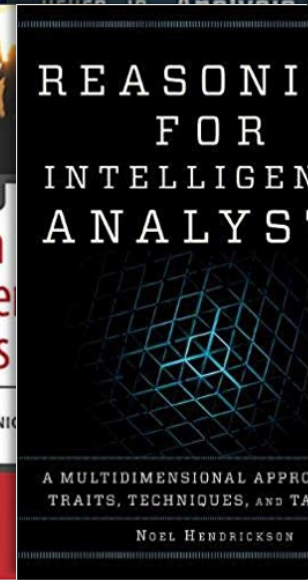
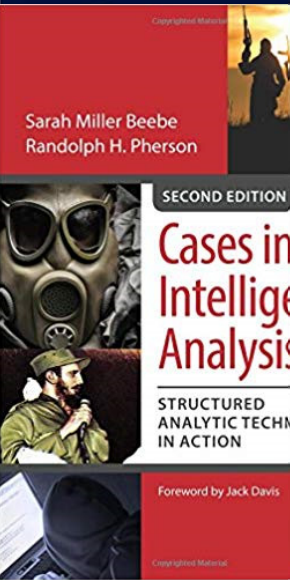
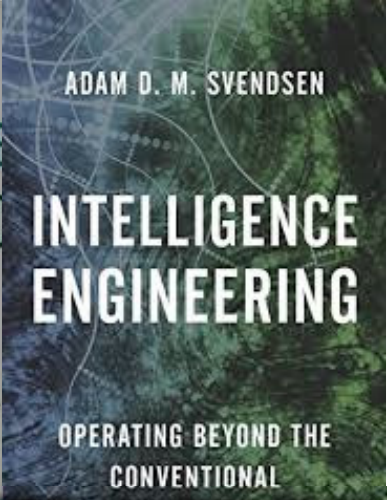
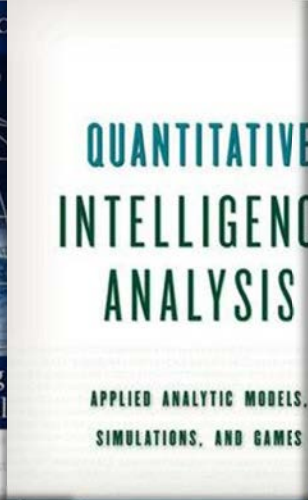
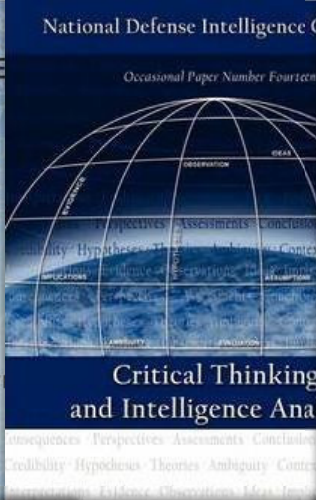
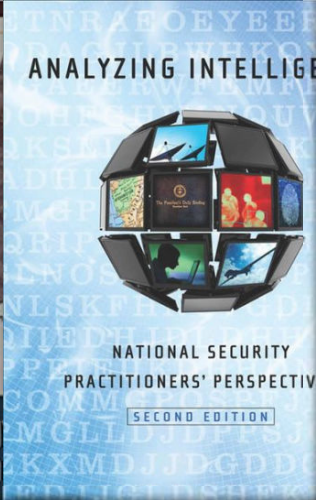
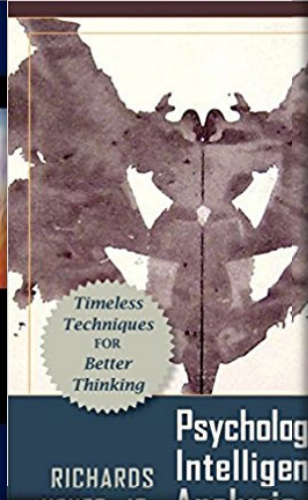
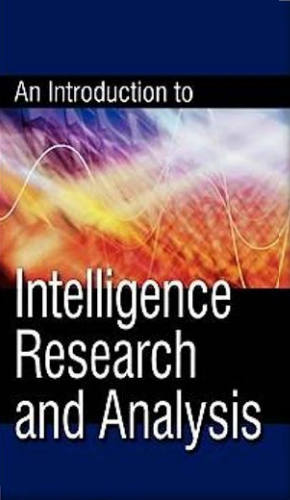
---

By A. DE MOIVRE,  
Fellow of the ROYAL SOCIETY, and Member of the ROYAL ACADEMIES  
OF SCIENCES of Berlin and Paris.



LONDON:  
Printed for A. MILLAR, in the Strand.  
MDCCLVI.







DECLASSIFIED Authority NND 947003

17- 30-3

**APPROVED FOR RELEASE 1994  
CIA HISTORICAL REVIEW PROGRAM**

**TITLE:** Bayes' Theorem For Intelligence Analysis

**AUTHOR:** Jack Zlotnick

**VOLUME:** 16 **ISSUE:** Spring **YEAR:** 1972

# Bayesian Inference in the Intelligence Community

“Due to the highly mathematical nature of Bayesian Decision Analysis, many users will feel uneasy trusting the resulting assessments.”

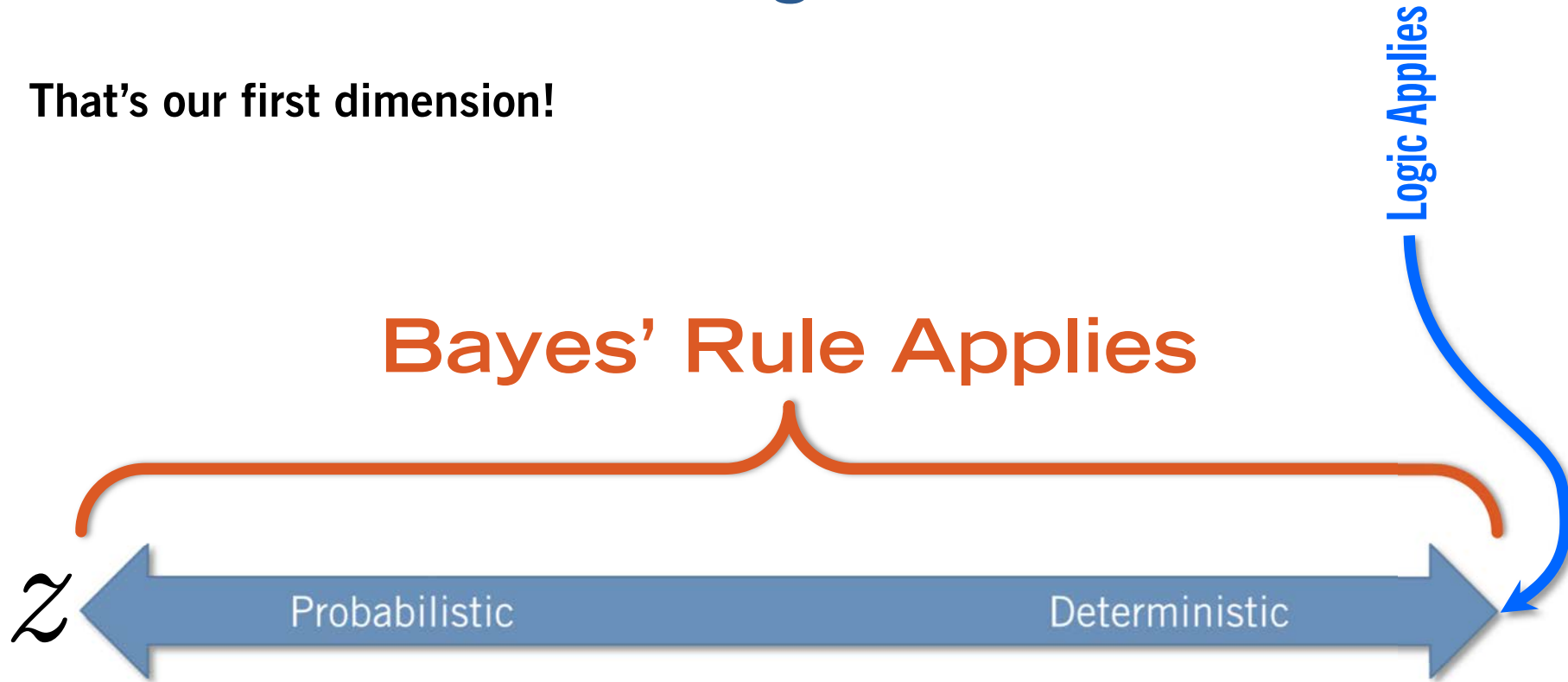
*Captain David Lawrence Graves, USAF, Bayesian Analysis Methods for Threat Prediction  
MSSI Thesis (Washington: Defense Intelligence College, July 1993)*

*Seriously?*



# Dimensions of Reasoning

That's our first dimension!



# Dimensions of Reasoning

*Statistical Science*  
2010, Vol. 25, No. 3, 289–310  
DOI: 10.1214/10-STS330  
© Institute of Mathematical Statistics, 2010

## To Explain or to Predict?

Galit Shmueli

**Abstract.** Statistical modeling is a powerful tool for developing and testing theories by way of causal explanation, prediction, and description. In many disciplines there is near-exclusive use of statistical modeling for causal explanation and the assumption that models with high explanatory power are inherently of high predictive power. Conflation between explanation and prediction is common, yet the distinction must be understood for progressing scientific knowledge. While this distinction is well understood in the philosophy of science, the statistical literature has not fully appreciated the differences that arise in the process of statistical modeling.

Description

Prediction

Explanation

Simulation

Attribution

Optimization

Association/Correlation

Model Purpose

Causation

**Key words and phrases:** Explanatory modeling, causality, predictive modeling, predictive power, statistical strategy, data mining, scientific research.

### 1. INTRODUCTION

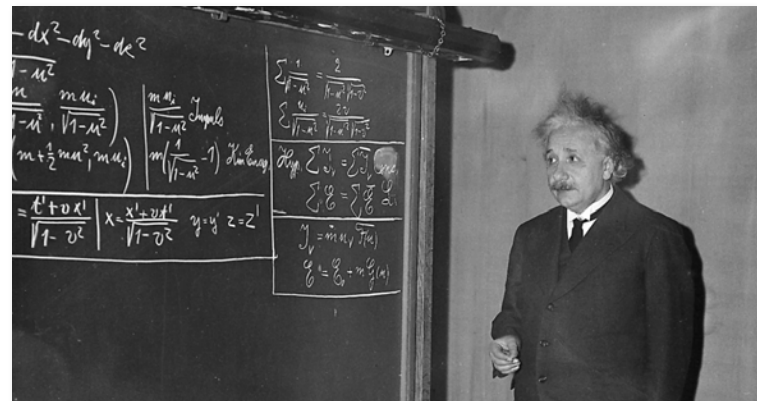
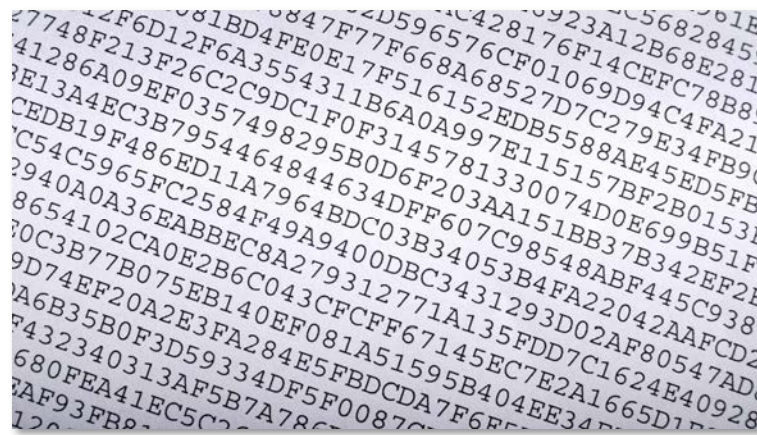
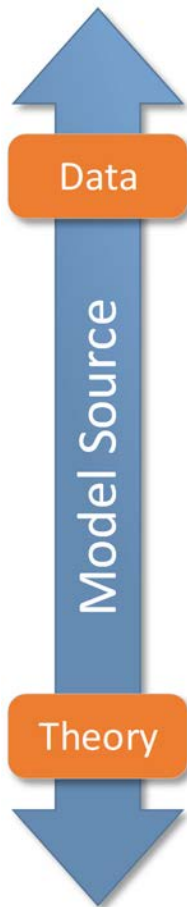
Looking at how statistical models are used in different scientific disciplines for the purpose of theory building and testing, one finds a range of perceptions regarding the relationship between causal explanation and empirical prediction. In many scientific fields such as economics, psychology, education, and environmental science, statistical models are used almost exclu-

focus on the use of statistical modeling for causal explanation and for prediction. My main premise is that the two are often conflated, yet the causal versus predictive distinction has a large impact on each step of the statistical modeling process and on its consequences. Although not explicitly stated in the statistics methodology literature, applied statisticians instinctively sense that predicting and explaining are different. This article

$x$

# Dimensions of Reasoning

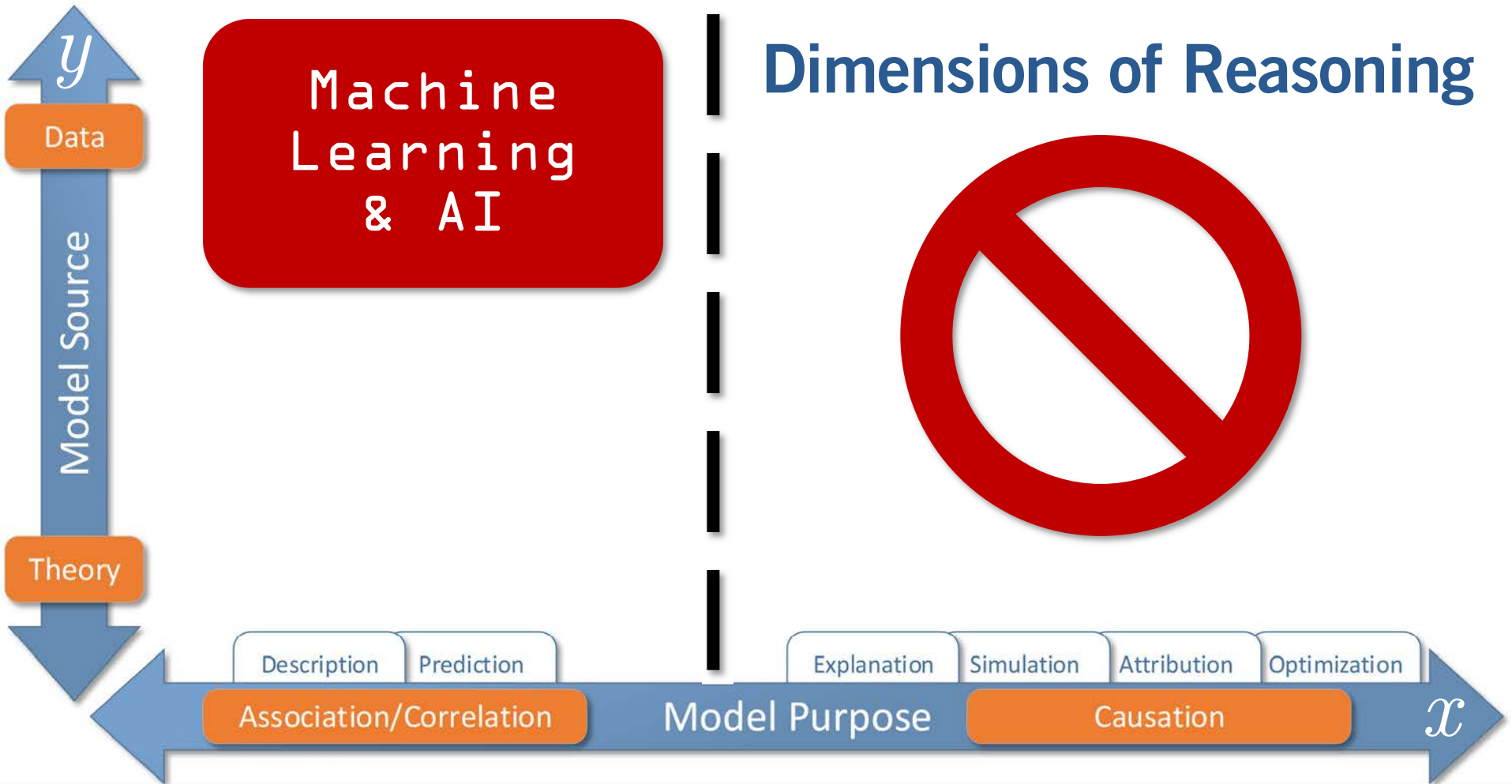
*y*

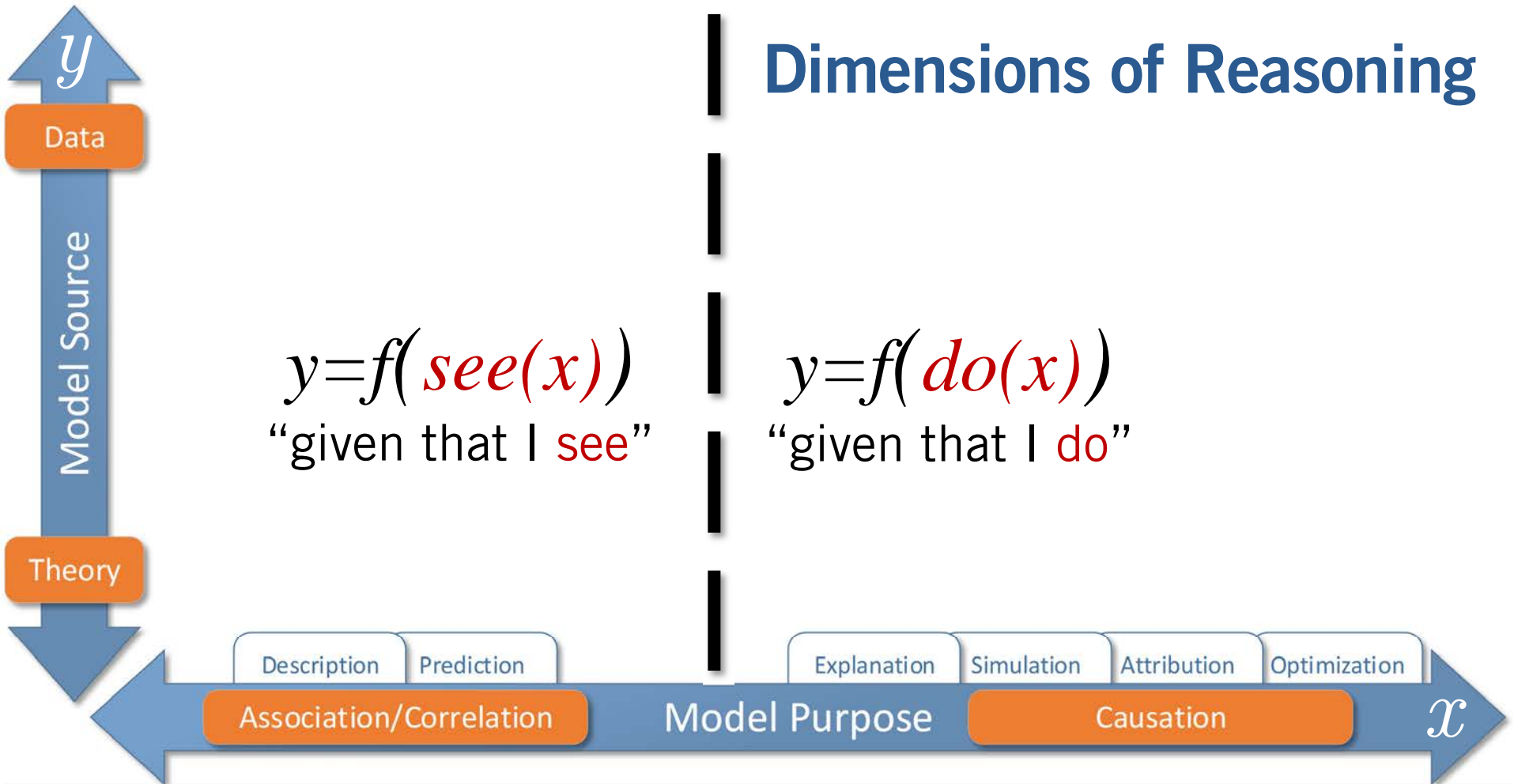


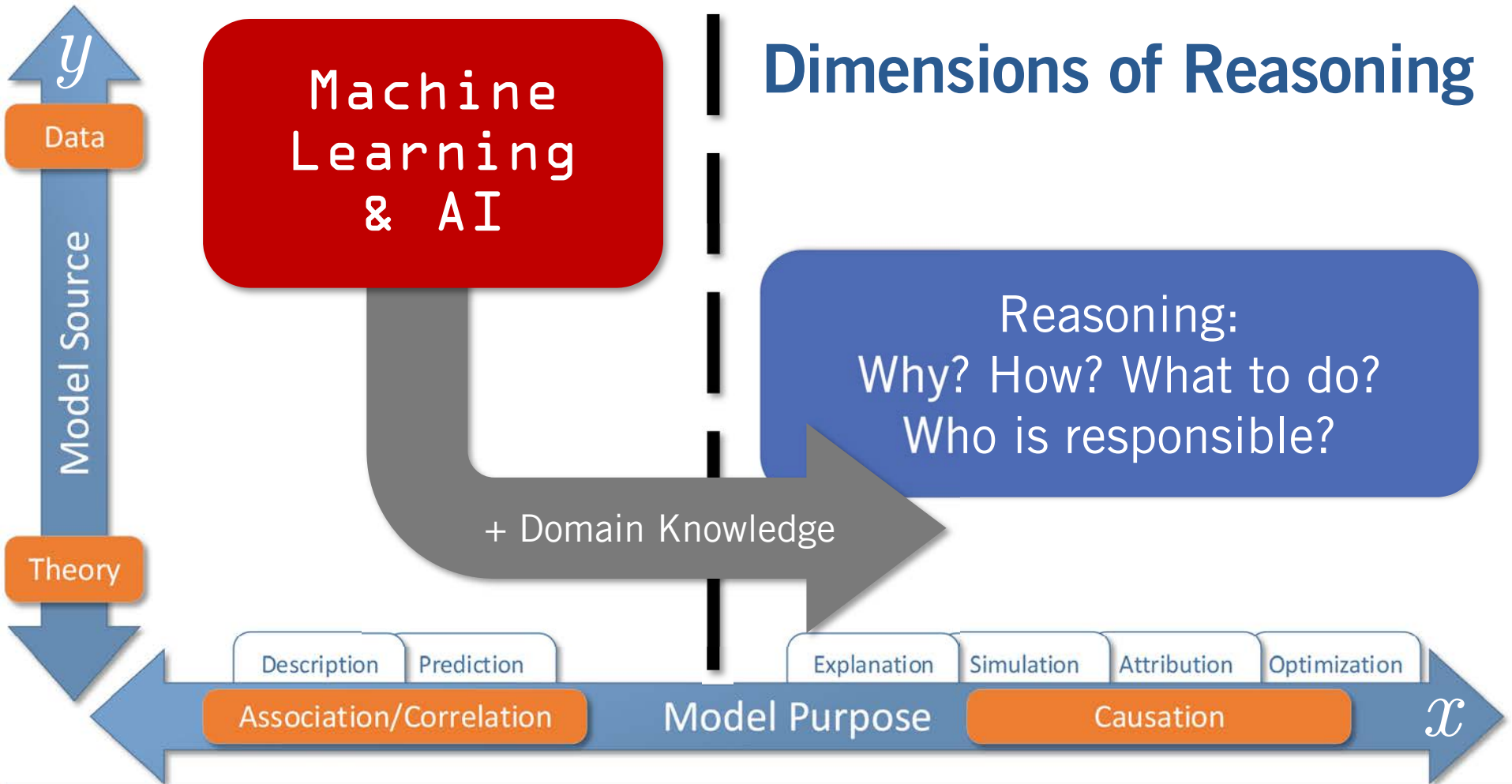
# The End of Theory?





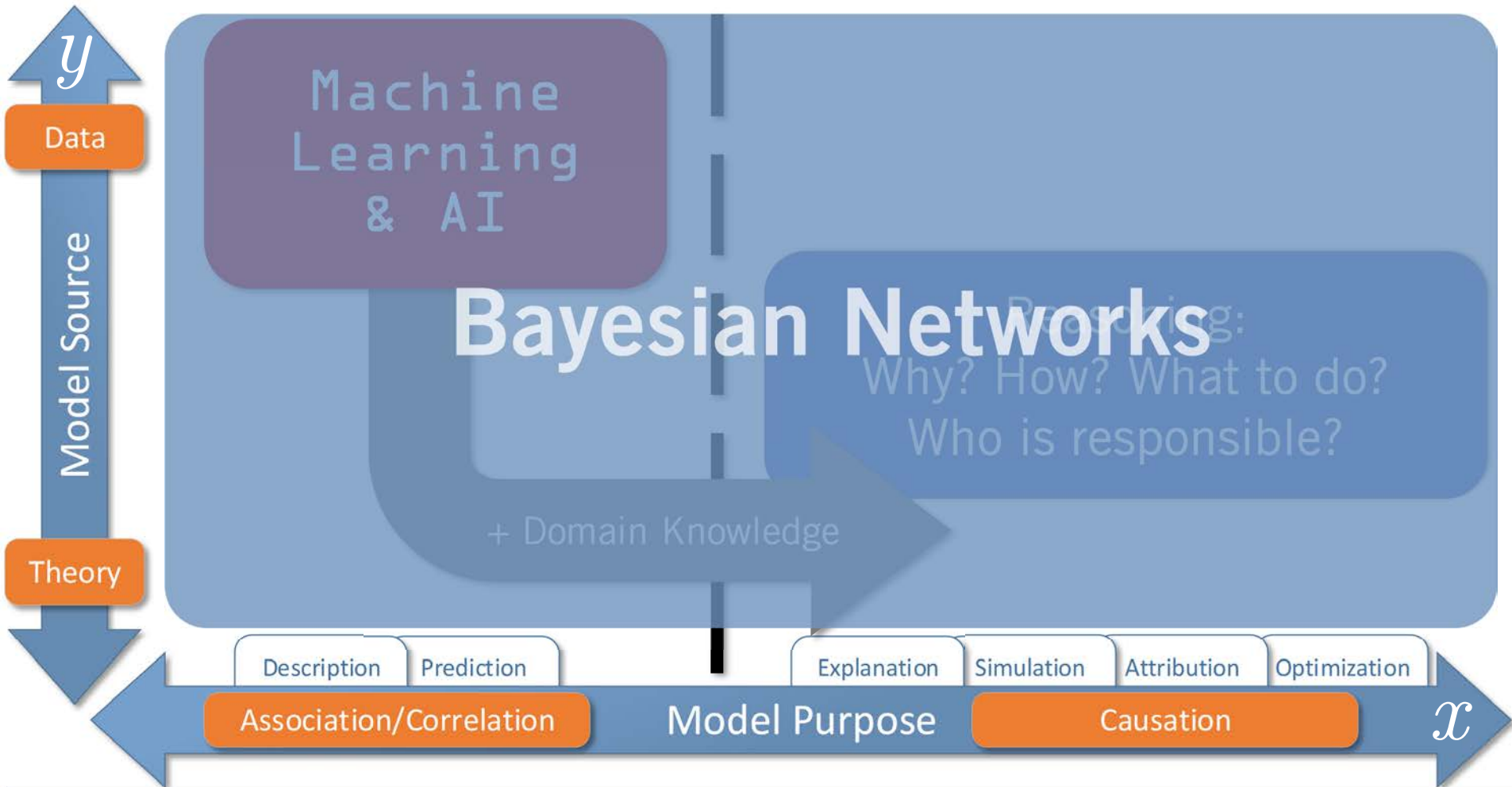




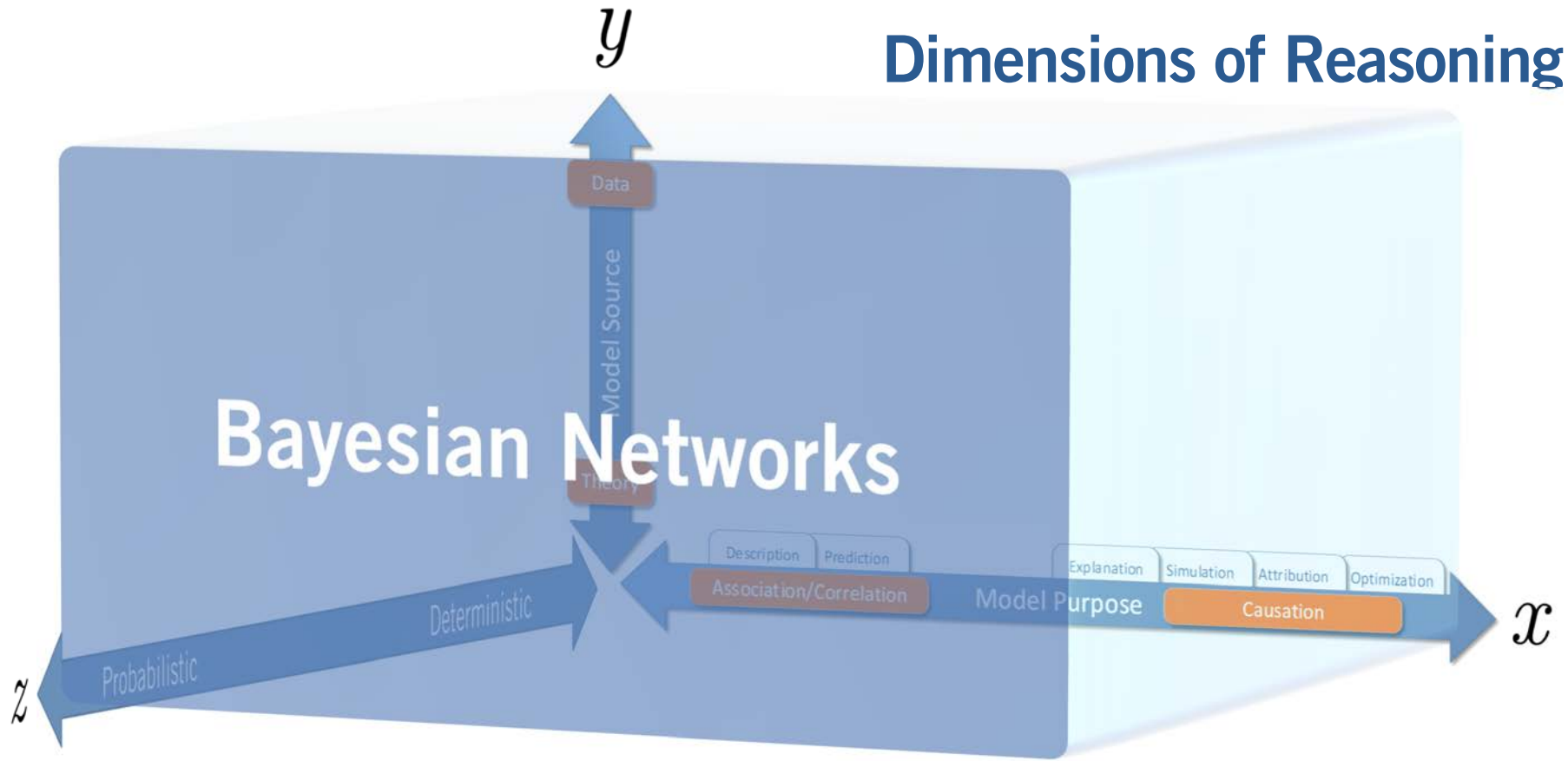








# Dimensions of Reasoning



# The New Paradigm: Bayesian Networks

BAYESIA

## CAUSALITY

MODELS, REASONING,  
AND INFERENCE



PROBABILISTIC REASONING  
IN INTELLIGENT SYSTEMS:

Networks of Plausible Inference

## BAYESIAN NETWORKS\*

Judea Pearl

Cognitive Systems Laboratory

Computer Science Department

University of California, Los Angeles, CA 90024

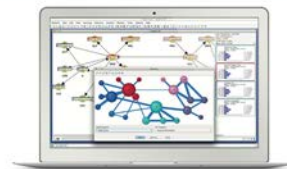
[judea@cs.ucla.edu](mailto:judea@cs.ucla.edu)

Bayesian networks were developed in the late 1970's to model distributed processing in reading comprehension, where both semantical expertise and statistical knowledge can be combined to form a coherent interpretation. The inferences filled a void in expert systems technology of the time, as they have ever since. Heckerman et al.

PROBABILISTIC GRAPH  
PRINCIPLES

Bayesian Networks  
& BayesiaLab

STEFAN CONRADY | LIONEL JOUFFE



A Practical Introduction for Researchers

[bayesia.ucl.ac.uk](http://bayesia.ucl.ac.uk) • [bayesia.com](http://bayesia.com) • [bayesia.org](http://bayesia.org)

BAYESIAN  
NETWORKS

tracking, time series, inference, uncertainty, data mining, statistics, data, decision, BAYESIAN REASONING, finance, kernels, clustering, sampling, language, classification, trees, and algorithms, labels, networks, filtering, recognition, prediction, control, modelling, robotics, MATLAB, LEARNING, graphs, bioinformatics, computational intelligence

David Barber

Studies in Computational Intelligence

Dawn E. Holmes  
Lakhmi C. Jain (Eds.)

Innovations in  
Bayesian Networks

Theory and Applications

Bayesian Networks  
A Practical Guide to



WILEY

STATISTICS

Editors  
OLIVIER POURRET, PATRICK NAIM  
AND BRUCE MARGOT

Bayesian  
Networks

Computer Science and Data Analysis Series

Bayesian  
Artificial  
Intelligence  
SECOND EDITION

Kevin B. Korb  
Ann E. Nicholson

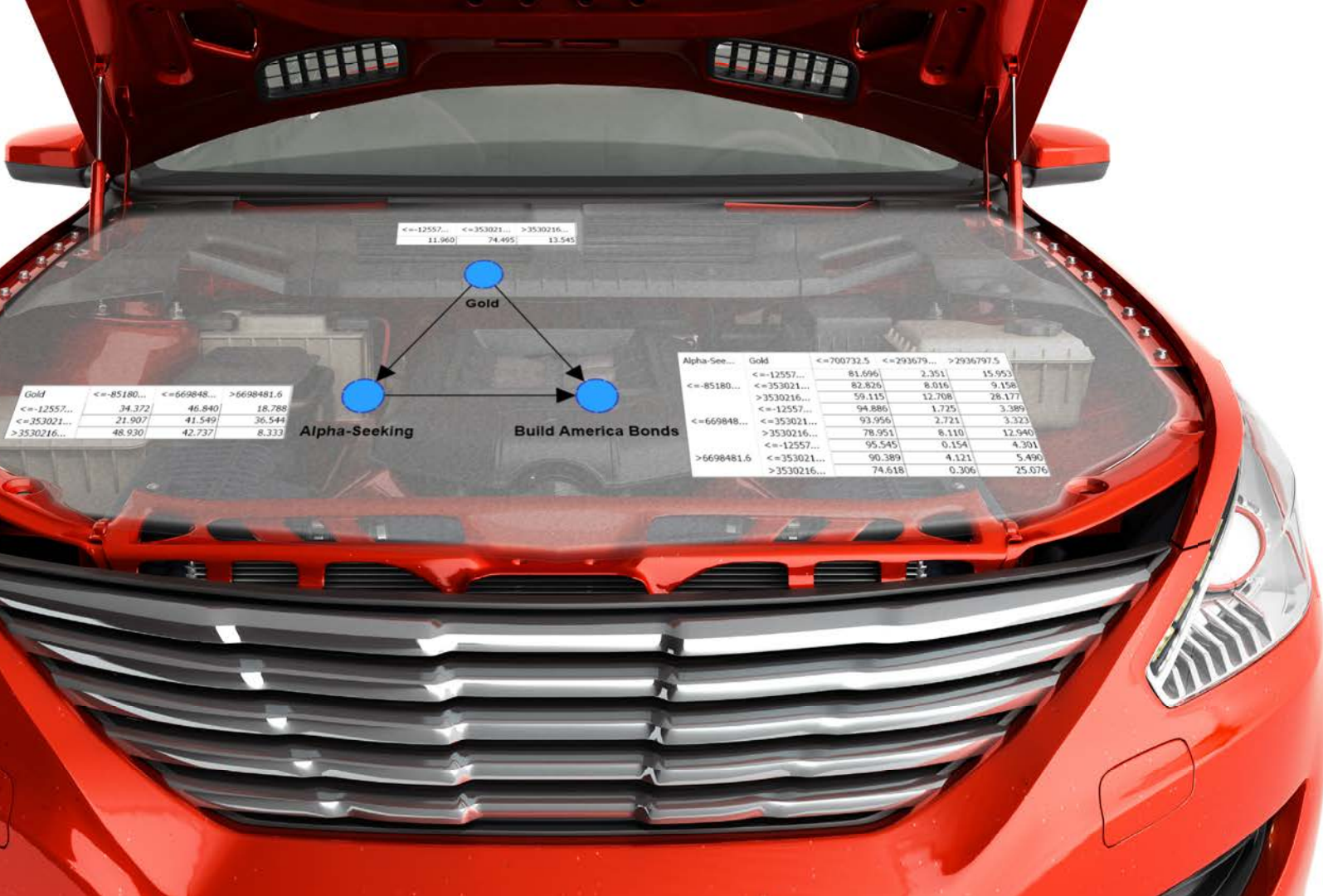
Causation, Prediction



RICHARD E. NEAPOLITAN  
PRENTICE HALL SERIES IN ARTIFICIAL INTELLIGENCE

Peter Spirtes,  
Clark Glymour, and  
Richard Scheines





|             |             |             |
|-------------|-------------|-------------|
| <=-12557... | <=353021... | >3530216... |
| 11.960      | 74.495      | 13.545      |

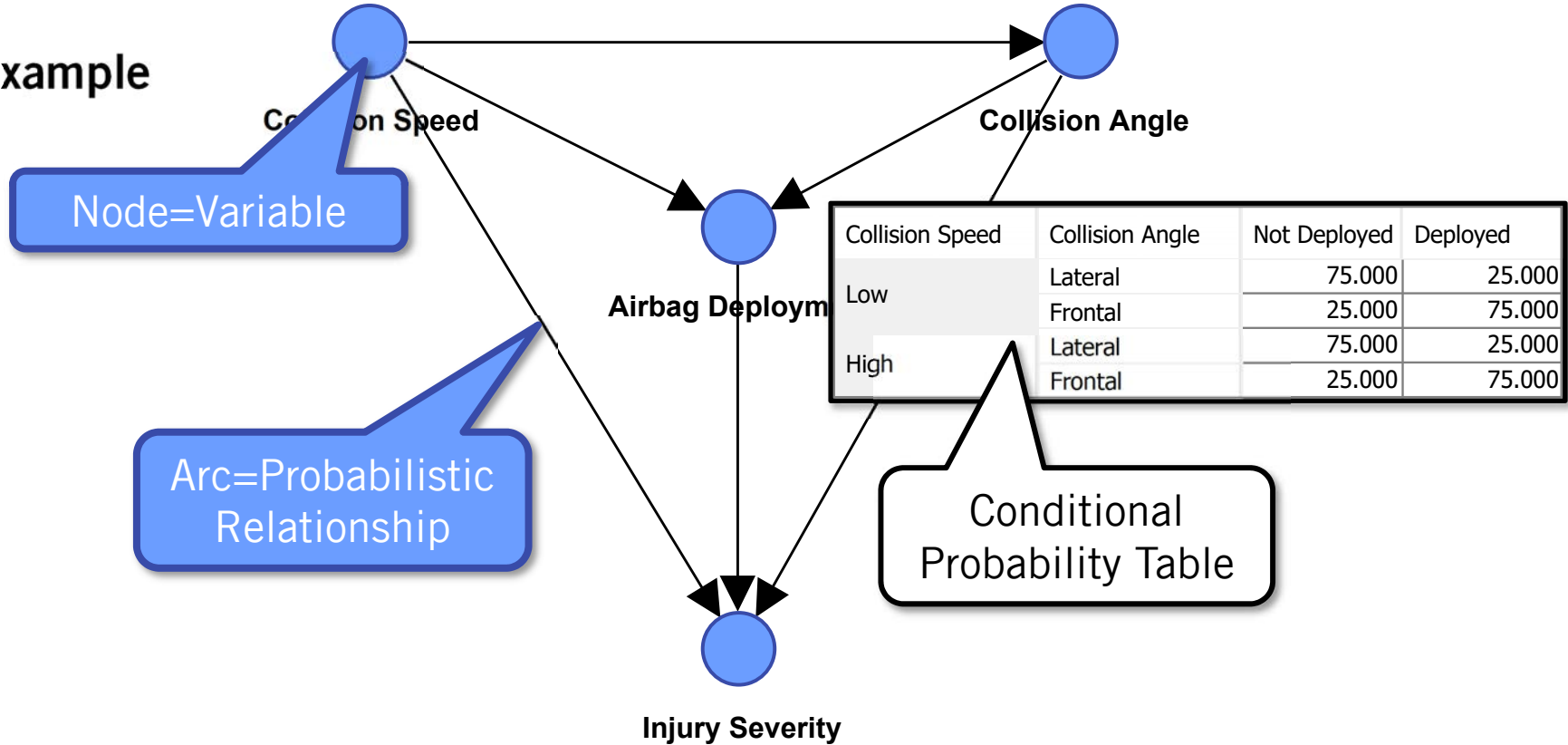
|             |             |             |            |
|-------------|-------------|-------------|------------|
| Gold        | <=-85180... | <=669848... | >6698481.6 |
| <=-12557... | 34.372      | 46.840      | 18.788     |
| <=353021... | 21.907      | 41.549      | 36.544     |
| >3530216... | 48.930      | 42.737      | 8.333      |

|              |             |            |             |            |
|--------------|-------------|------------|-------------|------------|
| Alpha-See... | Gold        | <=700732.5 | <=293679... | >2936797.5 |
| <=-85180...  | <=-12557... | 81.696     | 2.351       | 15.953     |
| >3530216...  | <=353021... | 82.826     | 8.016       | 9.158      |
| <=-12557...  | >3530216... | 59.115     | 12.708      | 28.177     |
| <=669848...  | <=-12557... | 94.886     | 1.725       | 3.385      |
| >3530216...  | <=353021... | 93.956     | 2.721       | 3.323      |
| >6698481.6   | >3530216... | 78.951     | 8.110       | 12.940     |
|              | <=-12557... | 95.545     | 0.154       | 4.301      |
|              | <=353021... | 90.389     | 4.121       | 5.490      |
|              | >3530216... | 74.618     | 0.306       | 25.076     |



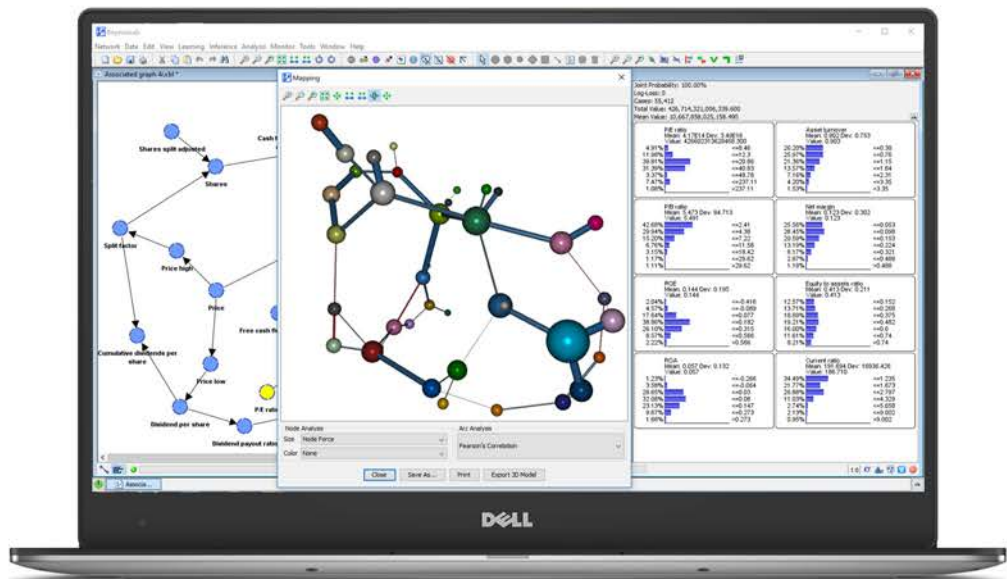
# The New Paradigm: Bayesian Networks

Example



# Mathematical Formalism → Research Software





A desktop software for:

- encoding
- learning
- editing
- performing inference
- analyzing
- simulating
- optimizing

with **Bayesian networks**.

# Artificial Intelligence?



# Implementation Example



<http://pubsonline.informs.org/journal/inte/>

INTERFACES

Vol. 47, No. 1, January–February 2017, pp. 1–21  
ISSN 0092-2102 (print), ISSN 1526-551X (online)



THE FRANZ EDELMAN AWARD  
*Achievement in Operations Research*

## Bayesian Networks for Combat Equipment Diagnostics

David Aebischer,<sup>a</sup> John Vatterott, Jr.,<sup>a</sup> Michael Grimes,<sup>a</sup> Andrew Vatterott,<sup>a</sup> Roderick Jordan,<sup>a</sup> Carlo Reinoso,<sup>a</sup> Bradford Alex Baker,<sup>a</sup> William D. Aldrich,<sup>a</sup> Luis Reinoso,<sup>a</sup> Rodolfo Villalba,<sup>a</sup> Michael Johnson,<sup>a</sup> Christopher Myers,<sup>a</sup> Stefan Conrady,<sup>a</sup> Joseph A. Tatman,<sup>a</sup> Suzanne M. Mahoney,<sup>a</sup> Darrin L. Whaley,<sup>a</sup> Amanda B. Hepler<sup>a</sup>

<sup>a</sup>U.S. Army Communications Electronics Command, Aberdeen, Maryland 21001

**Contact:** david.a.aebischer.civ@mail.mil (DA), johnjr@stltrades.com (JV), mgrimes@vettechgrp.com (MG), andrewv@stltrades.com (AV), roderickj@stltrades.com (RJ), carlor@stltrades.com (CR), abbaker@vettechgrp.com (BAB), billa@stltrades.com (WDA), luisr@stltrades.com (LR), rudyv@stltrades.com (RV), michaelj@stltrades.com (MJ), chrism@stltrades.com (CM), stefan.conrady@bayesia.us (SC), jatatman@innovatedecisions.com (JAT), smmahoney@innovatedecisions.com (SMM), dlwhaley@innovatedecisions.com (DLW), abhepler@innovatedecisions.com (ABH)

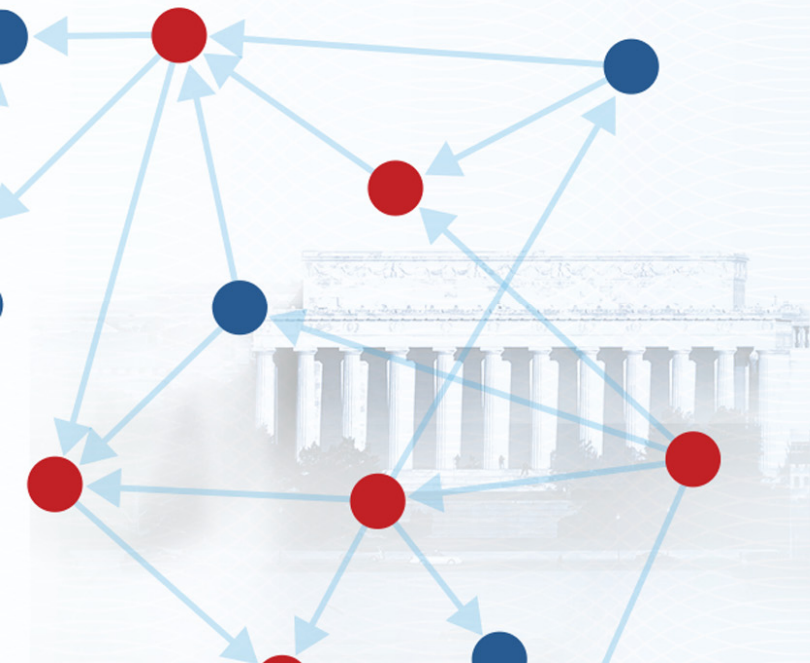
<https://doi.org/10.1287/inte.2016.0883>

Copyright © 2017 INFORMS

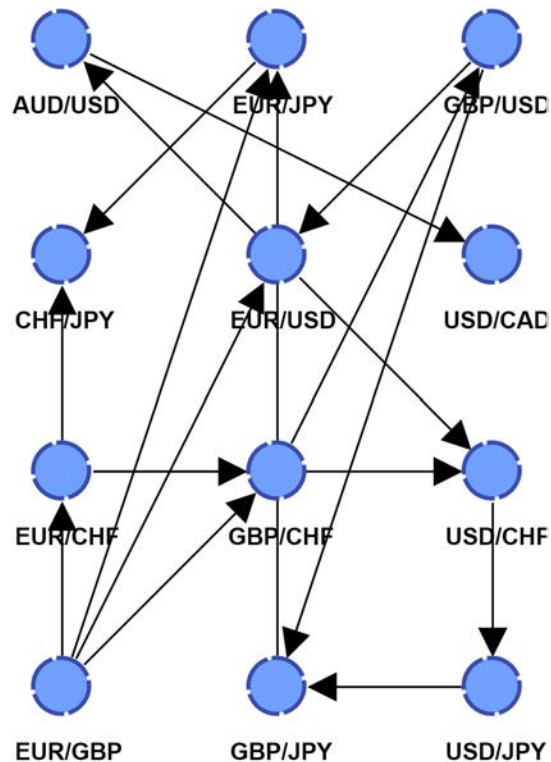
**Abstract.** The lives of U.S. soldiers in combat depend on complex weapon systems and advanced technologies. In combat conditions, the resources available to support the operation and maintenance of these systems are minimal. Following the failure of a critical system, technical support personnel may take days to arrive via helicopter or ground



# Conceptual Advantages of Bayesian Networks for Reasoning



# The New Paradigm: Bayesian Networks



## Key Properties

- Compact representation of the **Joint Probability Distribution**
- No distinction between dependent and independent variables
- Omni-directional Inference
- Nonparametric
- Probabilistic
- Causal

# The New Paradigm: Bayesian Networks

## Key Properties of Bayesian Networks

- No distinction between dependent and independent variables.
- Numerical and categorical variables are treated identically.
- Nonparametric.

Compare to algebraic formula:

Representation of **one** variable of the joint probability distribution, i.e.  $y=f(x)$

Dependent

$$y = \beta_0 + \beta_1 x_1 + \dots + \beta_n x_n$$

Independent

Independent




# The New Paradigm: Bayesian Networks

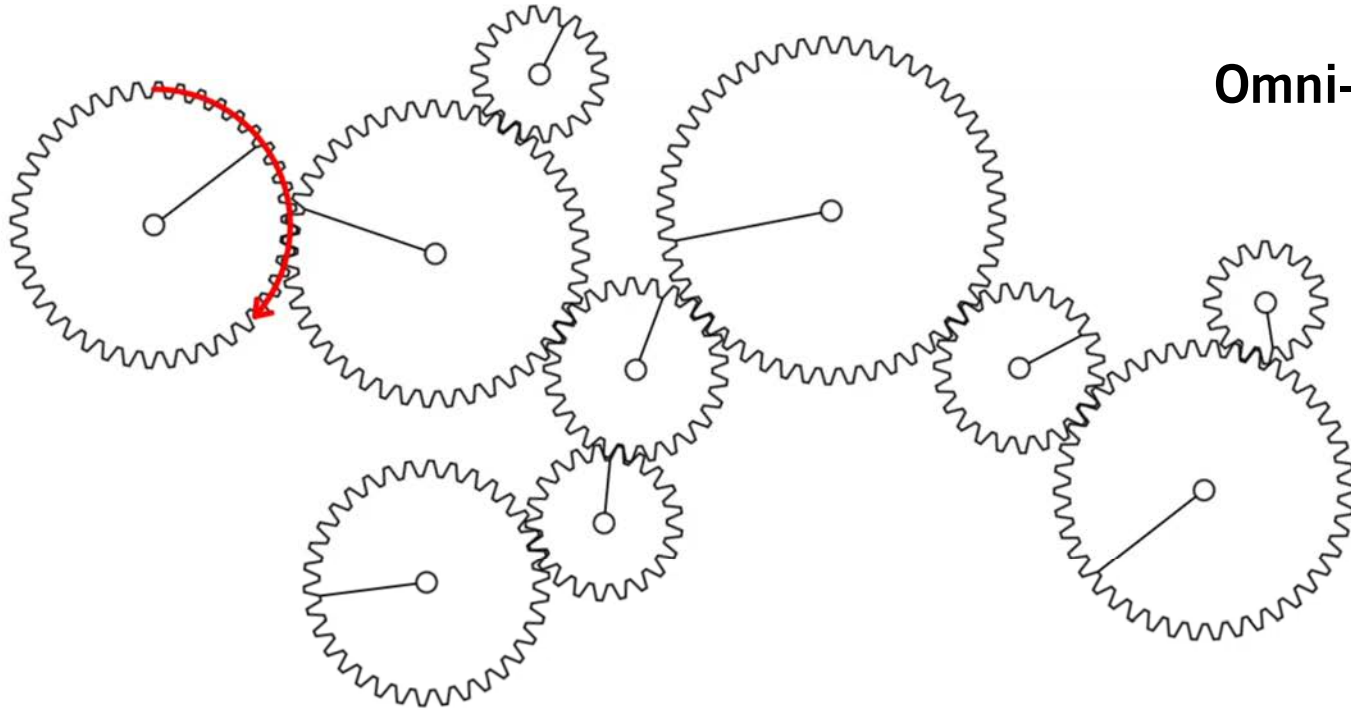
## Key Properties of Bayesian Networks

- Omni-directional Inference, i.e. evaluation is always performed in all directions.

Compare to “uni-directional” algebraic formula and human intuition

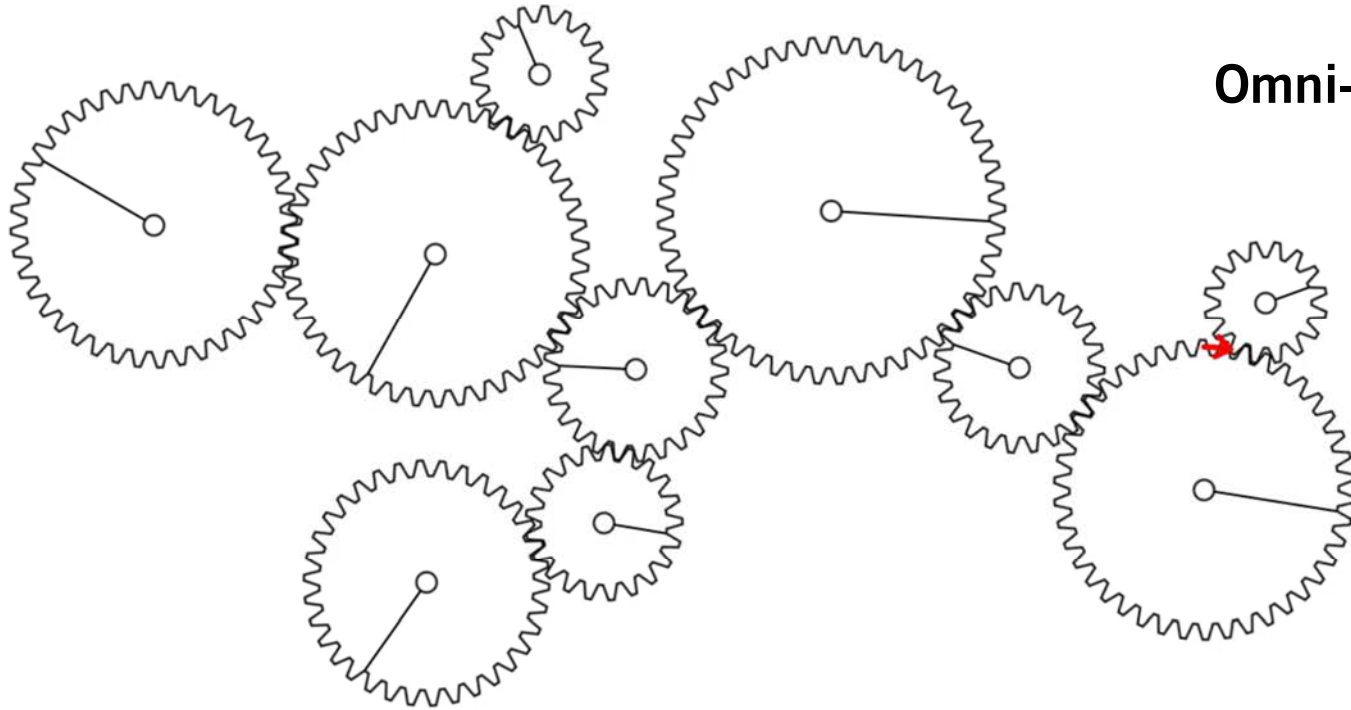

$$y = \beta_0 + \beta_1 x_1 + \dots + \beta_n x_n$$

# The New Paradigm: Bayesian Networks



**Omni-Directional  
Inference**

# The New Paradigm: Bayesian Networks

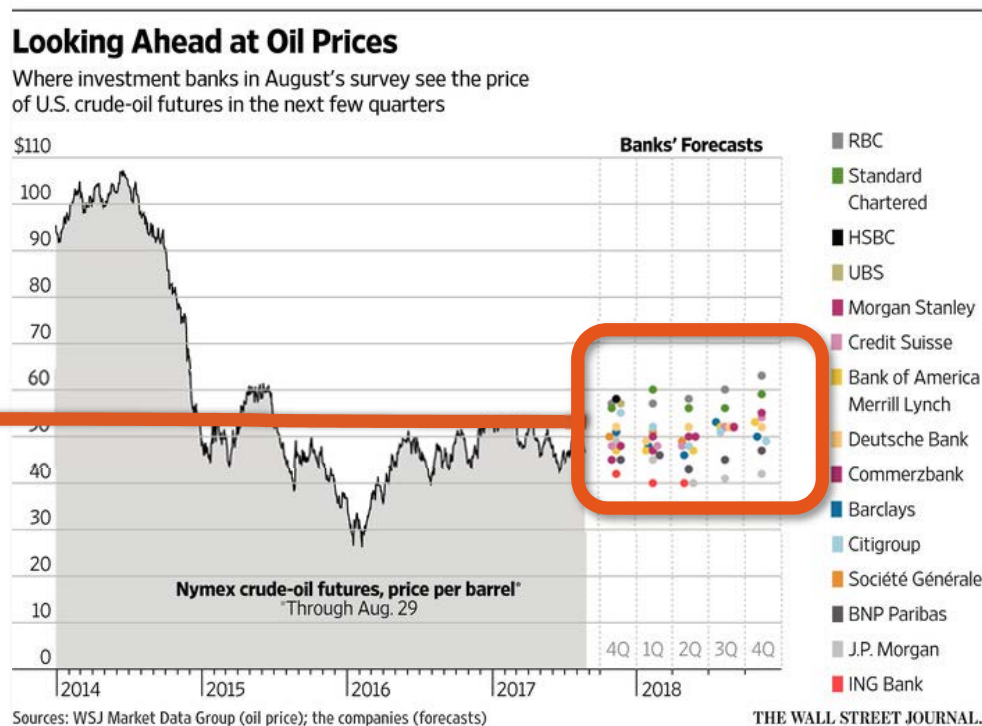


**Omni-Directional  
Inference**

# Bayesian Networks

## Key Properties

- Bayesian networks are inherently probabilistic.
- Evidence and inference are represented as distributions.
- Inference can be performed with partial evidence.





# The New Paradigm: Bayesian Networks

## Key Properties of Bayesian Networks

- Bayesian networks are inherently probabilistic.
- Evidence and inference are represented by distributions.
- Inference can be performed with partial evidence.

Deterministic  
Point Estimate

Compare to algebra

Single  
Value Input

Single  
Value Input

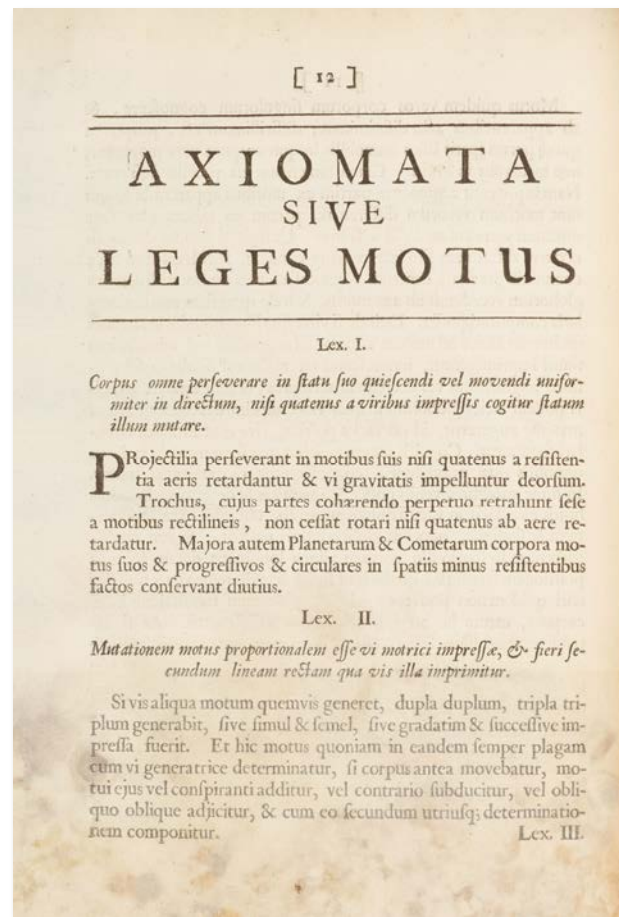
$$y = \beta_0 + \beta_1 x_1 + \dots + \beta_n x_n$$

# Bayesian Networks

## Key Properties of Bayesian Networks

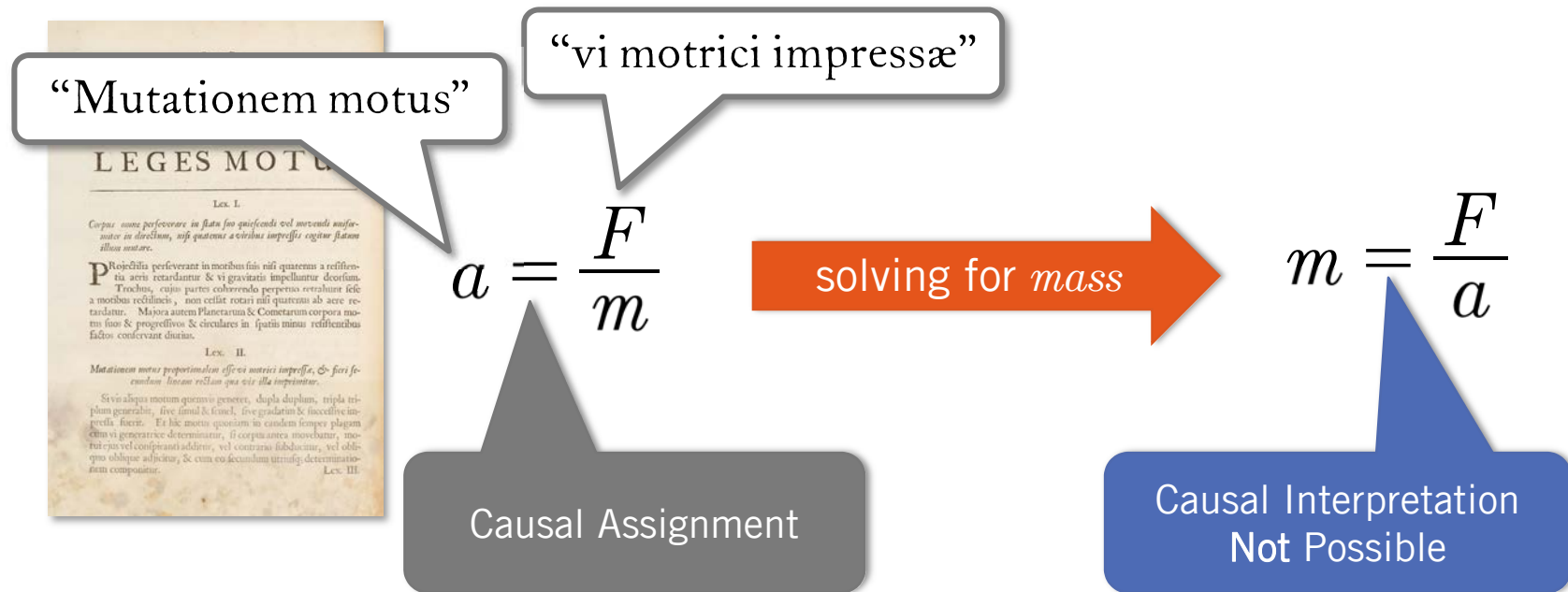
- Bayesian networks can encode causal direction, algebra cannot.
- Example: Newton's Second Law of Motion

$$F = m \cdot a$$



# The New Paradigm: Bayesian Networks

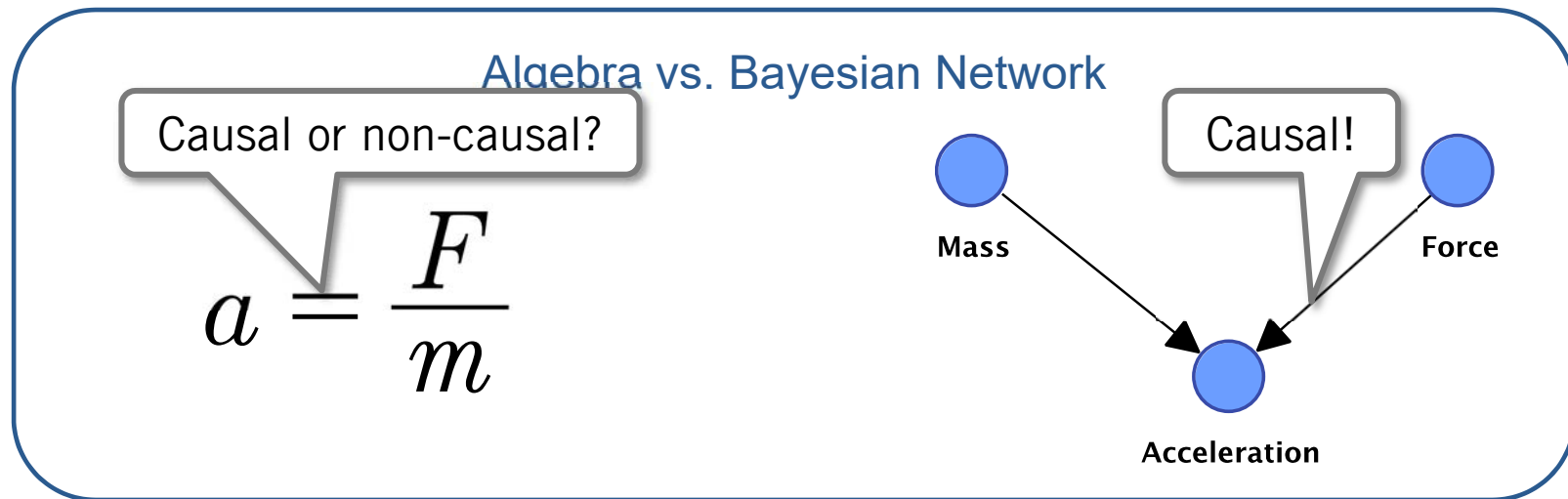
## Limitations of Algebra: Newton's Second Law of Motion



# The New Paradigm: Bayesian Networks

## Key Properties of Bayesian Networks

- Bayesian networks can formally encode a causal direction\*, algebra cannot.

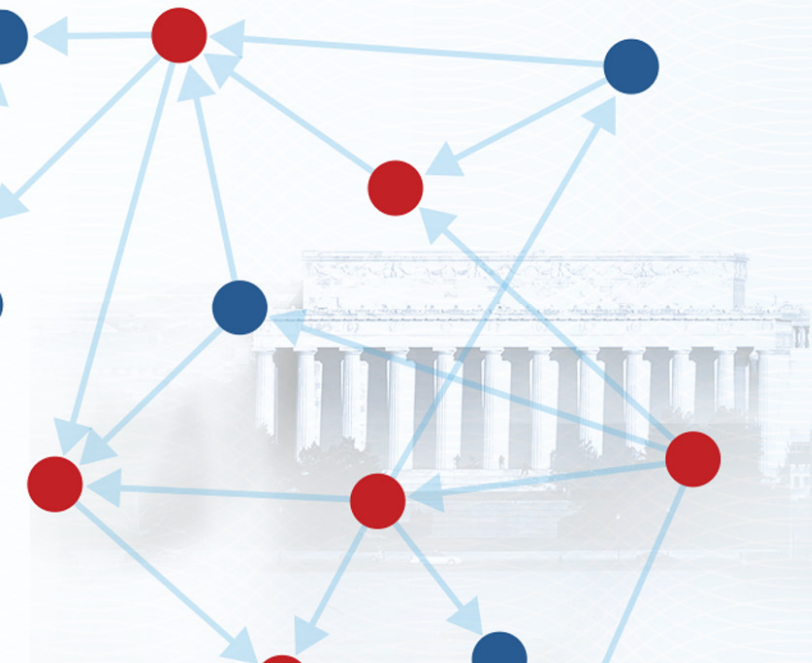


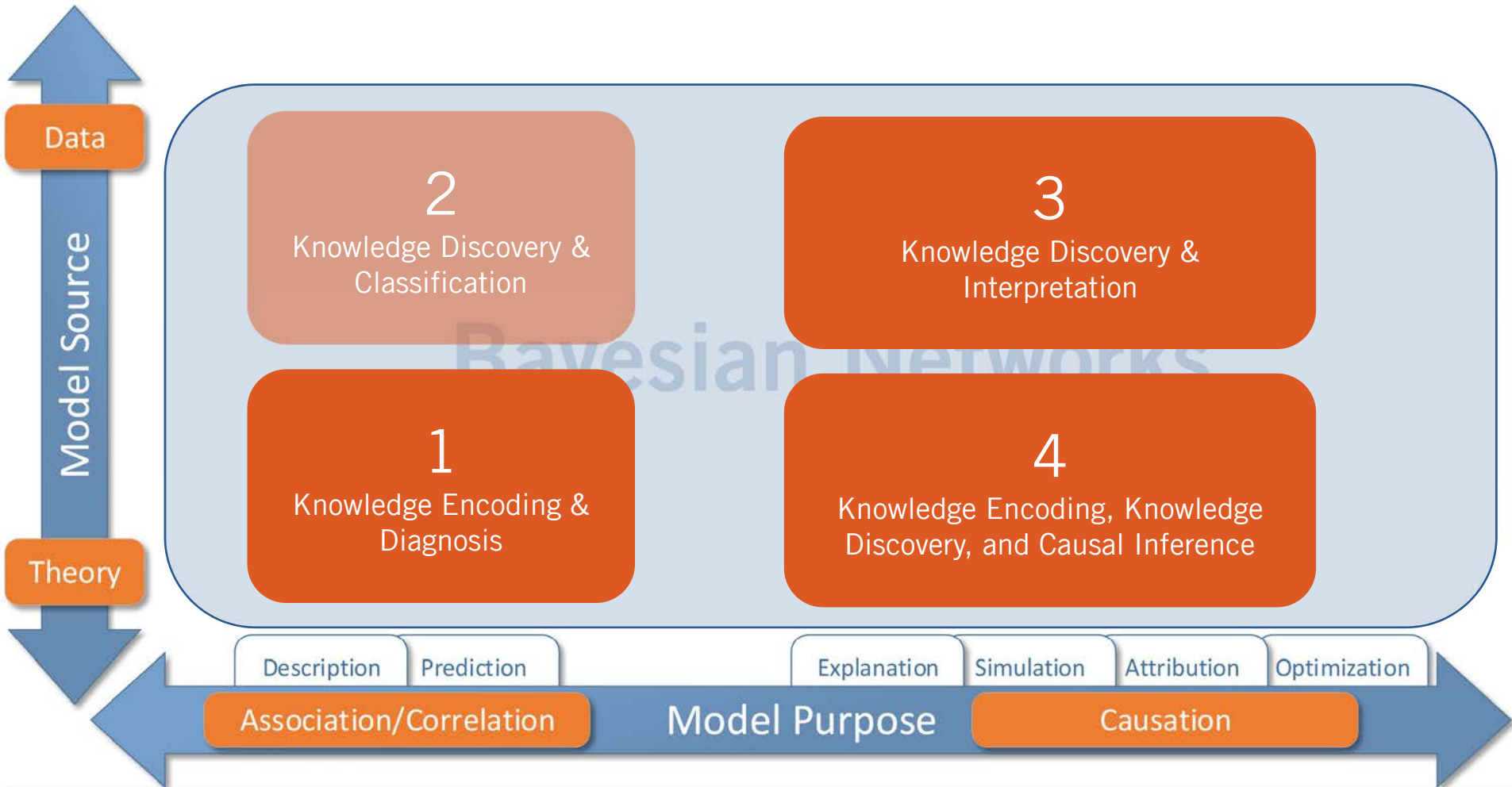
\*Applies to manually encoded networks

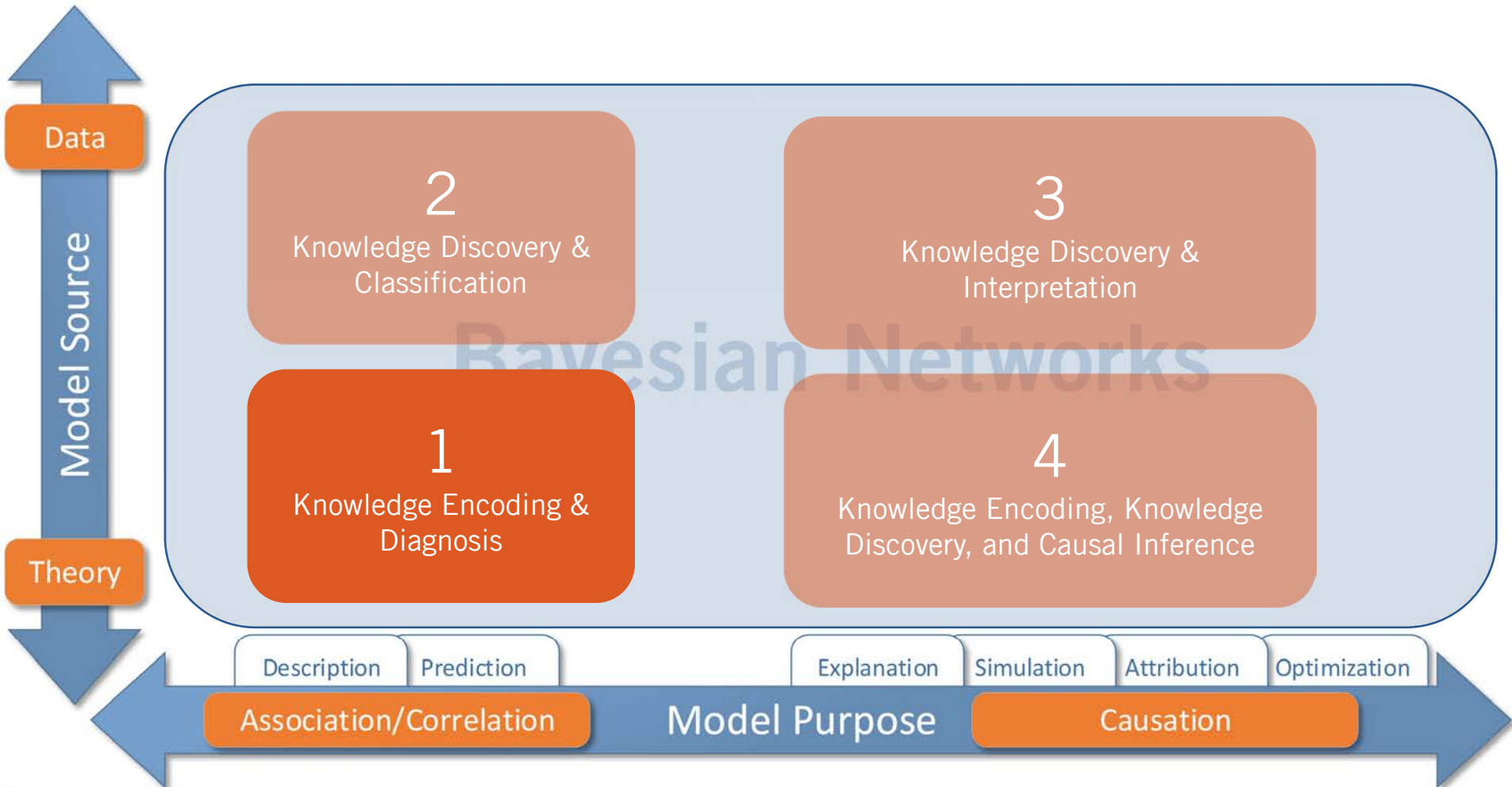




# Examples Bayesian Networks in Practice





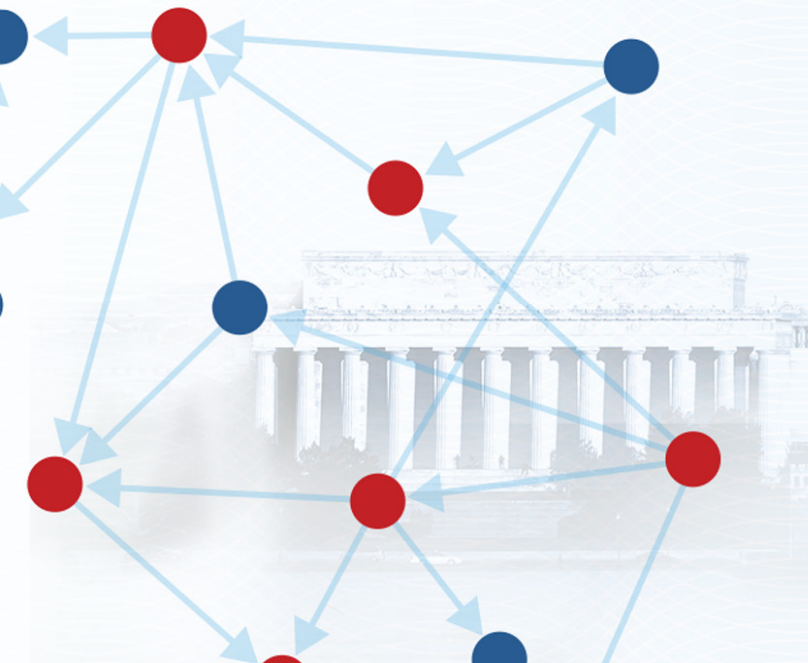






# Friend or Foe?

## Diagnostic Decision Support Under Extreme Uncertainty



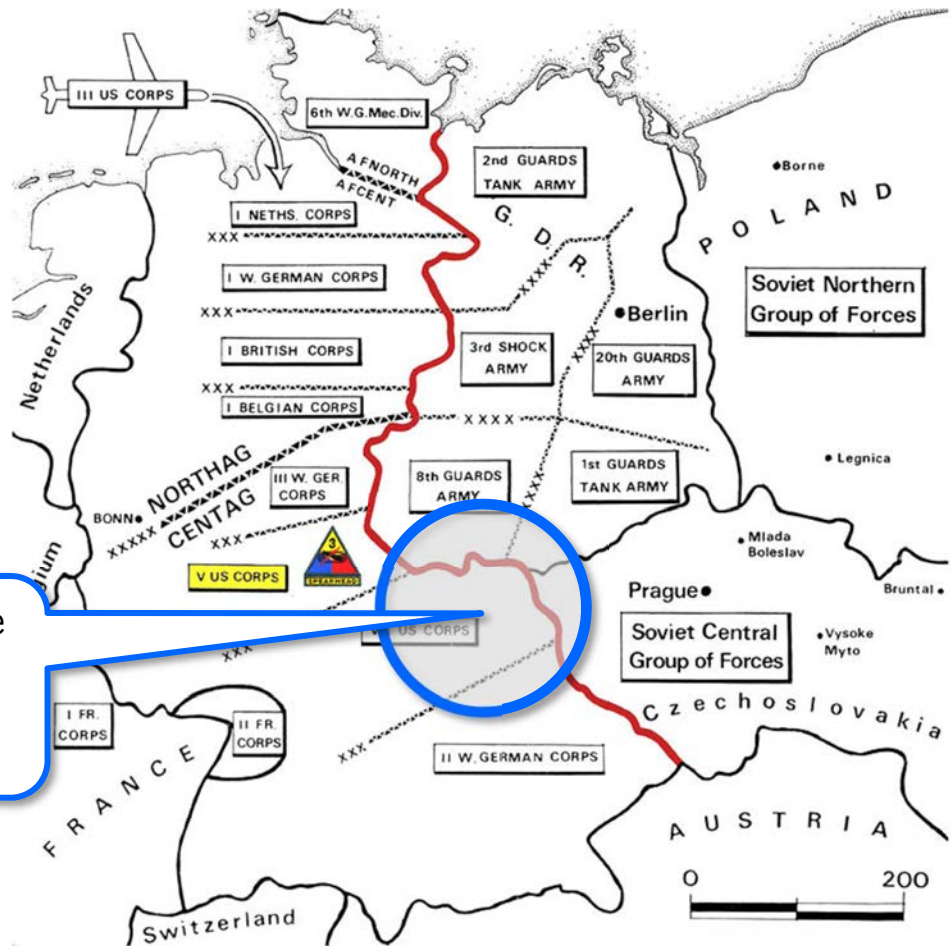


# Friend or Foe?

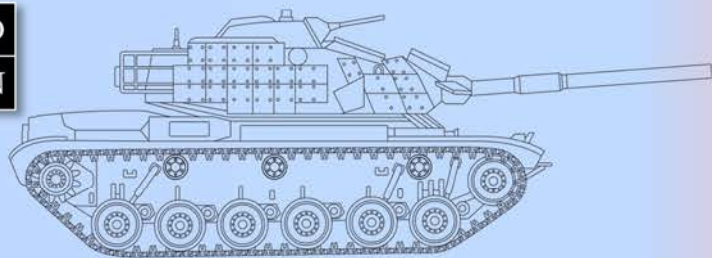
## A Counterfactual Scenario:

- Central Europe, Summer of 1989
- Warsaw Pact forces invade West Germany

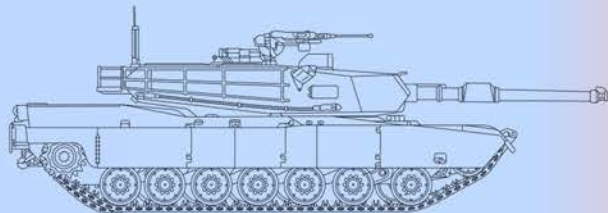
Nations in Combat within a 60-mile Radius: West Germany, East Germany, France, Canada, USA, Czechoslovakia, Soviet Union, etc.



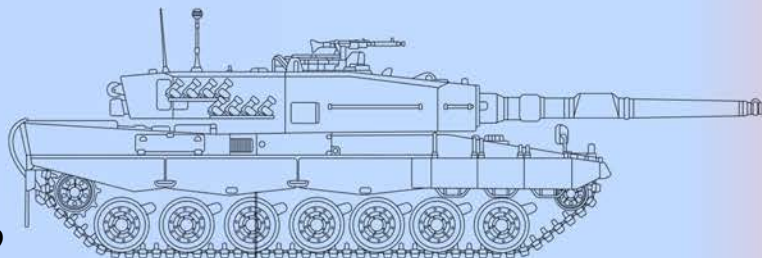
Map: Strategic Geography: NATO, the Warsaw Pact, and the Superpowers; by Hugh Faringdon; 1989.



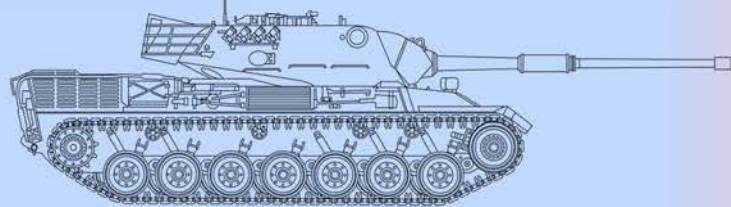
M48/M60



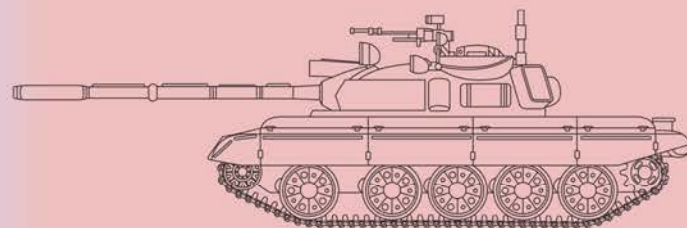
M1A1



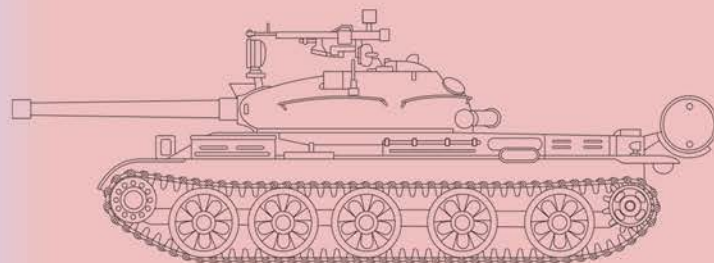
Leopard 2



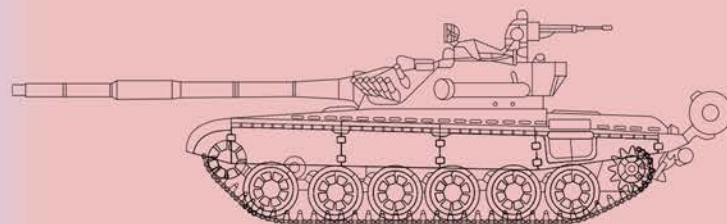
Leopard 1



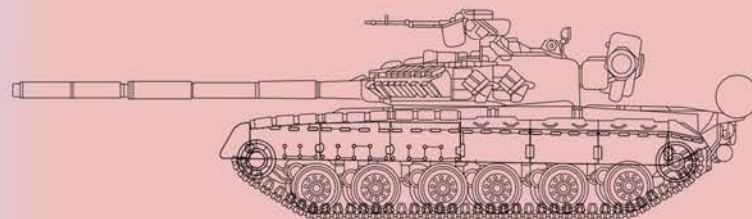
T-55



T-62



T-72



T-80



# Friend or Foe?

## Tank Identification Handbook, 1982



ST 7-193 F  
UNITED STATES

### TANK IDENTIFICATION HANDBOOK

UNITED STATES ARMY INFANTRY SCHOOL  
FORT BENNING, GEORGIA

### T-72 TANK



SUCCESSOR TO THE T-62 BATTLE TANK

1. TURRET CENTRALLY MOUNTED ON CHASSIS
2. TANK COMMANDER'S IR SEARCHLIGHT IS LOCATED ON RIGHT OF TURRET HATCH
3. VEHICLE ID NIGHT LIGHT
4. GUN SIMILAR TO T-62
5. THREE TRACK SUPPORT ROLLERS
6. SIX EVENLY SPACED ROAD WHEELS

1. WADING CAPABILITY SIMILAR TO T-55
2. GUN 115MM TO 122MM
3. COAX 7.62MM MG
4. CBR PROTECTIVE LINER
5. CREW: 4







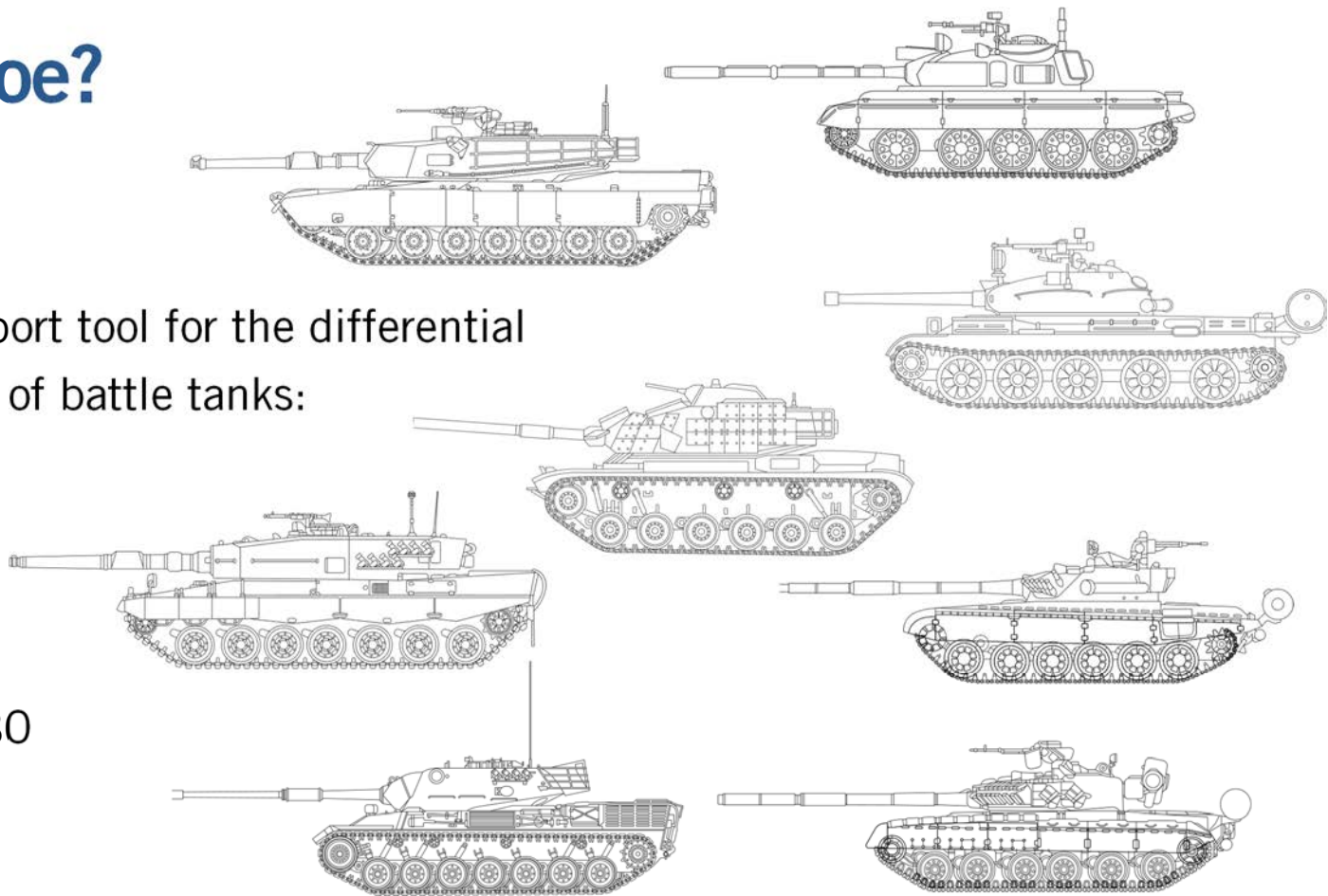
**“Fratricide is widely cited to account for between  
2% to 20% of Blue (friendly force) casualties.”**

**Robert Rasmussen, The Wrong Target  
Joint Forces Staff College, 2007**

# Friend or Foe?

## Objective

- Decision support tool for the differential identification of battle tanks:
- M1A1
- M48/60
- Leopard 1/2
- T-55/62/72/80



# Friend or Foe?

## This is an inference task!

- $P(\text{M1A1} \mid \text{Turret Shape, Barrel Length, Wheels, Wheel Distance, etc.})=?$
- $P(\text{T-80} \mid \text{Turret Shape, Barrel Length, Wheels, Wheel Distance, etc.})=?$
- Probability of  $\text{Turret Shape, Barrel Length, Wheels, Wheel Distance, etc.})=?$
- $P(\text{M60} \mid \text{Turret Shape, Barrel Length, Wheels, Wheel Distance, etc.})=?$

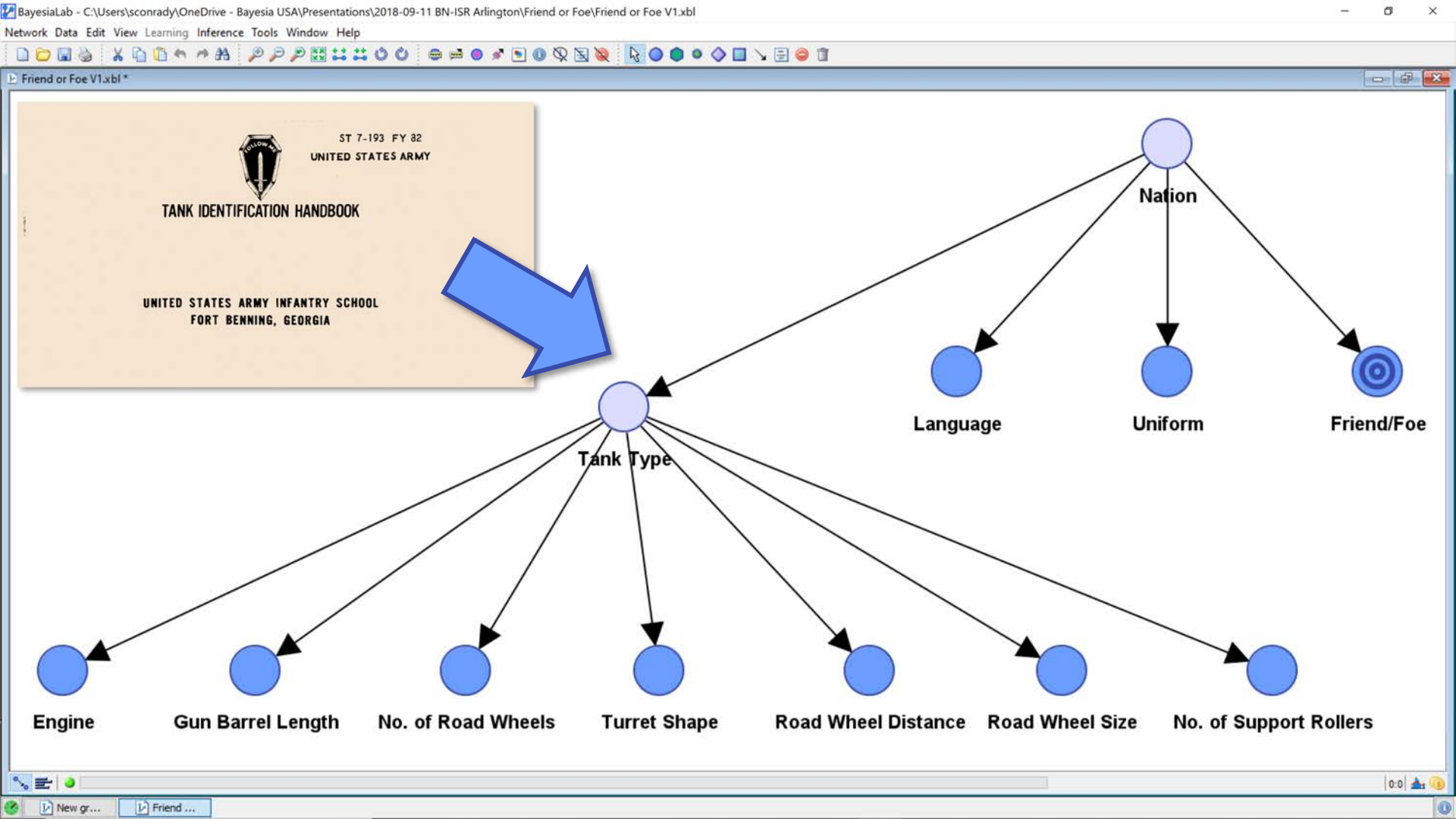
given





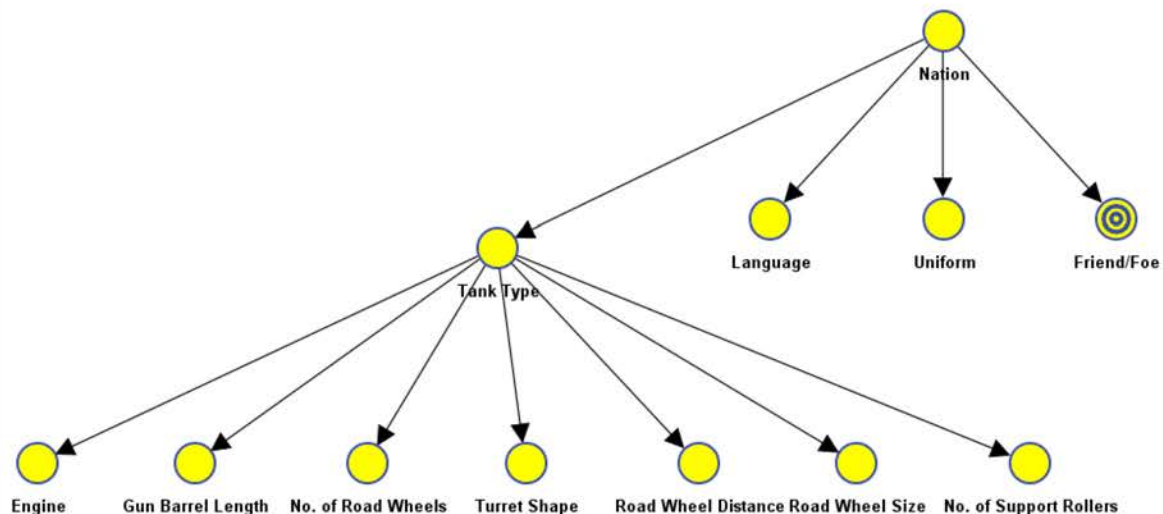
We need a  
knowledge base &  
inference engine!



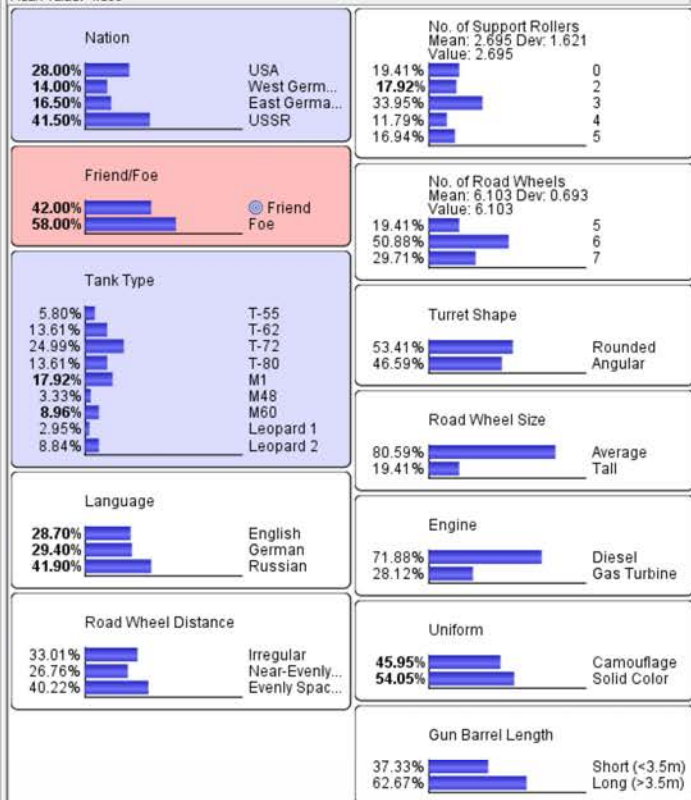




Friend or Foe V1.xbl \*

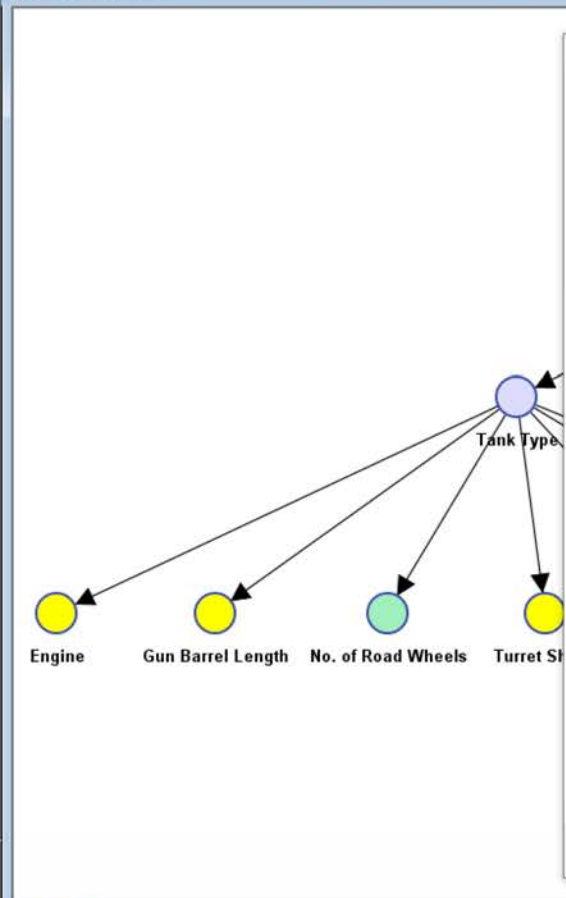


Joint Probability: 100.00%  
Log-Loss: 0  
Total Value: 8.798  
Mean Value: 4.399





Friend or foe V1.xbl



### Evidence Analysis (Friend or foe V1)

**Analysis Context**  
 No. of Road Wheels: 1 [5: 0.00%, 6: 100.00%, 7: 100.00%]  
 Uniform: Camouflage

**Overall consistency of the evidence: 0.24**

| Evidence Consistency Analysis |         |               |             |              |
|-------------------------------|---------|---------------|-------------|--------------|
| Node                          | Comment | State         | Consistency | Bayes Factor |
| Friend/foe                    |         | Friend        | 0.87        | 0.63         |
|                               |         | Foe           | -0.49       | -0.73        |
| Language                      |         | English       | 1.34        | 1.10         |
|                               |         | German        | -2.32       | -2.56        |
|                               |         | Russian       | -0.09       | -0.33        |
| Engine                        |         | Diesel        | -0.43       | -0.67        |
|                               |         | Gas Turbine   | 1.20        | 0.96         |
| Gun Barrel Length             |         | Short (<3.5m) | 0.40        | 0.15         |
|                               |         | Long (>3.5m)  | 0.14        | -0.10        |
| No. of Support Rollers        |         | 0             | ..90        | ..90         |
|                               |         | 2             | 1.45        | 1.21         |
|                               |         | 3             | 0.42        | 0.17         |
|                               |         | 4             | ..90        | ..90         |
|                               |         | 5             | 0.49        | 0.25         |
| Road Wheel Distance           |         | Uneven Gaps   | -0.67       | -0.91        |
|                               |         | Evenly Spaced | 0.54        | 0.30         |
| Road Wheel Size               |         | Average       | 0.55        | 0.31         |
|                               |         | Tall          | ..90        | ..90         |
| Turret Shape                  |         | Rounded       | -0.78       | -1.02        |
|                               |         | Angular       | 0.90        | 0.66         |

Close Save As... Print

Joint Probability: 38.81%  
 Log-Loss: 1.37  
 Total Value: 9.403  
 Mean Value: 4.701

**Friend/foe**  
 64.94% Friend  
 35.06% Foe

**Engine**  
 45.29% Diesel  
 54.71% Gas Turbine

**Language**  
 61.69% English  
 5.00% German  
 33.31% Russian

**Uniform**  
 100.00% Camouflage  
 0.00% Solid Color

**Gun Barrel Length**  
 41.56% Short (<3.5m)  
 58.44% Long (>3.5m)

**No. of Support Rollers**  
 Mean: 2.987 Dev: 1.105  
 Value: 2.987  
 0.00% 0  
 41.56% 2  
 38.31% 3  
 0.00% 4  
 20.13% 5

**No. of Road Wheels**  
 Mean: 6.416 Dev: 0.493  
 Value: 6.416  
 0.00% 5  
 58.44% 6  
 41.56% 7

**Turret Shape**  
 26.30% Rounded  
 73.70% Angular

**Road Wheel Distance**  
 17.53% Uneven Gaps  
 82.47% Evenly Spaced

**Road Wheel Size**  
 100.00% Average  
 0.00% Tall

# Knowledge Base & Inference Engine







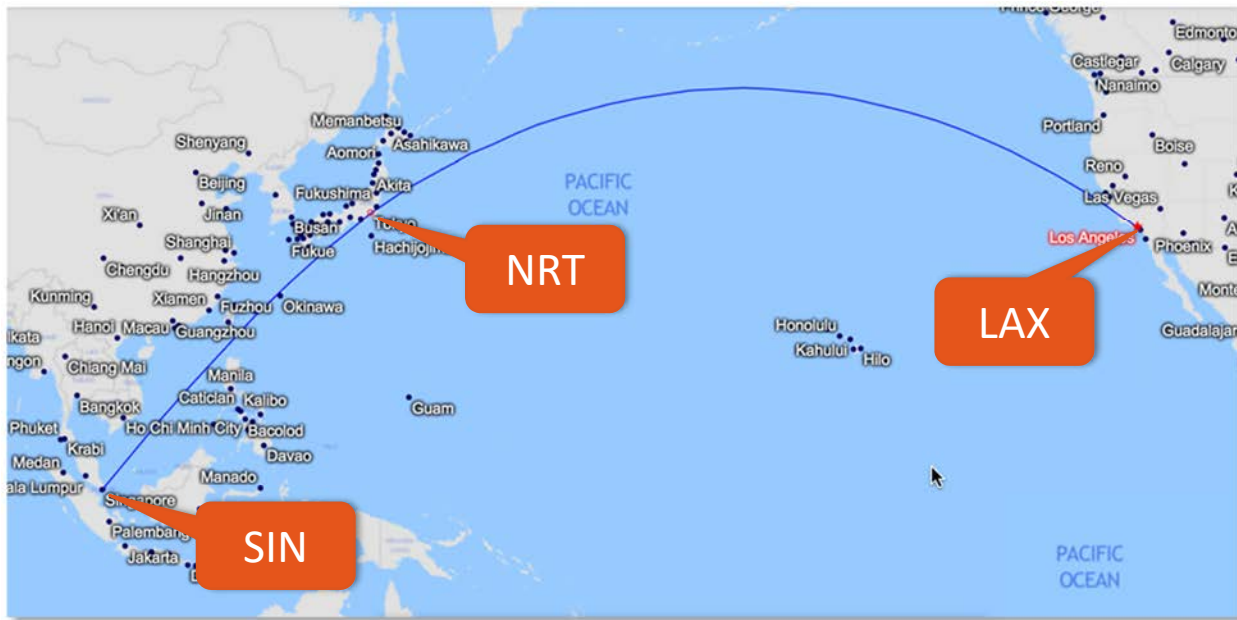
See Chapter 4

# Where is my bag?

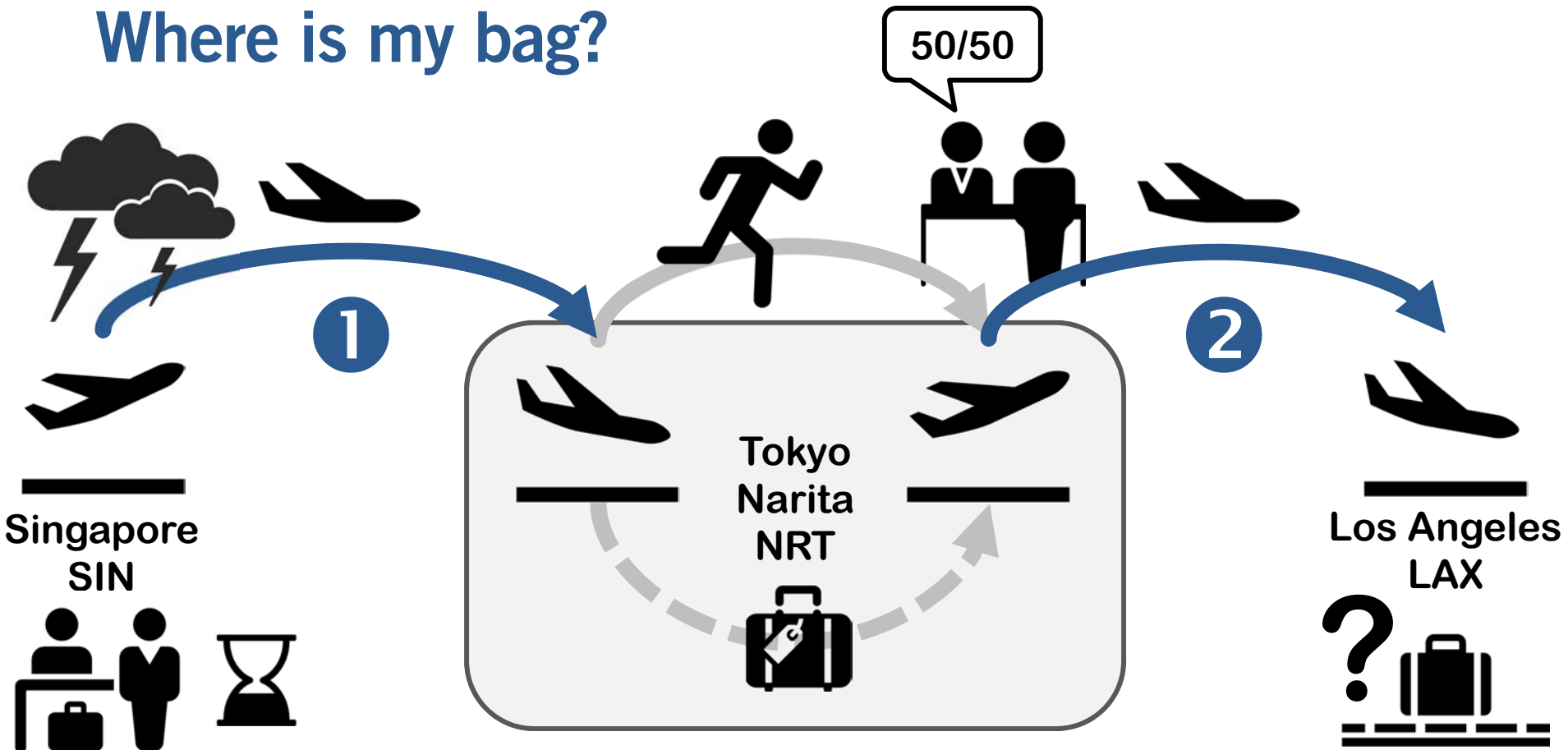
Knowledge Modeling & Reasoning Under Uncertainty

# Example: Where is my bag?

Travel Route: Singapore (SIN) → Tokyo/Narita (NRT) → Los Angeles (LAX)



# Where is my bag?

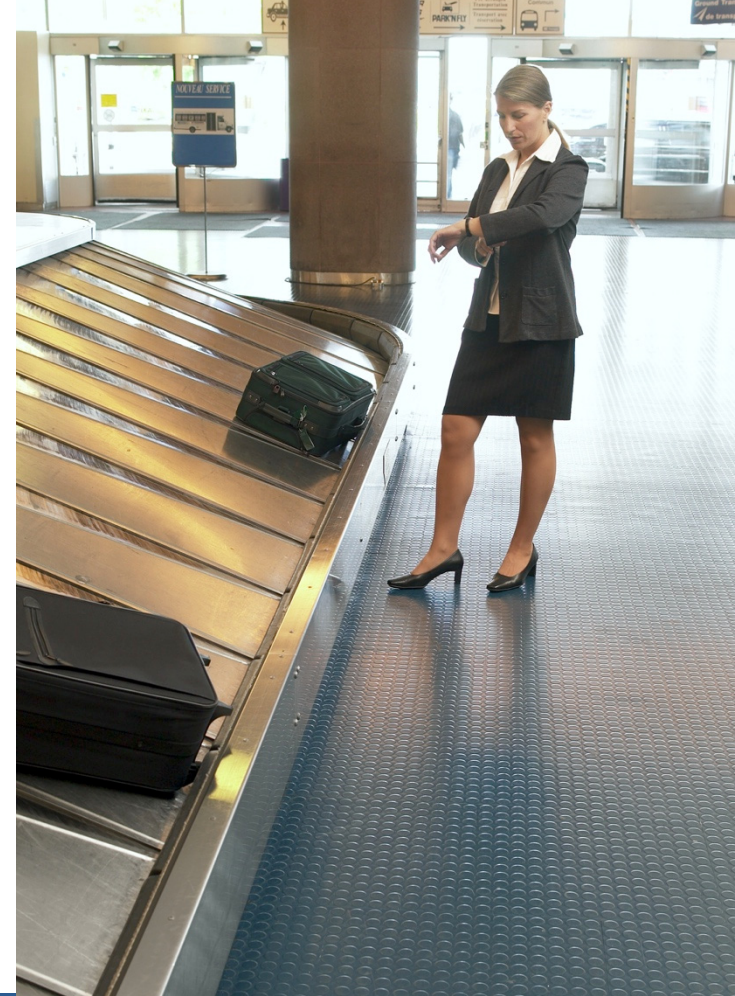




# Where is my bag?

## Scenario 1

- Luggage delivery starts onto the carousel.
- **After 5 minutes**, I still do not see my bag.
- What is the probability that I will still get my bag?





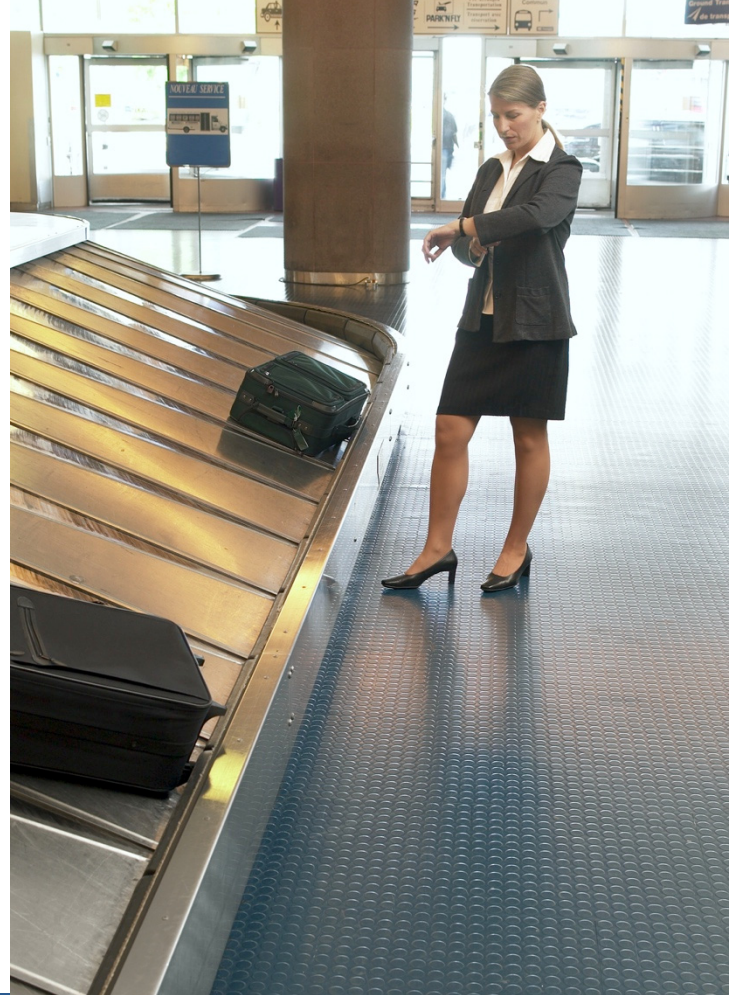


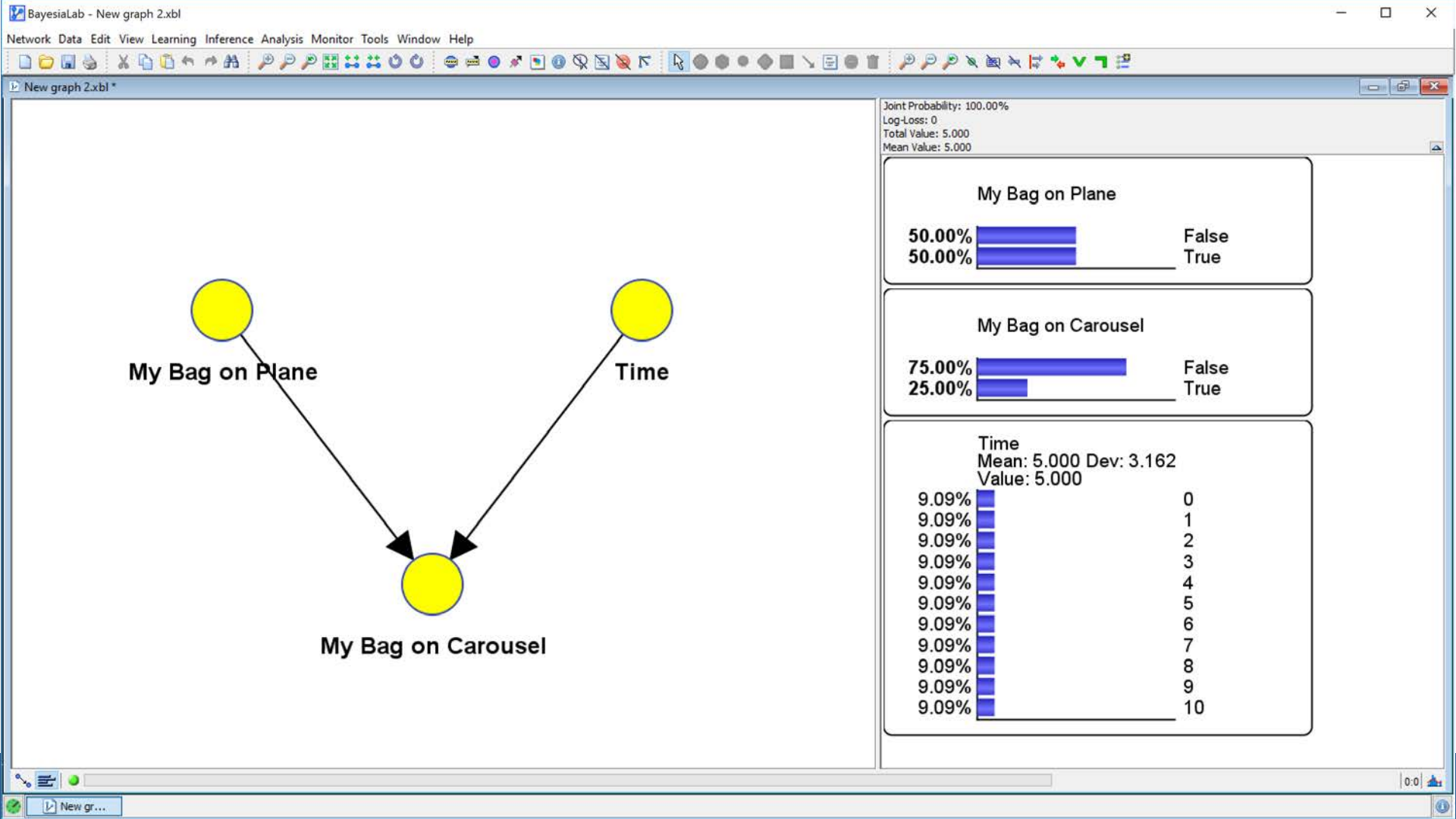
IS MY BAG  
IN THERE?

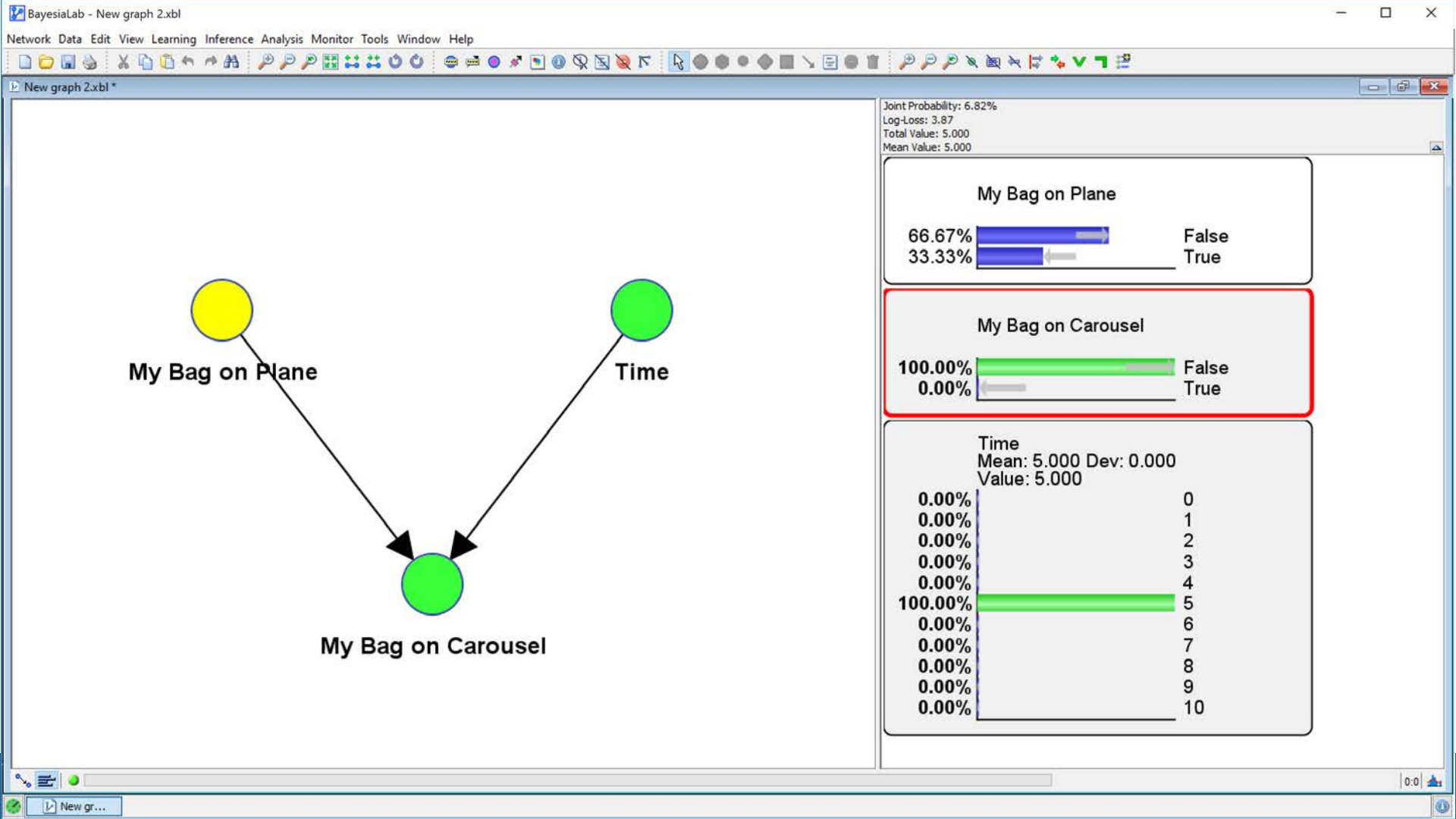
# Where is my bag?

## Proposed Workflow

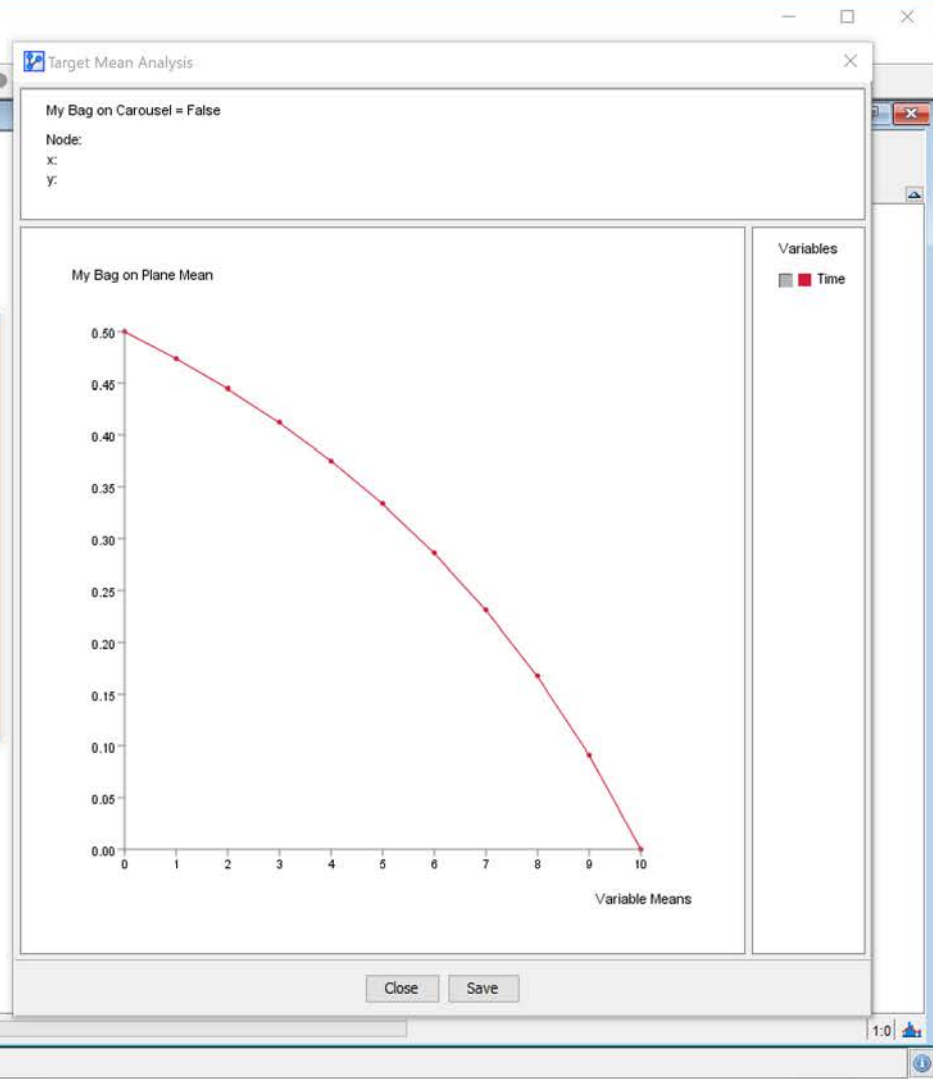
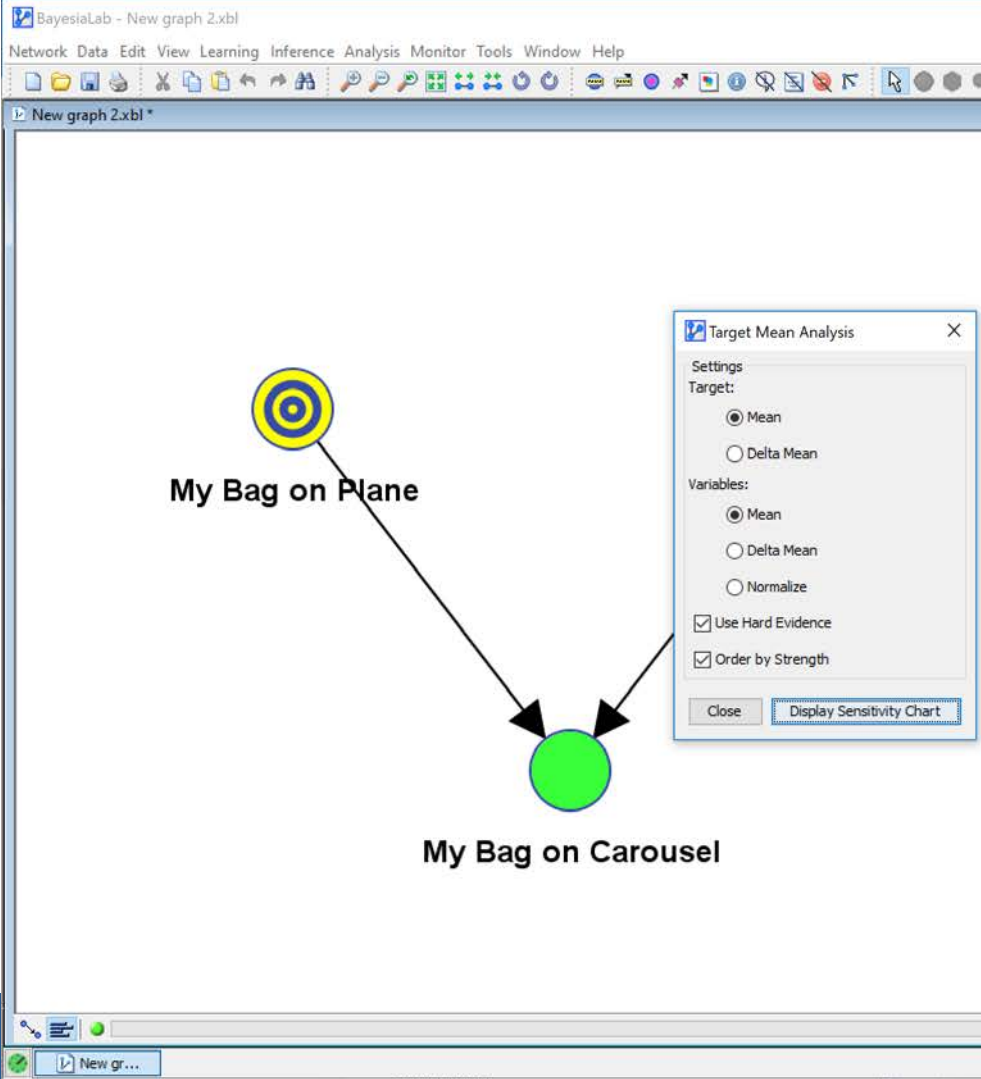
- Encode the available — albeit very limited — knowledge into a Bayesian network.
- Use BayesiaLab to perform probabilistic inference given our observations.







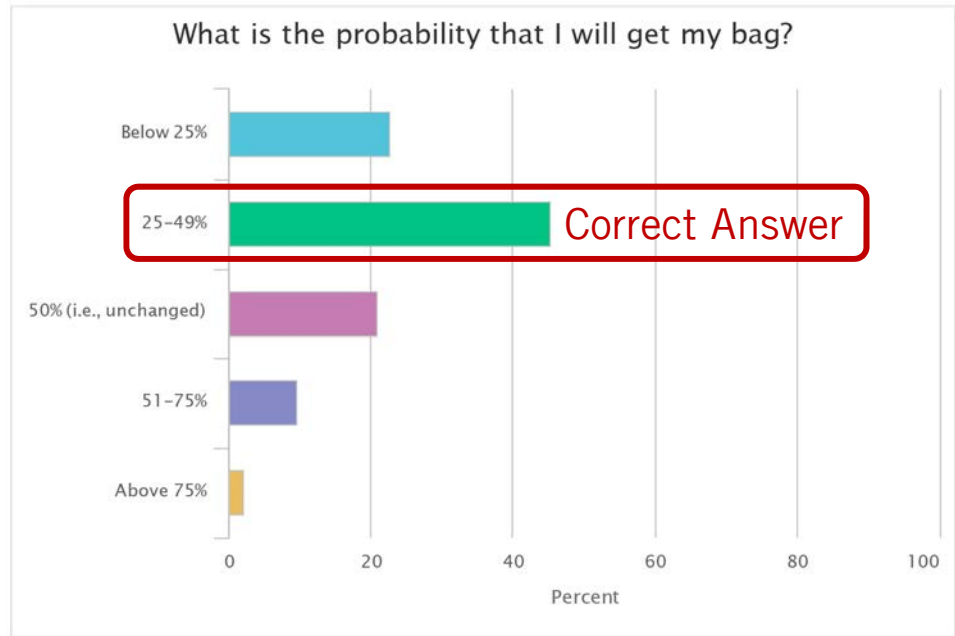




# Where is my bag?

## Results from Webinar Poll

- Only 45% of the participants arrived at the correct answer.



# Where is my bag?

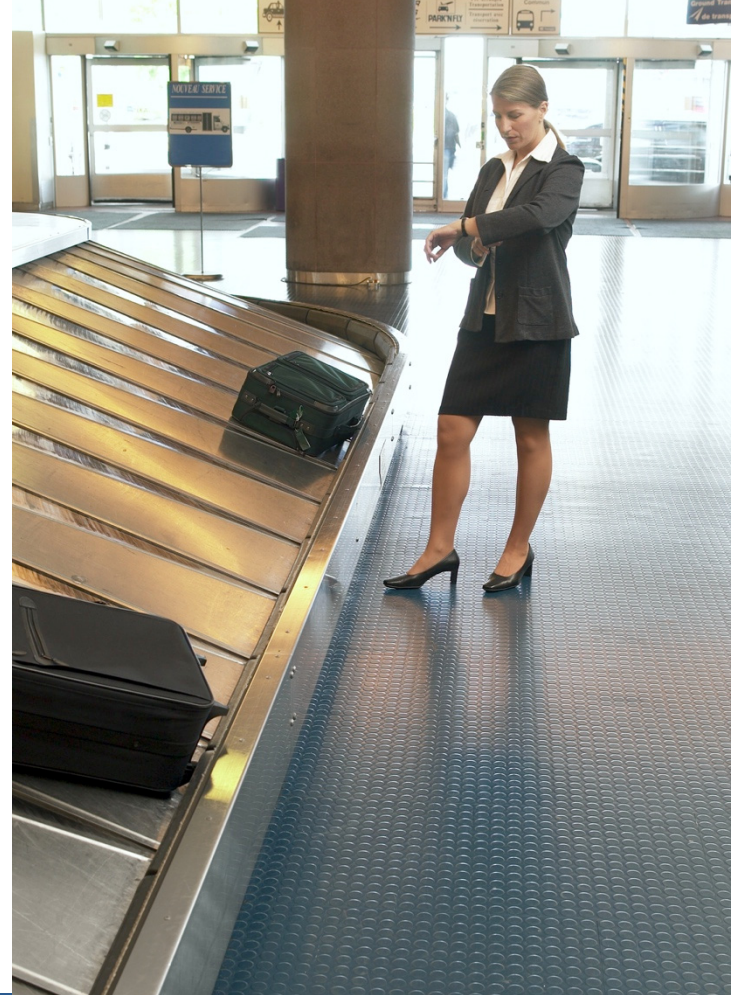
## More important questions:

- Will the patient ultimately respond to the current treatment?
- Should we continue a search and rescue effort?
- Should we still follow the original business strategy, i.e. “hold the course”?

# Where is my bag?

## Key Points

- Encoding of knowledge
- Reasoning under uncertainty
- Reasoning
  - from cause to effect (simulation)
  - from effect to cause (diagnosis)
- Inter-causal reasoning

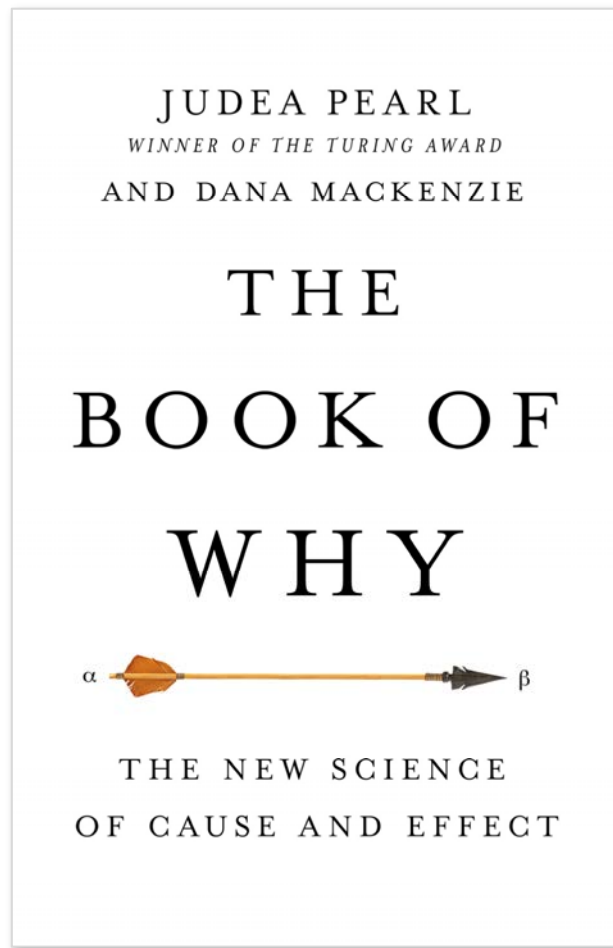




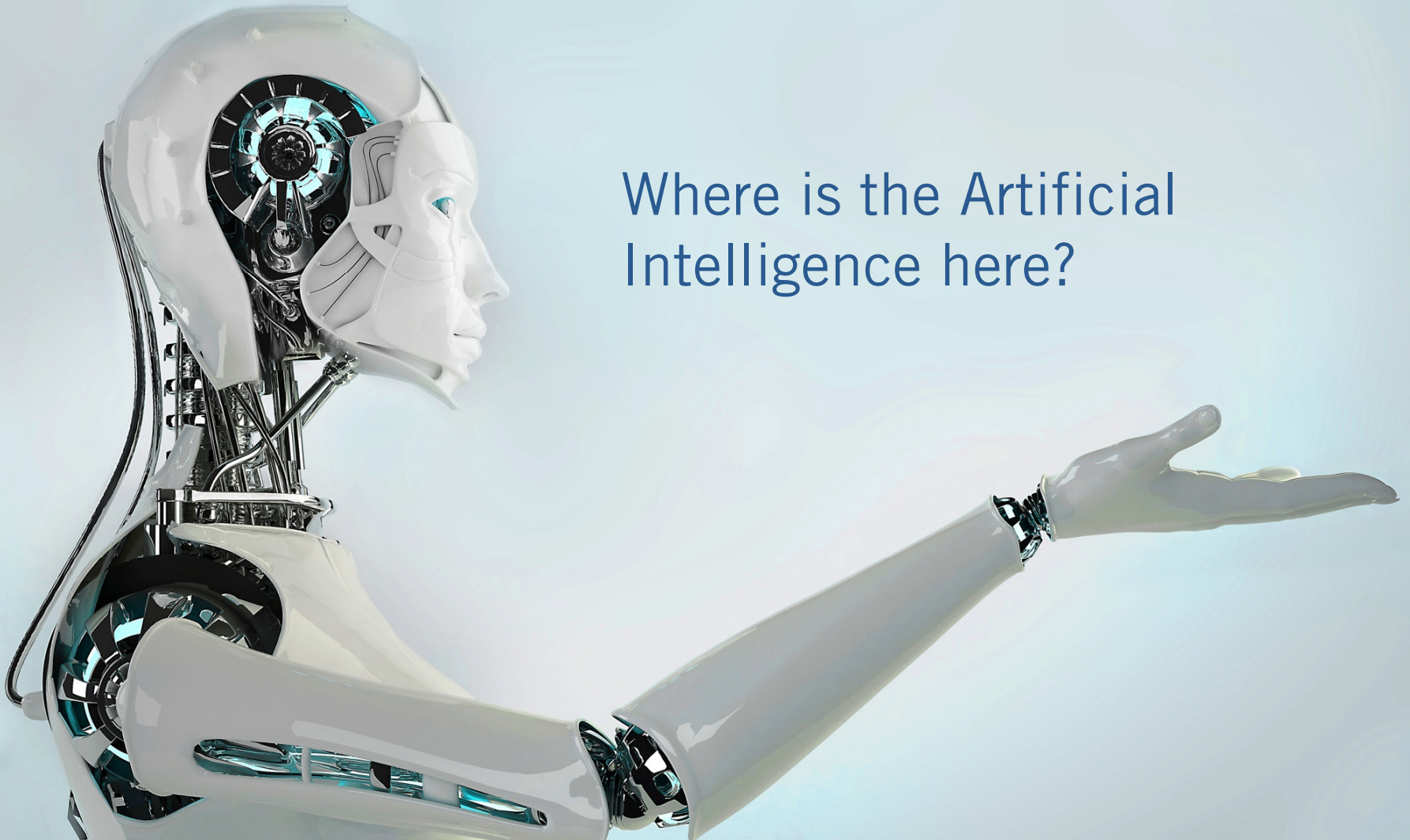
# Where is my bag?

Learn more about this example...

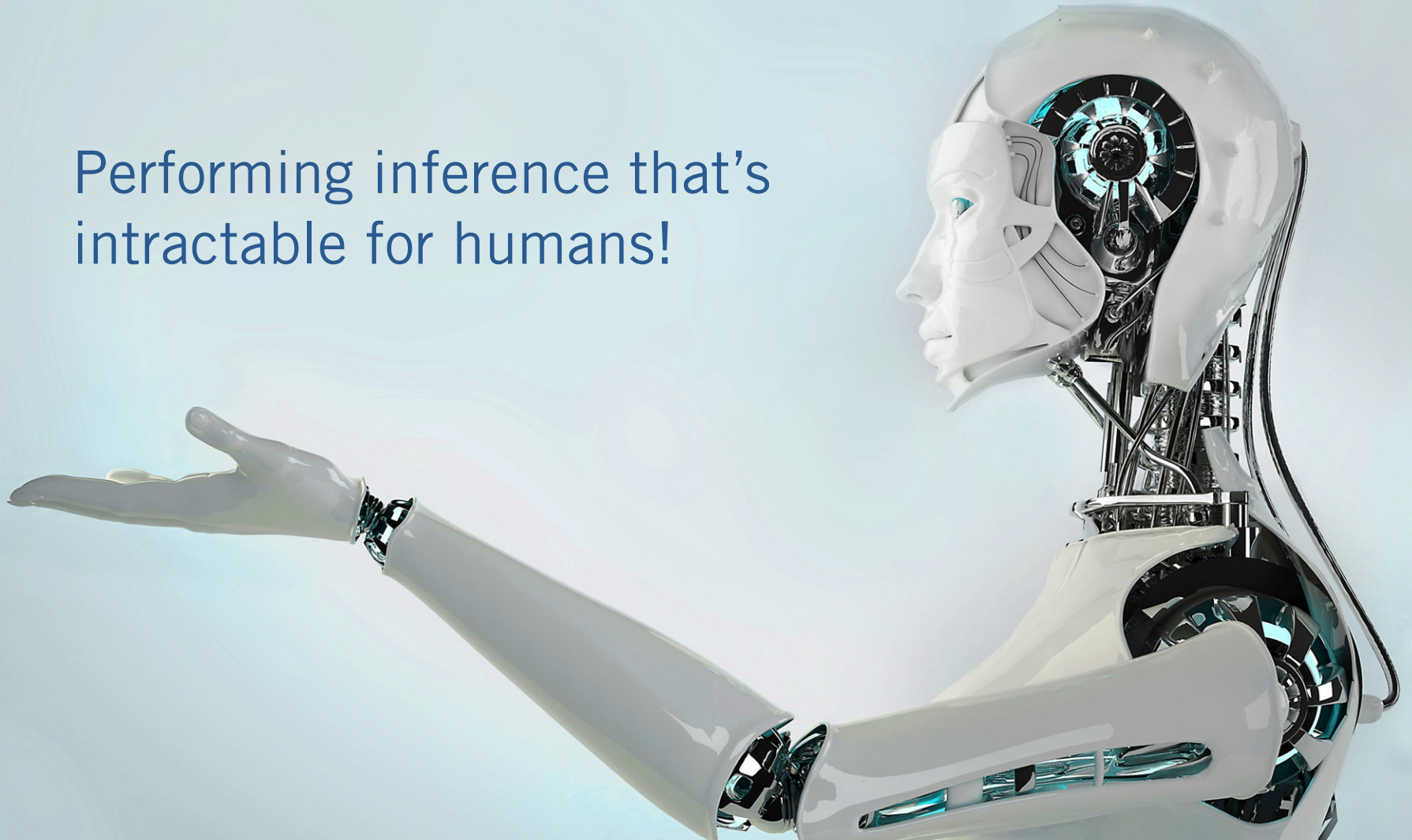
- pp. 118-119



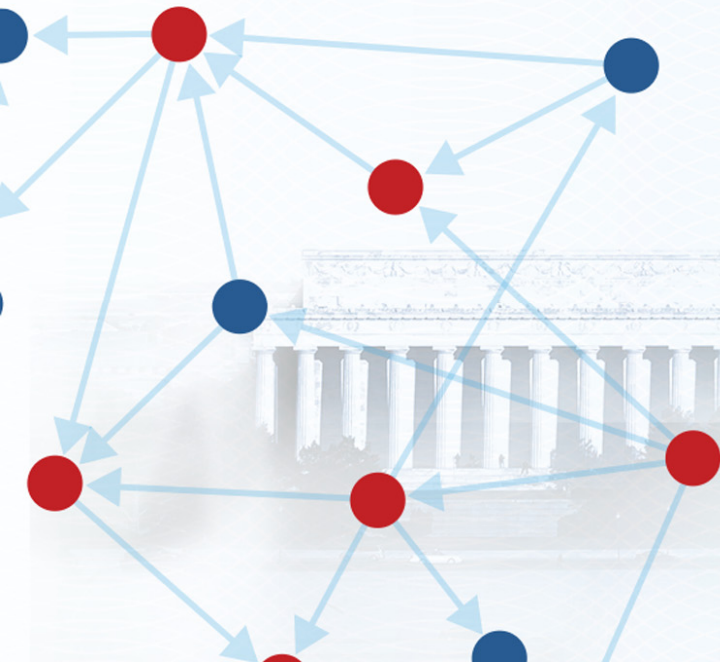
Where is the Artificial  
Intelligence here?



Performing inference that's  
intractable for humans!







## Coffee Break





# The Monty Hall Puzzle



# Mission

## Hypothetical Mission Assignment

- You are tasked with to conduct a raid to destroy a secret aircraft prototype on enemy territory.
- This aircraft has been traced to a remote military air base and is presumed to be located in one of three separate underground hangars inside a mountain on this facility.
- As a result, you have a one-in-three chance of hitting your target with your first strike.



Data SIO, NOAA, U.S. Navy, NGA, GEBCO  
Image Landsat / Copernicus  
Image IBCAO  
Image U.S. Geological Survey

Google Earth



Underground Hangars

1

2

3





# Mission

## Expected Conditions

- Each hangar entrance is guarded by infantry soldiers.
- Furthermore, the base has two infantry fighting vehicles, which can be dispatched to the hangars within minutes.



A man in a suit and glasses, a woman in a military uniform and glasses, and another man in a military uniform are gathered around a laptop in a dimly lit control room. The man in the suit is pointing at the screen. A speech bubble above the man in the suit contains the text "Let's go for #2". The background shows rows of server racks with glowing lights.

Let's go for #2



Underground Hangars

1

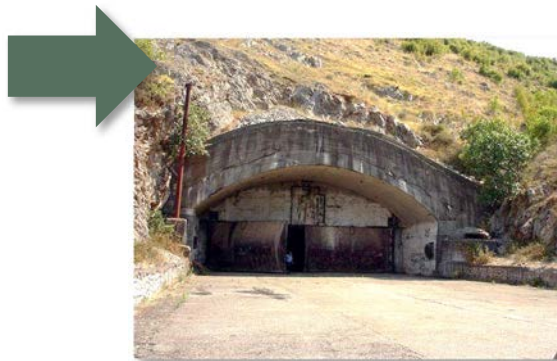
2

3

# Mission

## Mission Progress

- Your raid — and your approach to hangar #2 — is detected, and two infantry fighting vehicles are immediately positioned as a defense in front of hangars #1 and #2.
- Hangar #3 remains unprotected, thus revealing that this hangar does not contain the target.
- Since the target can only be in hangar #1 or #2, one of the hangars is the true target while the other one is merely a decoy.



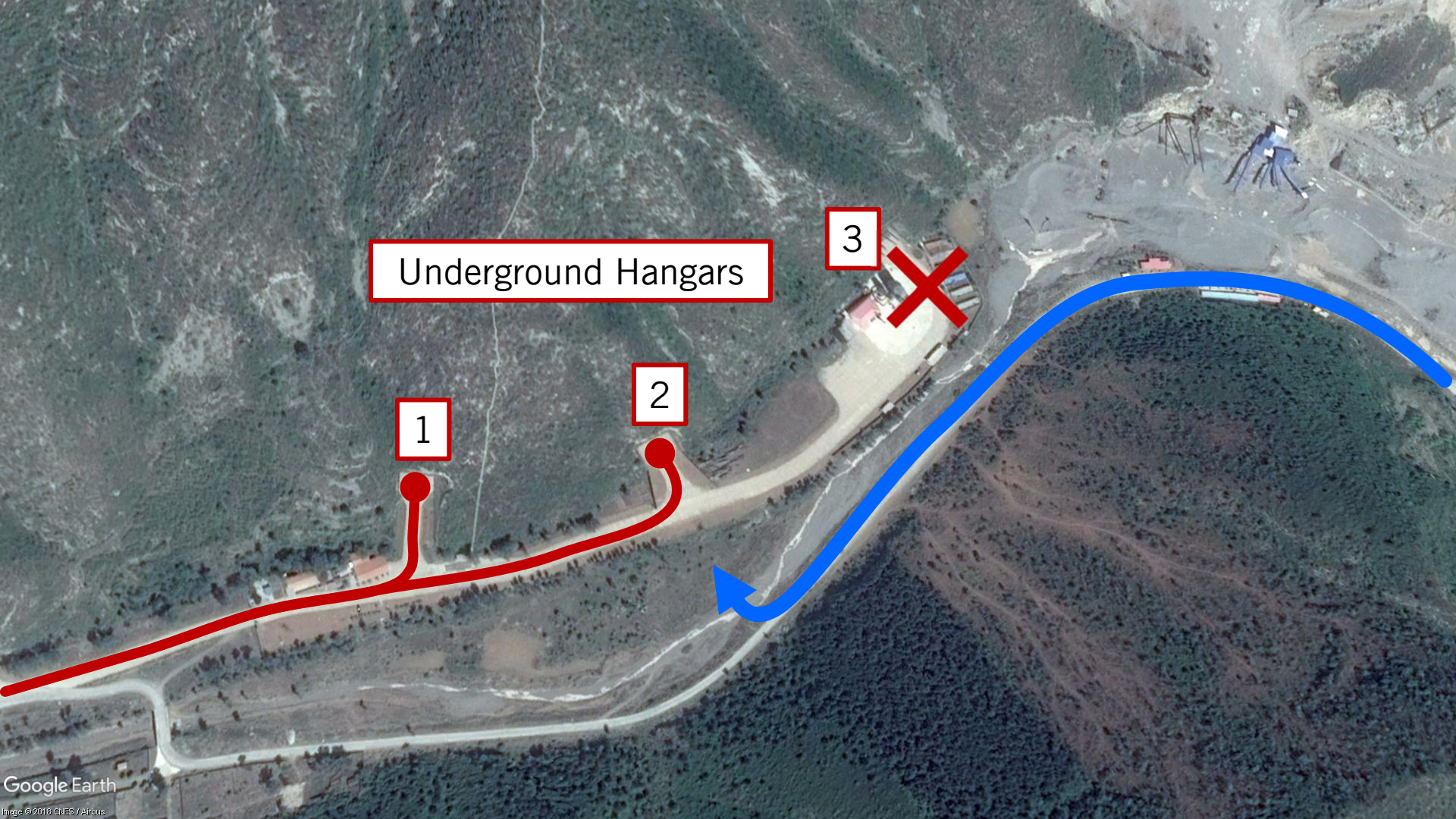


Underground Hangars

1

2

3



# Choose Your Battle Wisely!

## Mission Status

- You have enough time and firepower to overpower the enemy forces and carry out your mission at either one of the two hangars, but not at both.
- So, you have only one shot at completing your task!

## Decision Point

- Do you proceed with your original objective of attacking hangar #2?
- Or, do you change your original plan to go after hangar #1?

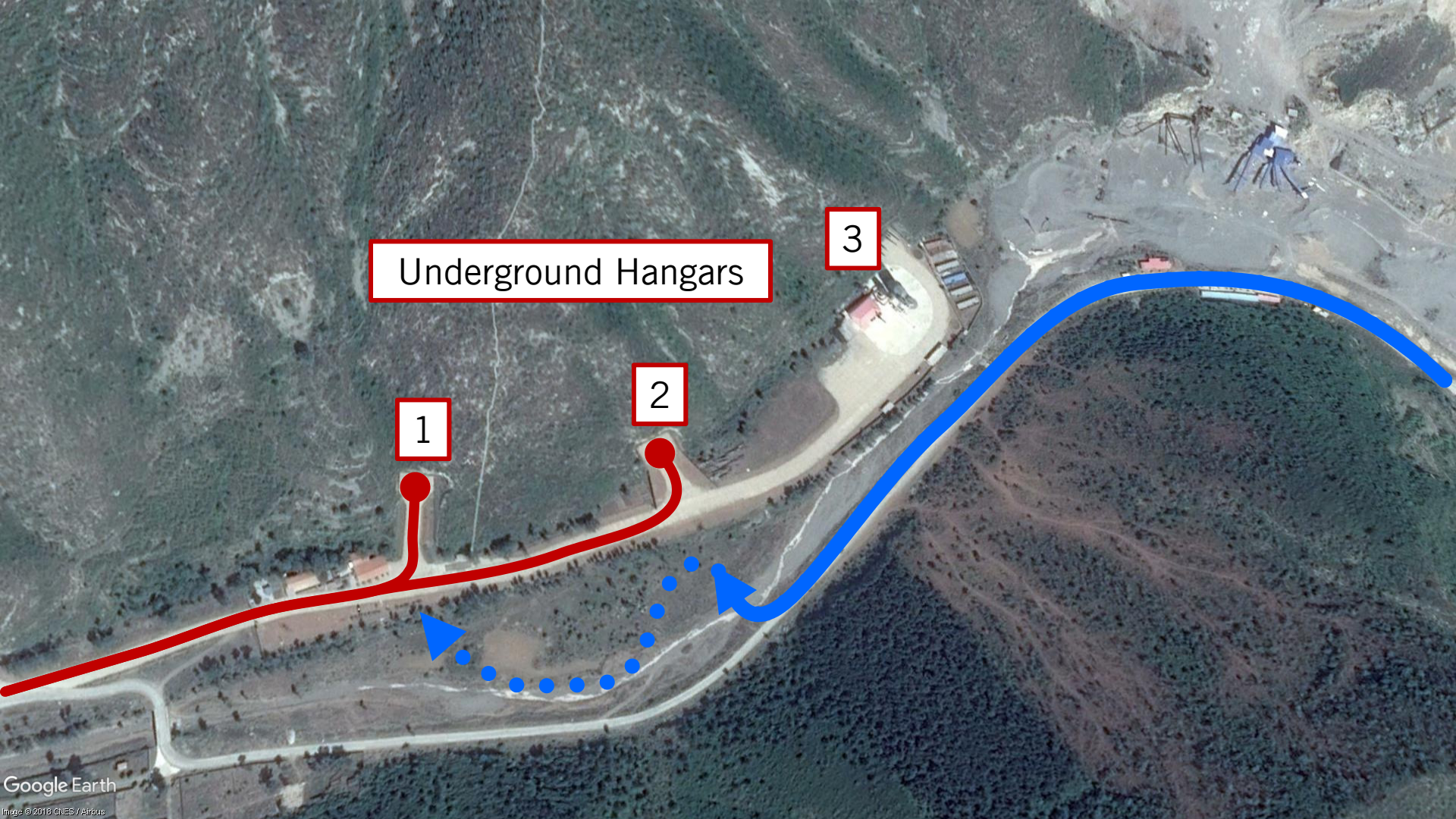


Underground Hangars

1

2

3



# Choose Your Battle Wisely!

Let's take a vote...

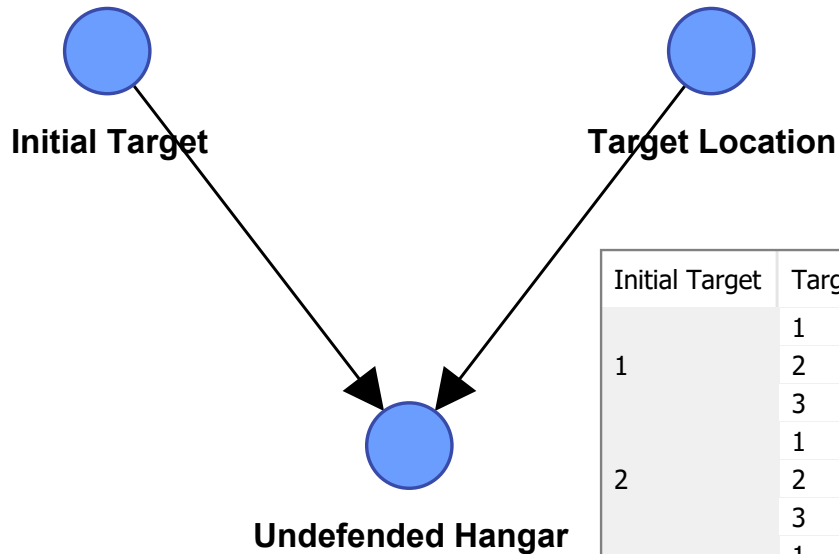




# Encoding our Intelligence

| 1      | 2      | 3      |
|--------|--------|--------|
| 33.333 | 33.333 | 33.333 |

| 1      | 2      | 3      |
|--------|--------|--------|
| 33.333 | 33.333 | 33.333 |

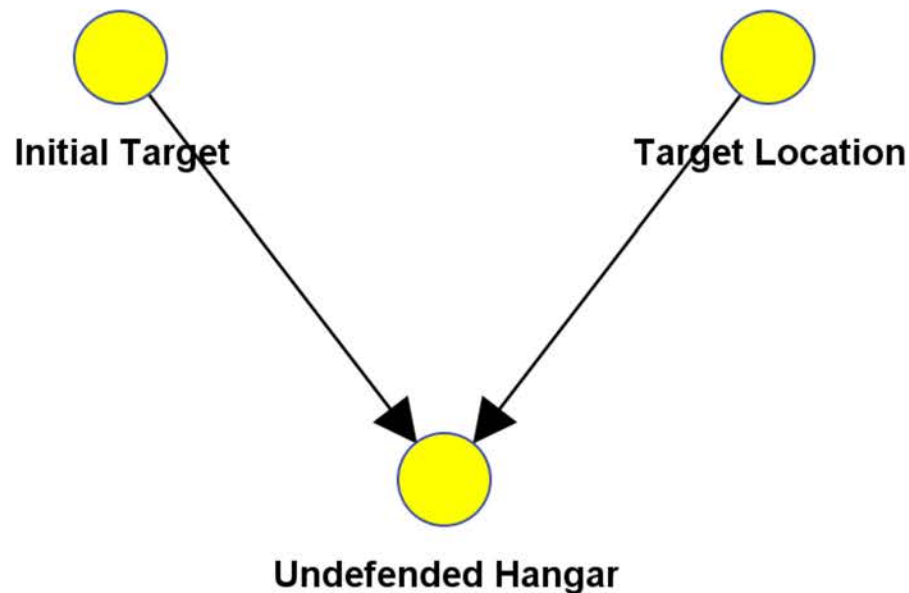


Our beliefs about the enemy's behavior.

| Initial Target | Target Location | 1       | 2       | 3       |
|----------------|-----------------|---------|---------|---------|
| 1              | 1               | 0.000   | 50.000  | 50.000  |
|                | 2               | 0.000   | 0.000   | 100.000 |
|                | 3               | 0.000   | 100.000 | 0.000   |
| 2              | 1               | 0.000   | 0.000   | 100.000 |
|                | 2               | 50.000  | 0.000   | 50.000  |
|                | 3               | 100.000 | 0.000   | 0.000   |
| 3              | 1               | 0.000   | 100.000 | 0.000   |
|                | 2               | 100.000 | 0.000   | 0.000   |
|                | 3               | 50.000  | 50.000  | 0.000   |



Monty Hall.xbl \*



Joint Probability: 100.00%  
Log-Loss: 0  
Total Value: 6.000  
Mean Value: 2.000

**Initial Target**

Mean: 2.000 Dev: 0.816

Value: 2.000



**Undefended Hangar**

Mean: 2.000 Dev: 0.816

Value: 2.000



**Target Location**

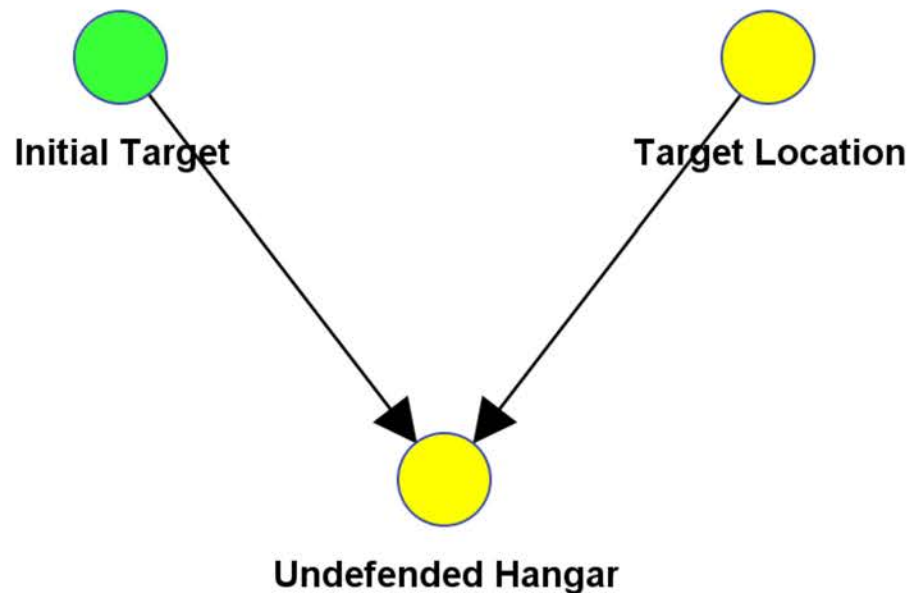
Mean: 2.000 Dev: 0.816

Value: 2.000





Monty Hall.xbl \*



Joint Probability: 33.33%  
Log-Loss: 1.58  
Total Value: 6.000  
Mean Value: 2.000

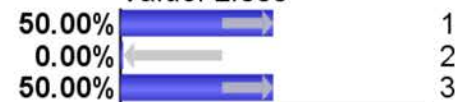
Initial Target

Mean: 2.000 Dev: 0.000  
Value: 2.000 (-0.000)



Undefended Hangar

Mean: 2.000 Dev: 1.000  
Value: 2.000



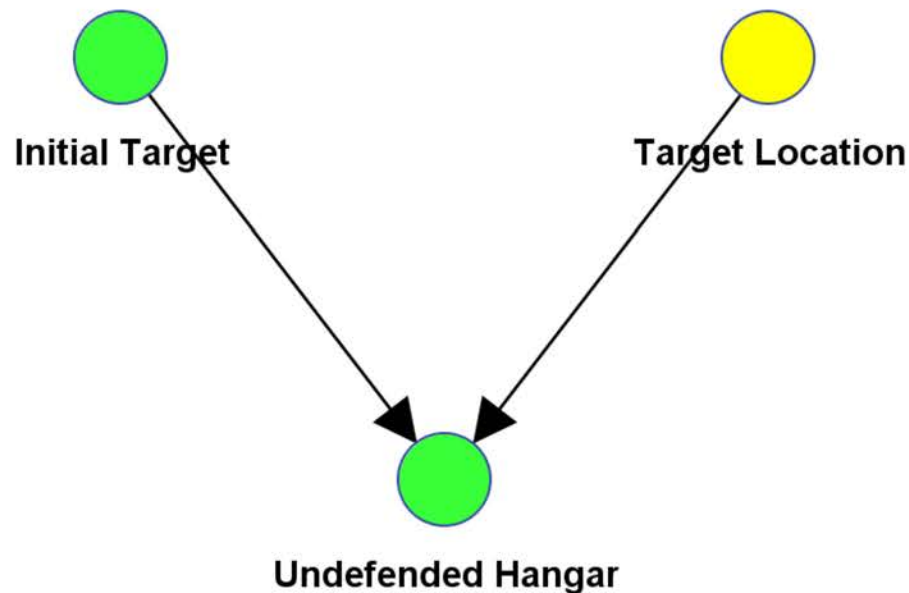
Target Location

Mean: 2.000 Dev: 0.816  
Value: 2.000 (-0.000)





Monty Hall.xbl \*



Joint Probability: 16.67%  
Log-Loss: 2.58  
Total Value: 6.333  
Mean Value: 2.111

Initial Target

Mean: 2.000 Dev: 0.000

Value: 2.000



Undefended Hangar

Mean: 3.000 Dev: 0.000

Value: 3.000 (+1.000)



Target Location

Mean: 1.333 Dev: 0.471

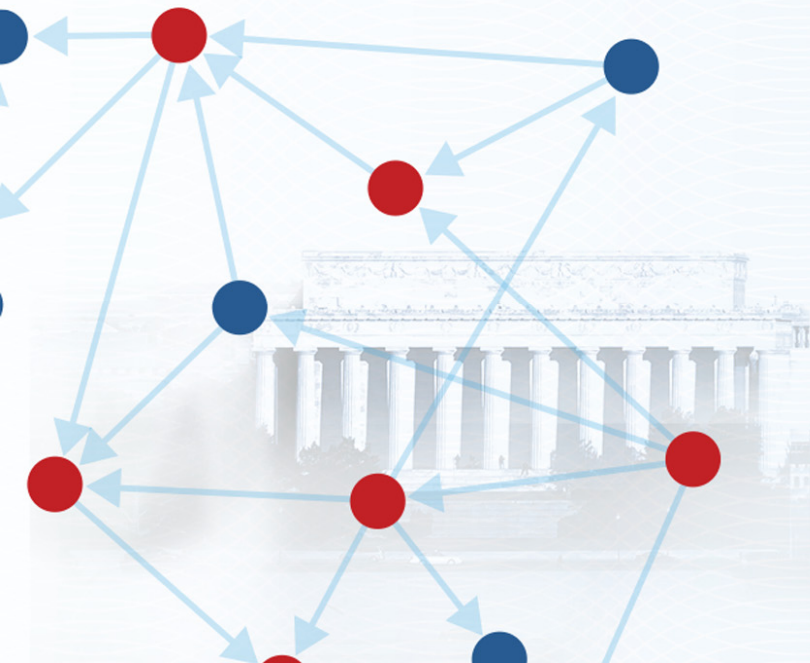
Value: 1.333 (-0.667)



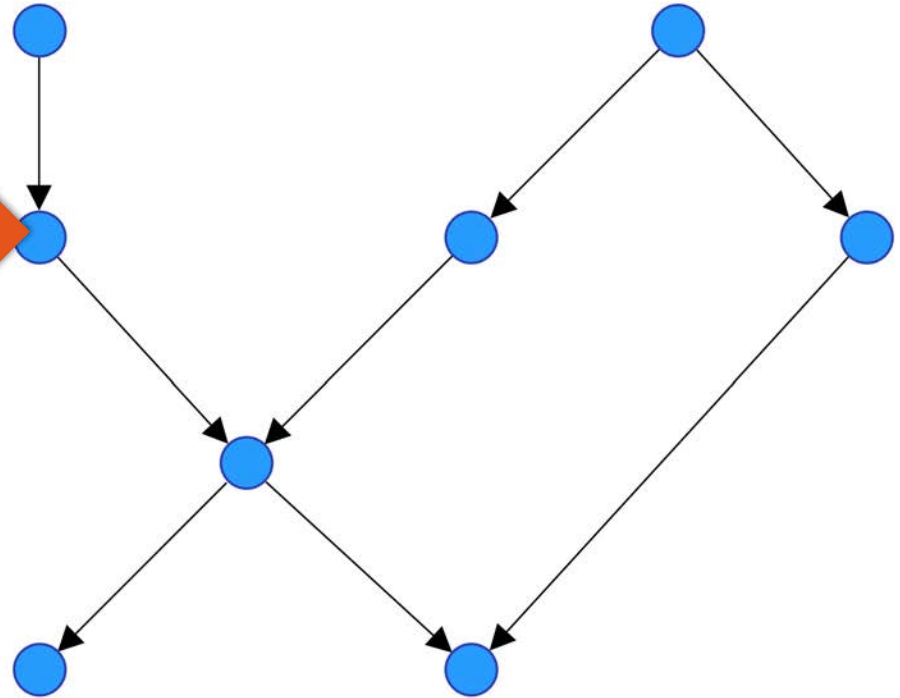




# The Bayesia Expert Knowledge Elicitation Environment



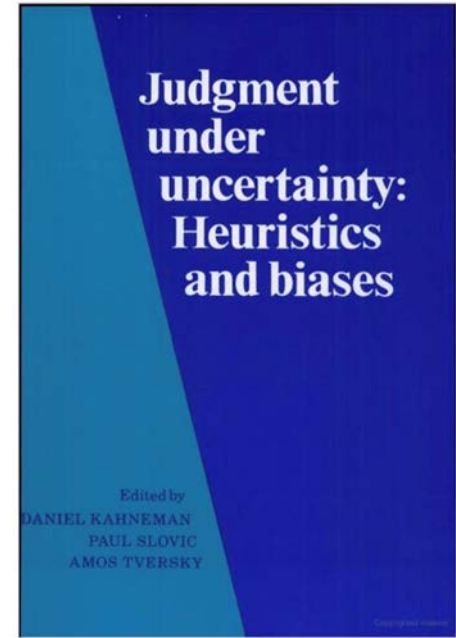
# Knowledge Elicitation?



# Individual Biases

## Examples

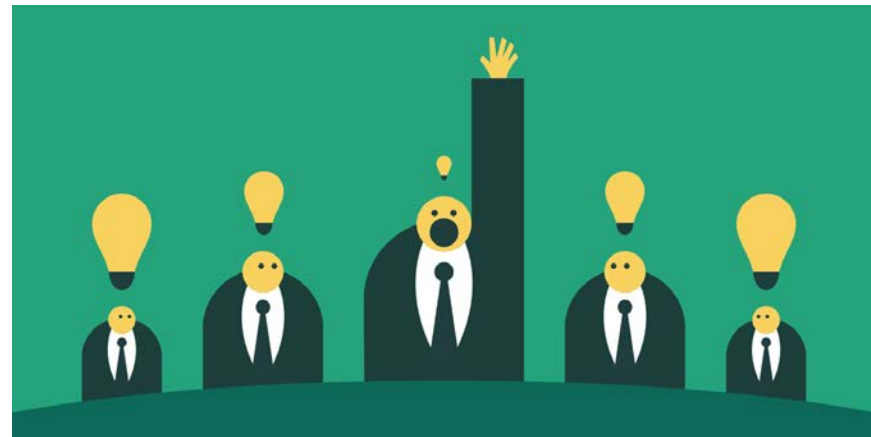
- Overconfidence
- Confirmation bias
- Framing effect
- Escalation of commitment
- Availability bias
- Illusion of control
- Anchoring bias



# Group Biases

## Examples

- Groupthink (“toeing the line”)
- Social loafing (“hiding in the crowd”)
- Group polarization (“taken to the extreme”)
- Escalation of commitment (“throwing good money after bad”, “sunk costs fallacy”)







# The Delphi Method



A Consultation of the Delphic Oracle:  
Themis on the Tripod with King Aegeus, c. 440 BC

# The Delphi Method

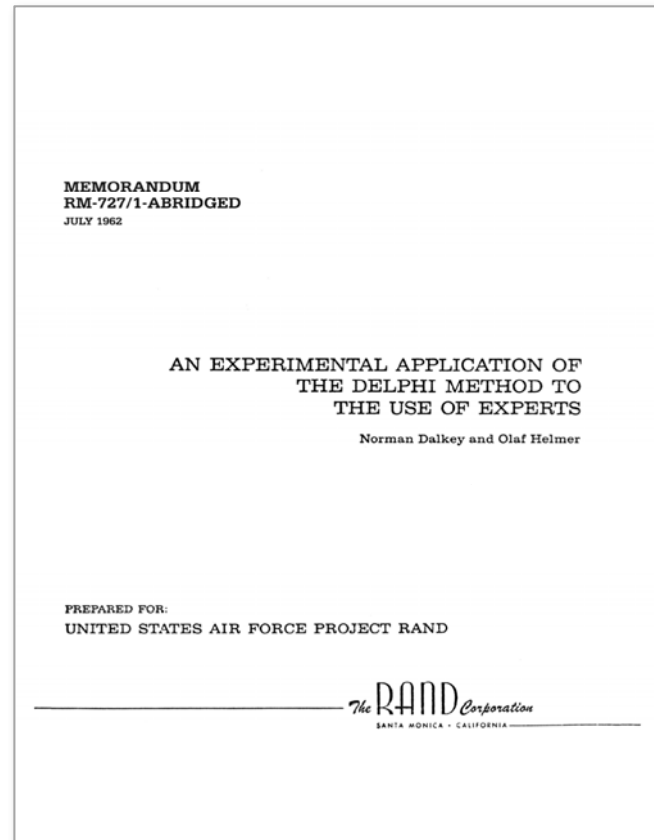
## Interacting Groups

- Take the positive, e.g.
  - Knowledge from a variety of sources
  - Creative synthesis
- Prevent the negative, e.g.
  - Groupthink (“toeing the line”)
  - Social loafing (“hiding in the crowd”)
  - Group polarization (“taken to the extreme”)

# The Delphi Method

## Origins

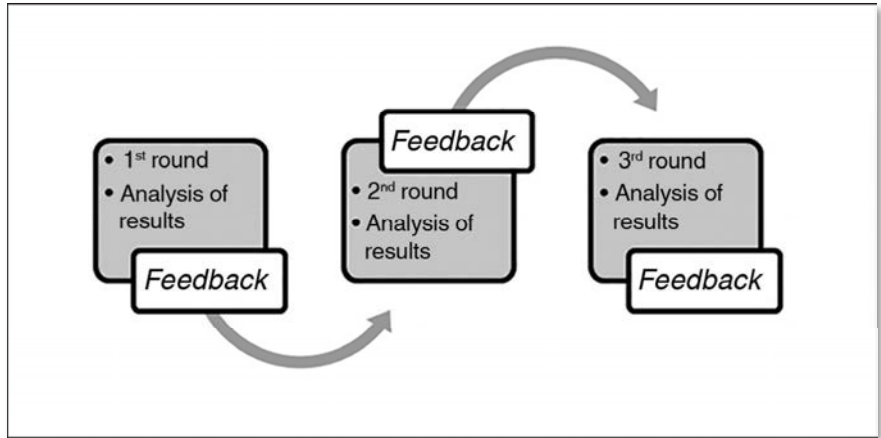
- The original Delphi method was developed in the 1940s and 50s by Norman Dalkey of the RAND Corporation.
- The Delphi method was devised in order to obtain the most **reliable opinion consensus of a group of experts** by subjecting them to a series of questionnaires in depth interspersed with controlled opinion feedback.



# The Delphi Method

## The Classical Delphi

- Interviews via questionnaires
- Anonymity of participants
- Iteration
- Controlled feedback
- Statistical aggregation





# First Experimental Application

"to solicit expert opinion to the selection, from the point of view of a Soviet strategic planner, of an optimal U.S. industrial target system..."



# Delphi Method Assessment

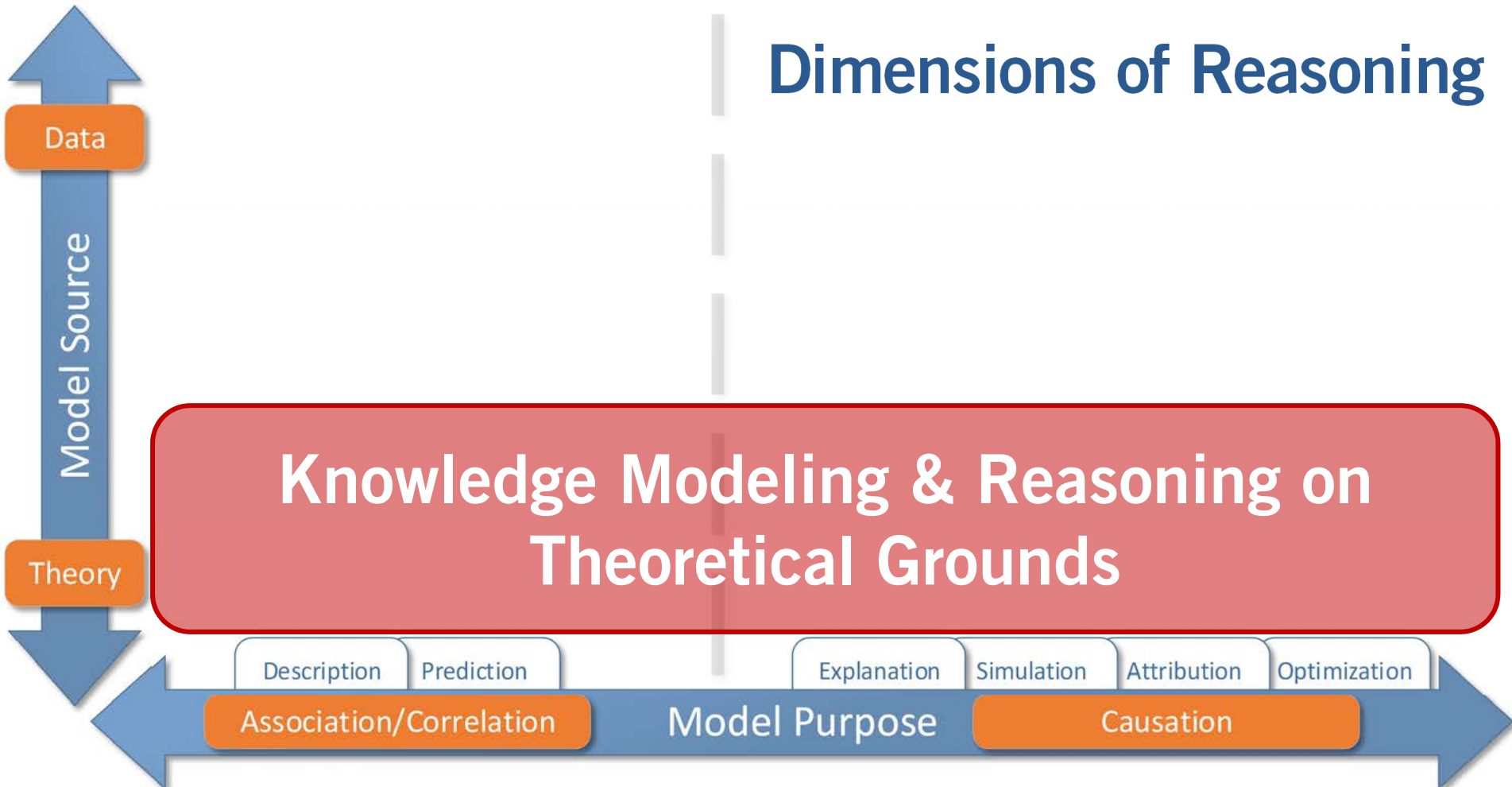
“In view of the absence of a proper theoretical foundation and the consequent inevitability of having, to some extent, to rely on intuitive expertise—a situation which is still further compounded by its multidisciplinary characteristics—we are faced with two options: **we can either throw up our hands in despair** and wait until we have an adequate theory enabling us to deal with socioeconomic and political problems as confidently as we do with problems in physics and chemistry, **or we can make the most of an admittedly unsatisfactory situation and try to obtain the relevant intuitive insights of experts** and then use their judgments as systematically as possible.”

ANALYSIS OF THE FUTURE: THE DELPHI METHOD

Olaf Helmer

March 1967

# Dimensions of Reasoning









# Conceptual Overview

| Source | Objective                       | Methodology       | Technology        |
|--------|---------------------------------|-------------------|-------------------|
| Data   | Knowledge Discovery & Inference | Bayesian Networks | <b>BAYESIALAB</b> |
| Theory | Knowledge Elicitation           | Delphi Method     | <b>BEKEE</b>      |

# Policy Development?

## Proposed Policy Development Approach

- Domain Knowledge Encoding



Plasmodium spp.



Rapid Diagnostic Test



- Probability Elicitation



| Plasmodium spp | False  | True   |
|----------------|--------|--------|
| False          | 80.000 | 20.000 |
| True           | 20.000 | 80.000 |

- Cost/Utility Assessment



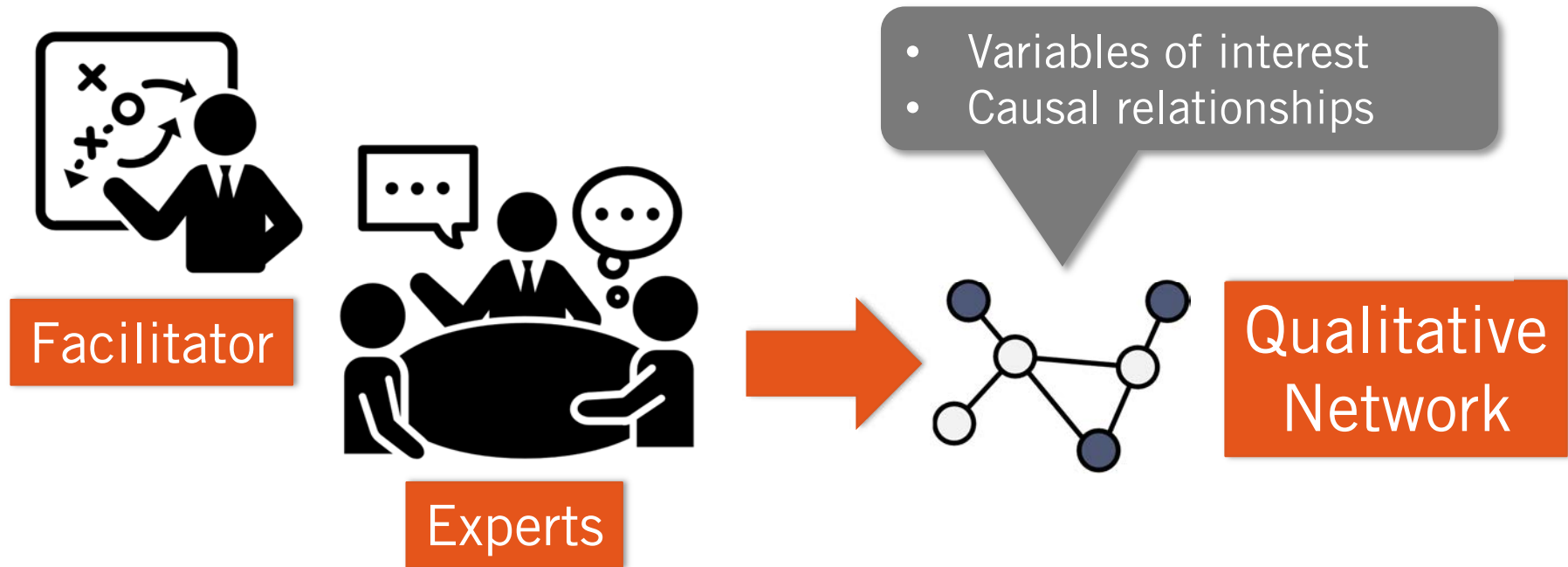
RDT Cost

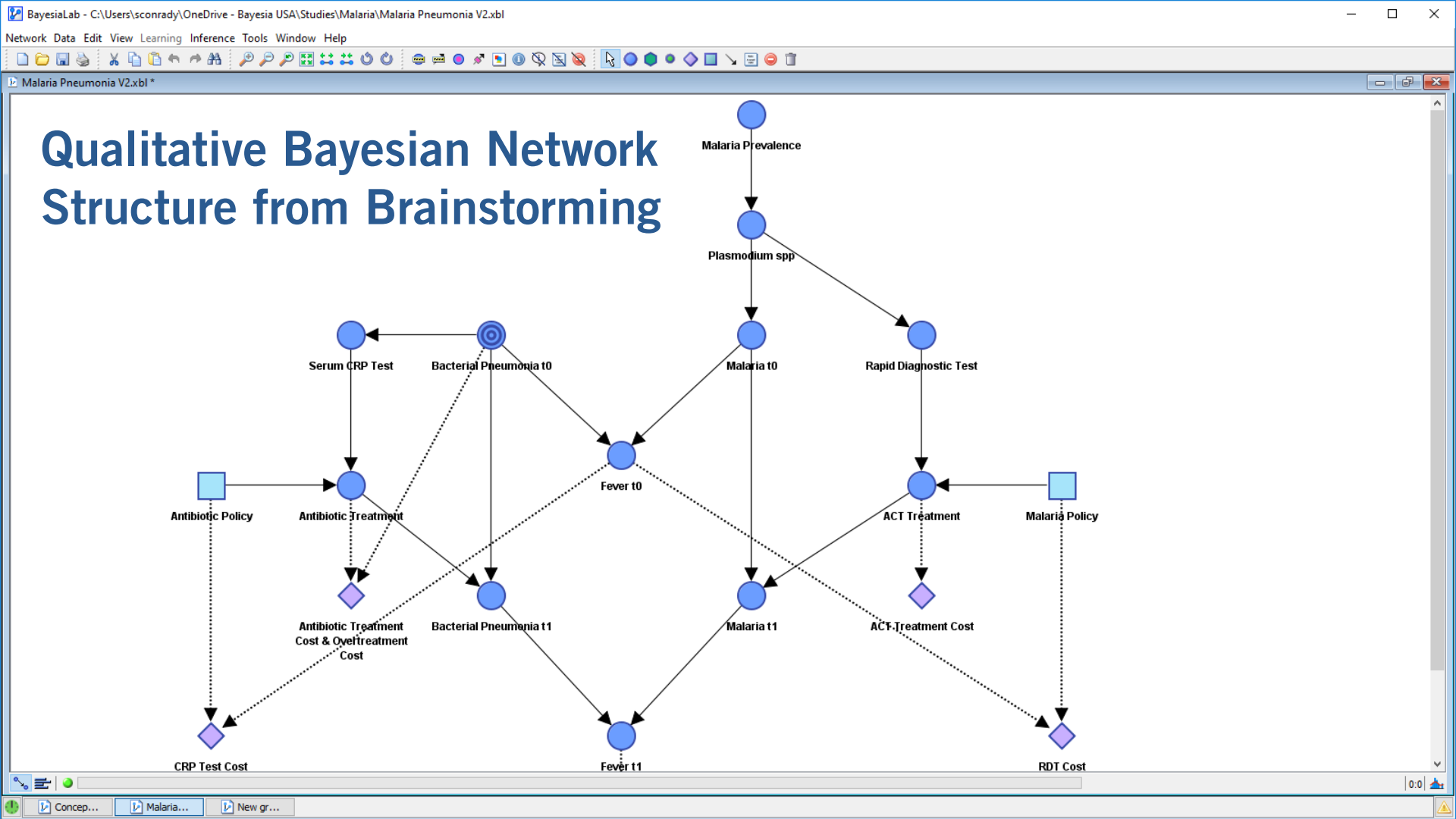
- Optimization



Malaria Policy

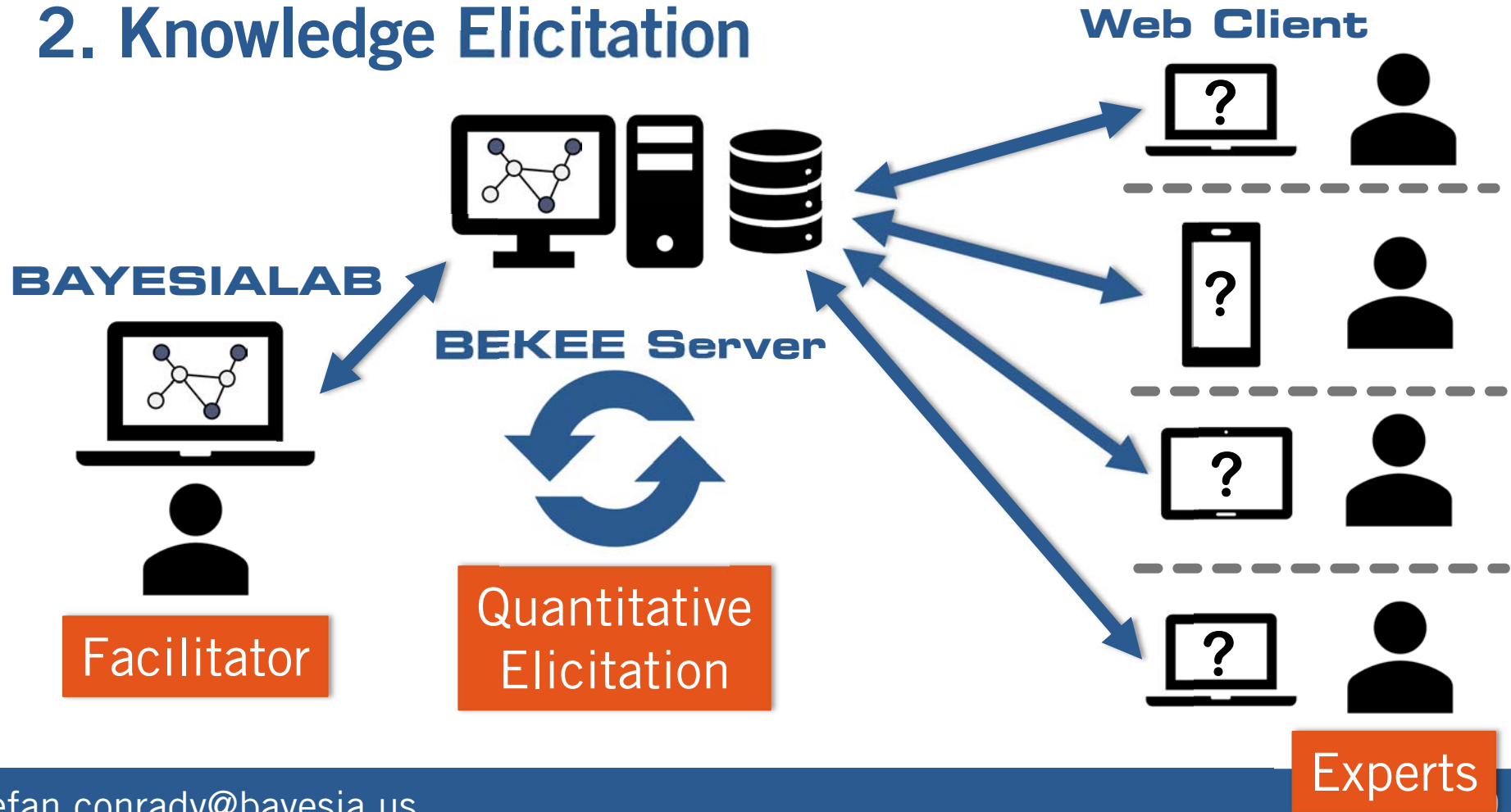
# 1. Brainstorming & Model Construction







## 2. Knowledge Elicitation



# Knowledge Elicitation

## Your Assessment Task

← → ↺ | bekee3.bayesia.com/#!Expert%20Sessions

BEKEE Navigation Pane

Stefan Conrady - Bayesia USA-SG ▾

Expert Sessions

### EV\_NYC - EV

**Environment**

Urban  47.25 % ☐

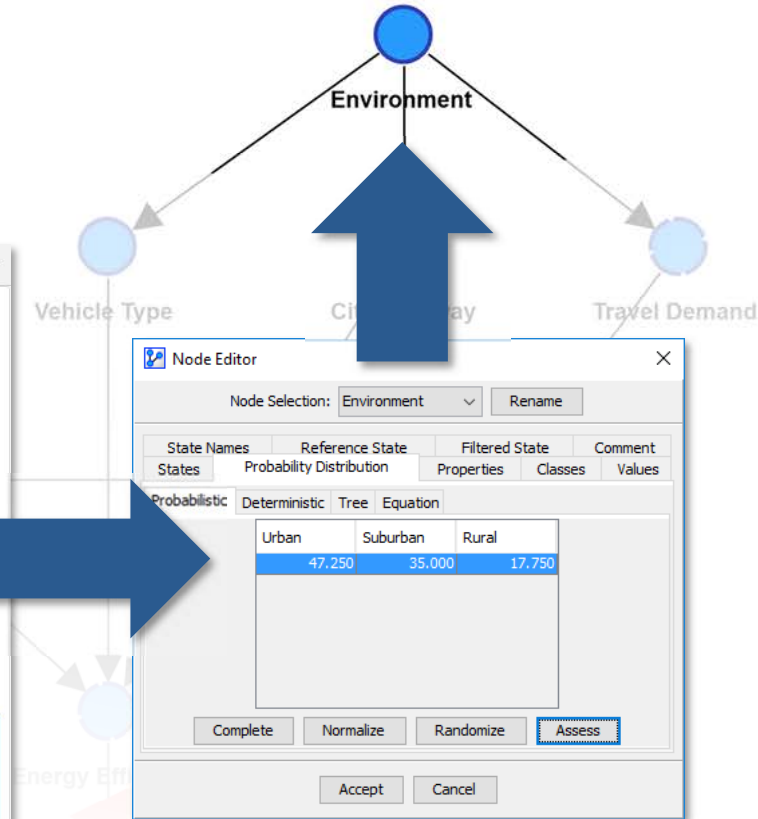
Suburban  35.0 % ☐

Rural  17.75 % ☐

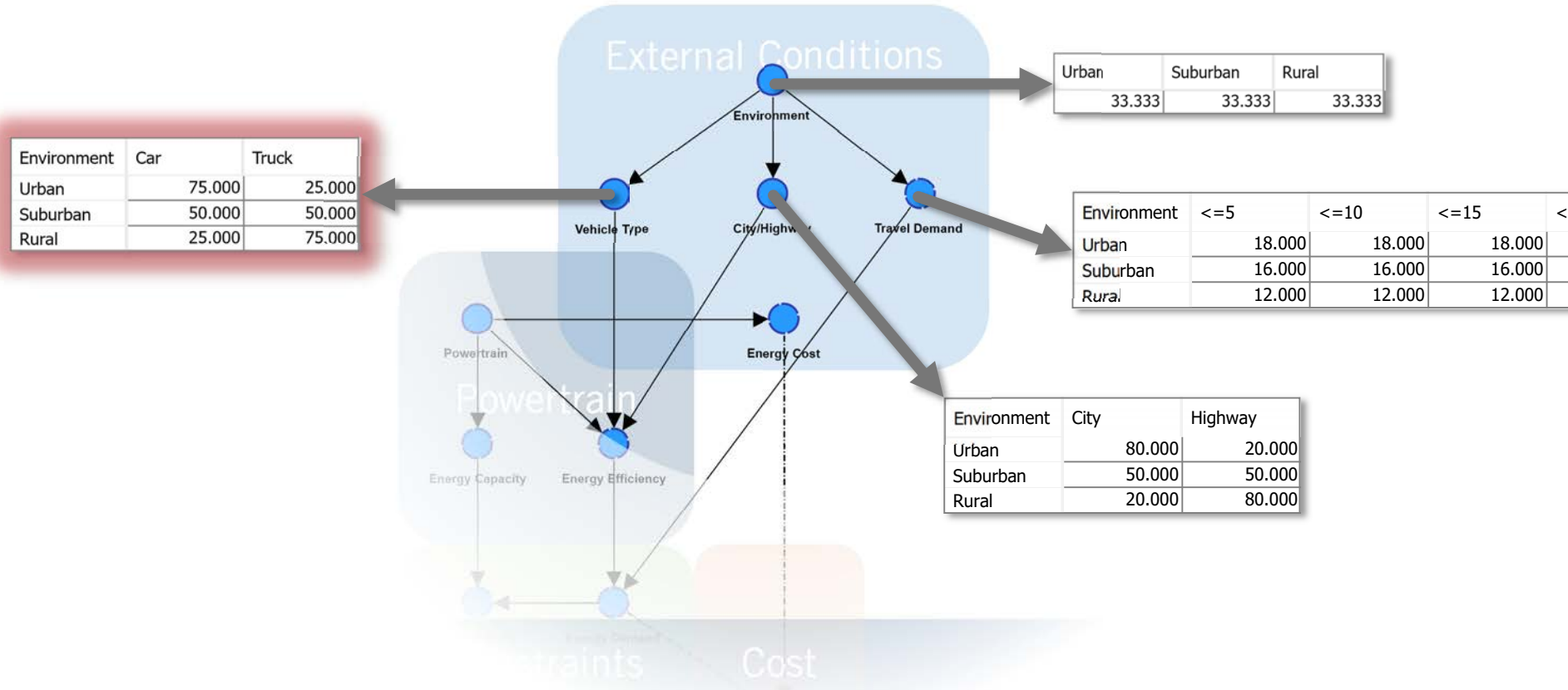
Confidence  75.0%

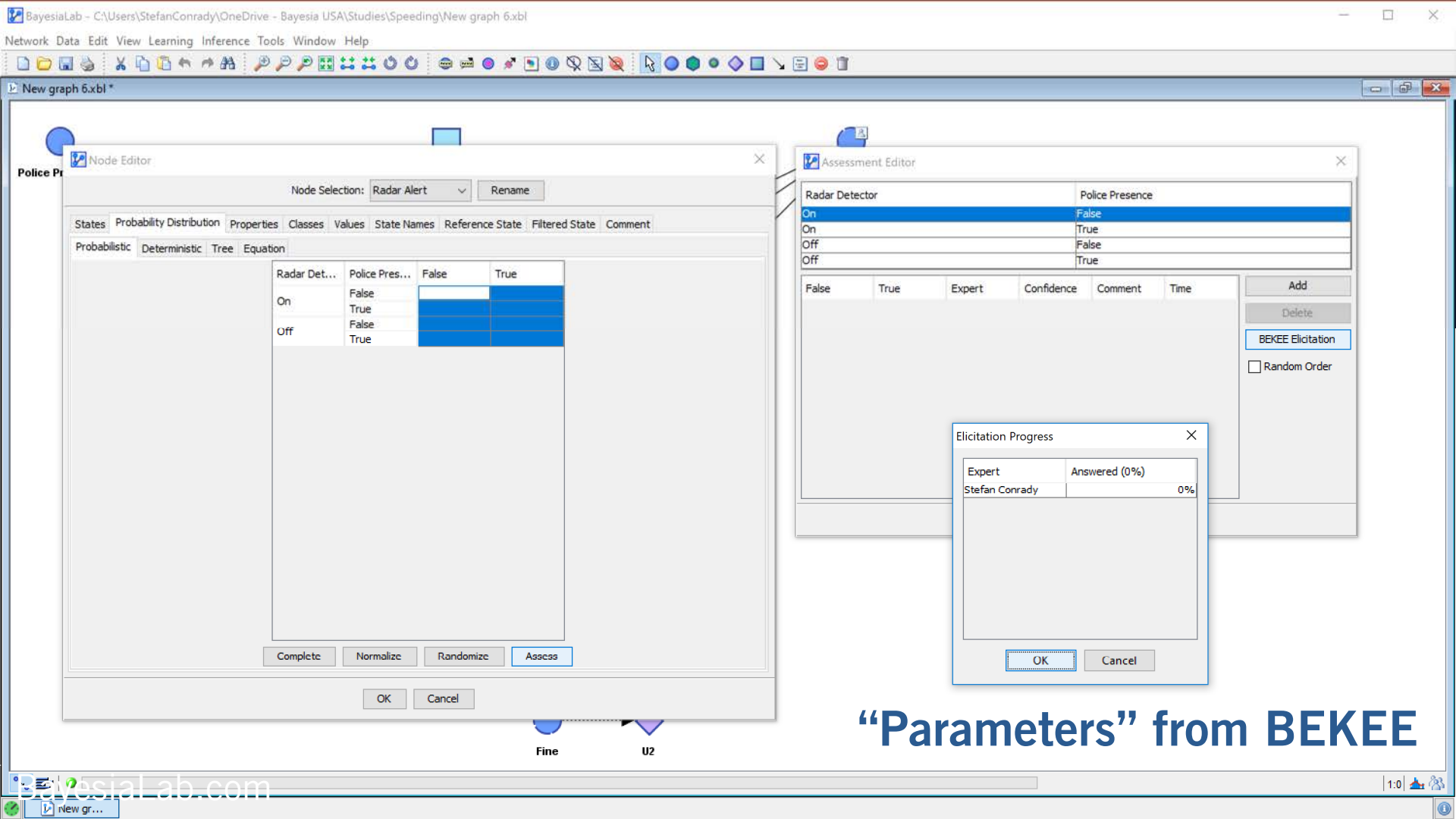
Comment

Validate



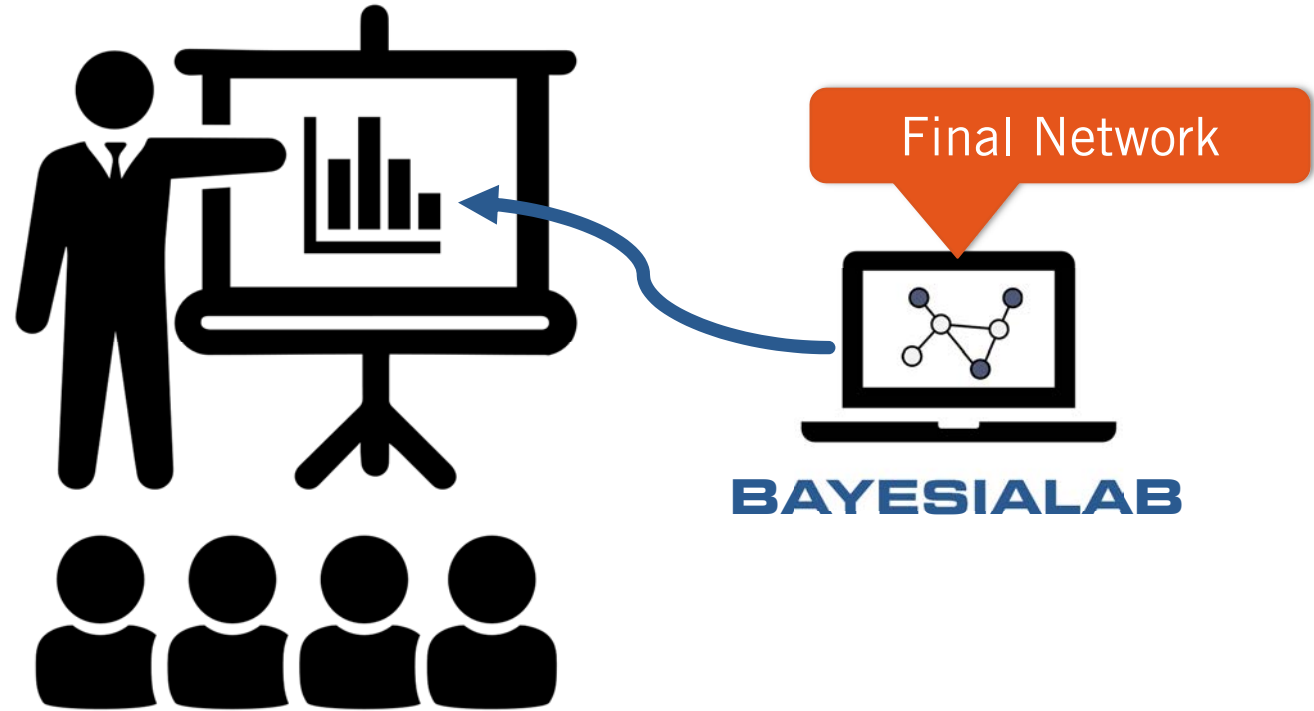
# Knowledge Elicitation

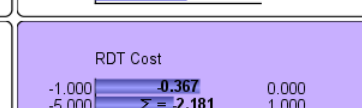
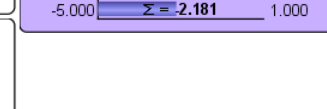
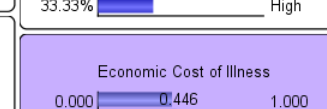
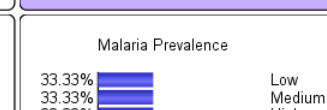
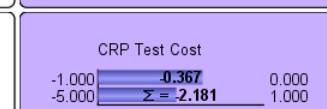
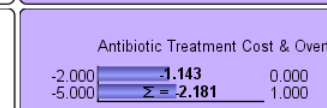
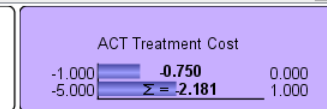
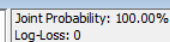
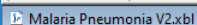






### 3. Inference, Analysis, and Optimization

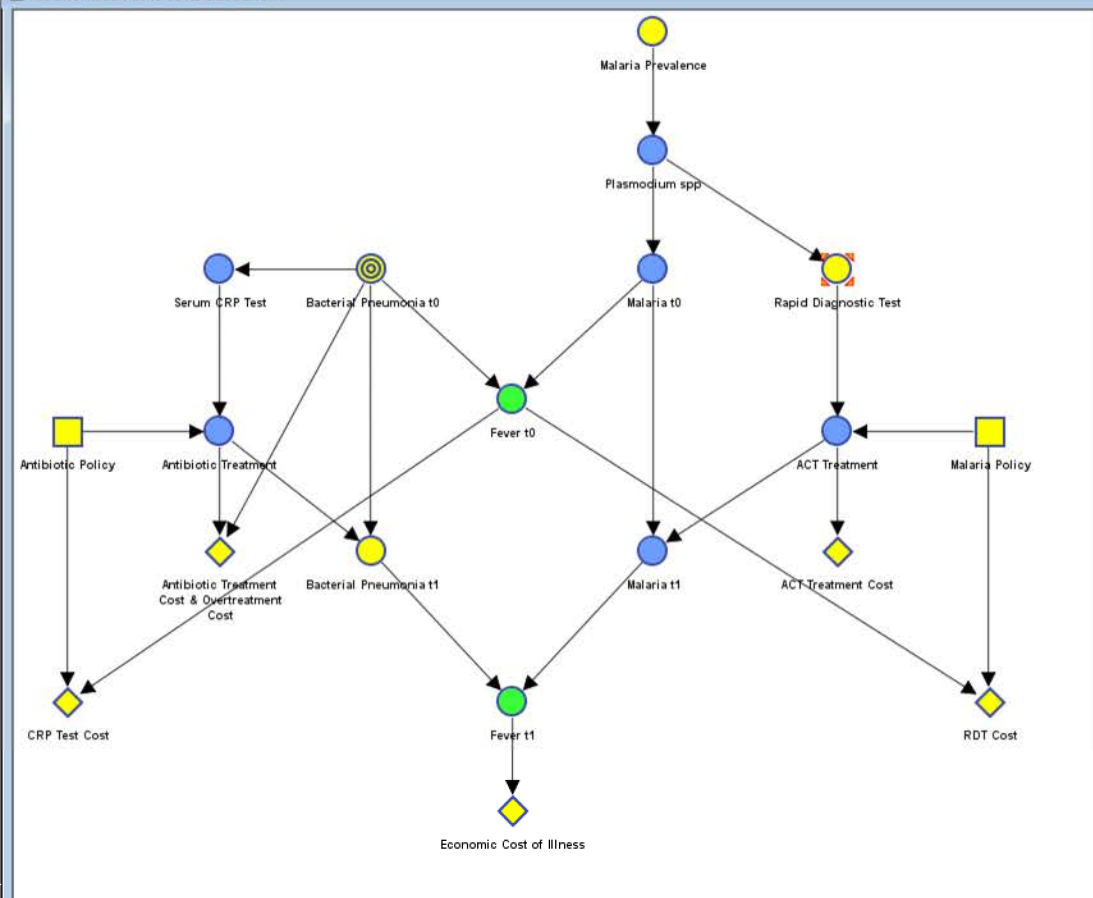




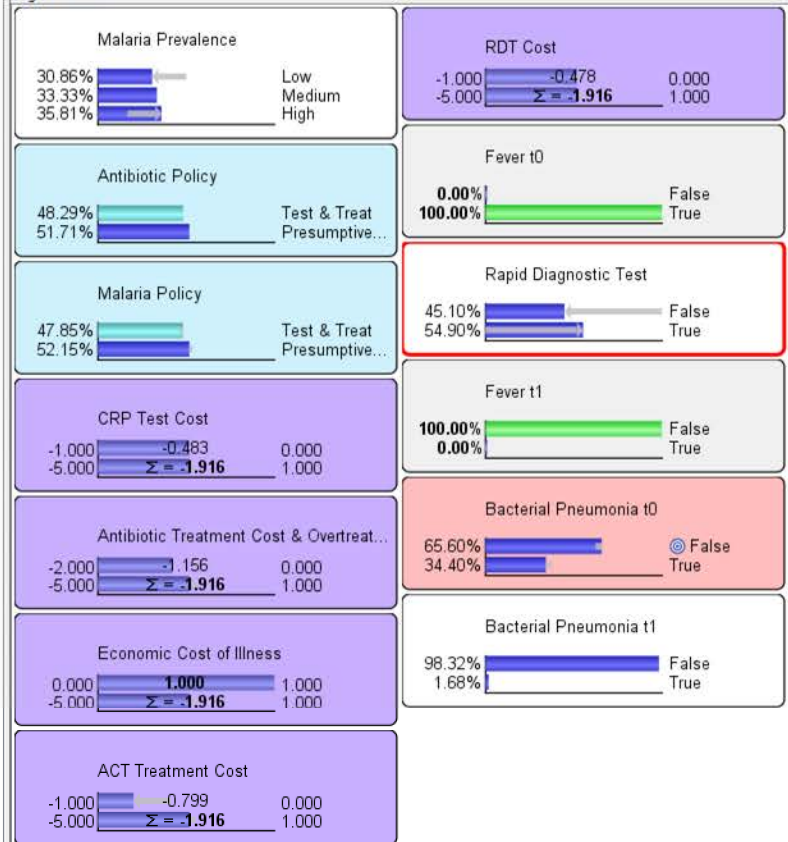
## Inference & Optimization

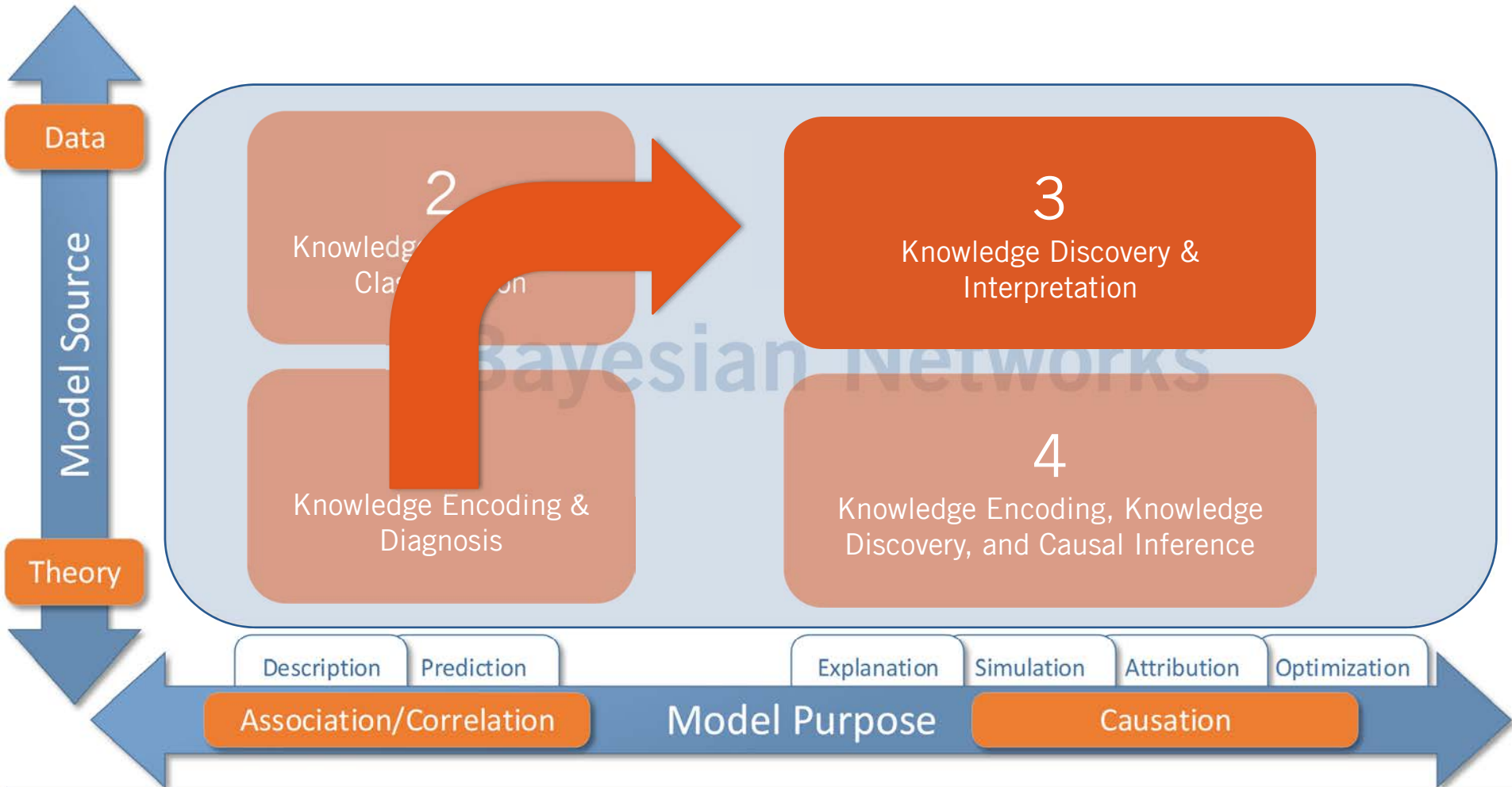


Malaria Pneumonia V3 reference.xbl \*



Joint Probability: 31.74%  
Log-Loss: 1.66

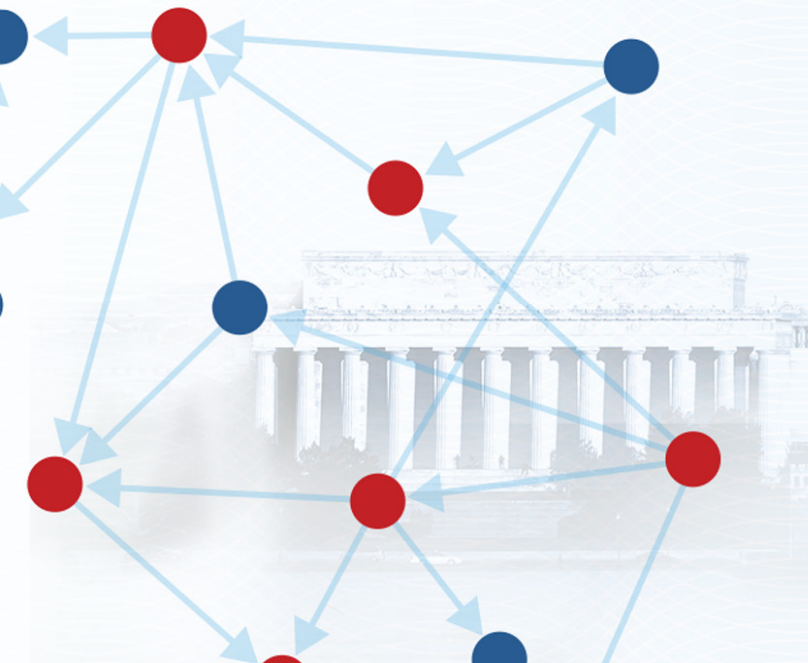








Exchange-Traded Funds  
Knowledge Discovery,  
Interpretation, and  
Anomaly Detection



# Problem Domain: Money Flows



Daily ETF Flows  
By Investment Focus





Main  
Objective

Deep  
Understanding



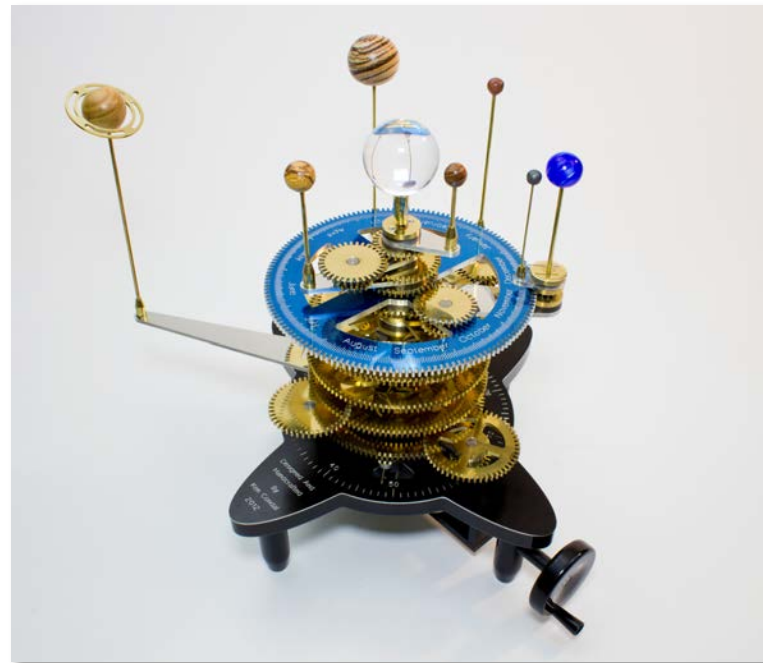




# Objective: Deep Understanding

“Deep understanding means knowing, not merely how things behaved yesterday, but also how things will behave under new hypothetical circumstances...”

*Judea Pearl, Causality (2009),  
Cambridge University Press*

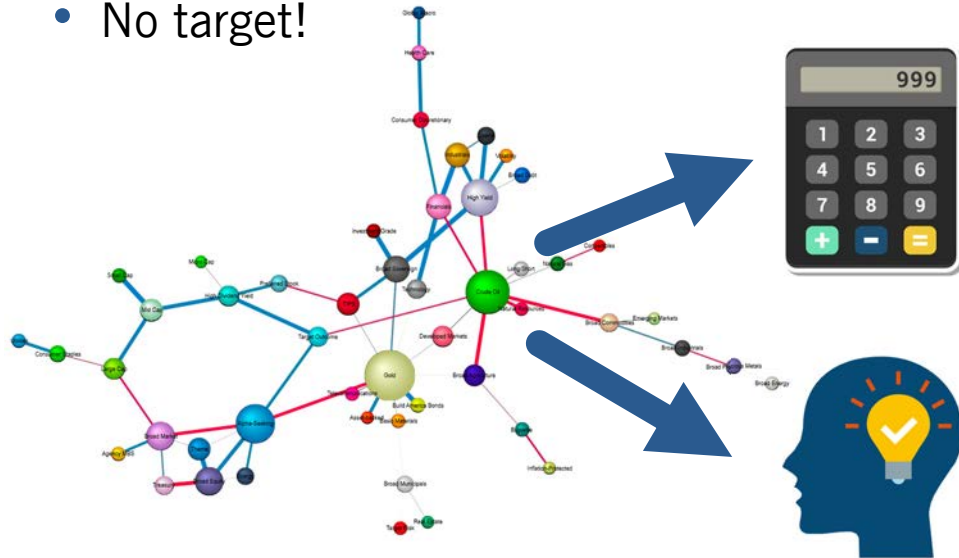


# Bayesian Network Learning



## Objective

- Learn single model for all 51 variables.
- No target!



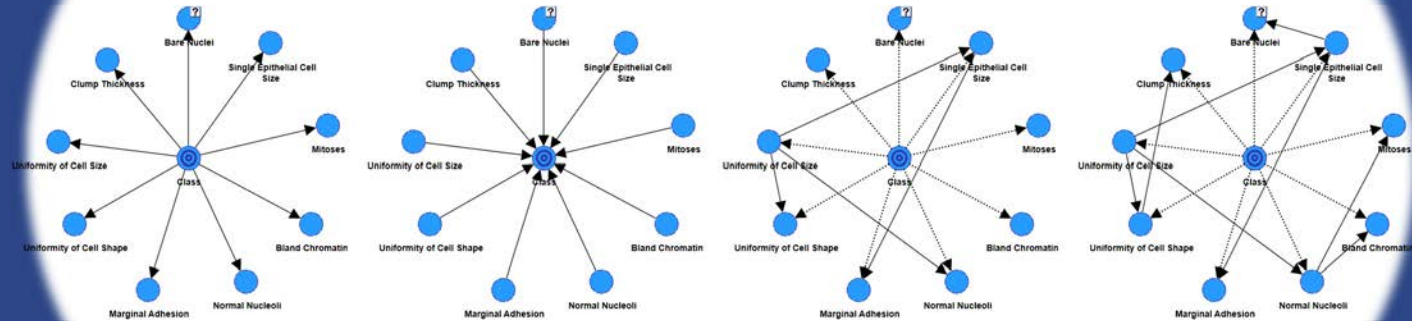
# Example 4: Exchange-Traded Funds

## BayesiaLab Workflow

- Data Source:
  - 1,147 Exchange-Traded Funds
  - Timeframe: 2014 – 2018
  - Daily Flow grouped by 51 investment themes
- Data Import
- Unsupervised Learning
  - SopLEQ (SC=0.35)

- 
- Alpha-Seeking
  - Basic Materials
  - Broad Equity
  - Consumer Discretionary
  - Energy
  - Financials
  - High Dividend Yield
  - Industrials
  - Mid Cap
  - Natural Resources
  - Preferred Stock
  - Technology
  - Agency MBS
  - Asset-backed
  - Broad Agriculture
  - Broad Commodities
  - Broad Debt
  - Broad Energy
  - Broad Industrials
  - Broad Market
  - Broad Municipals
  - Broad Sovereign
  - Build America Bonds
  - Buywrite
  - Consumer Staples
  - Convertibles
  - Crude Oil
  - Developed Markets
  - Emerging Markets
  - Global Macro
  - Gold
  - Health Care
  - High Yield
  - Inflation-Protected
  - Investment Grade
  - Large Cap
  - Loans
  - Long/Short
  - Micro Cap
  - Natural Gas
  - Real Estate
  - Small Cap
  - TIPS
  - Target Outcome
  - Target Risk
  - Telecommunications
  - Theme
  - Treasury
  - Utilities
  - Volatility
  - Broad Precious Metals

# Learning=Searching

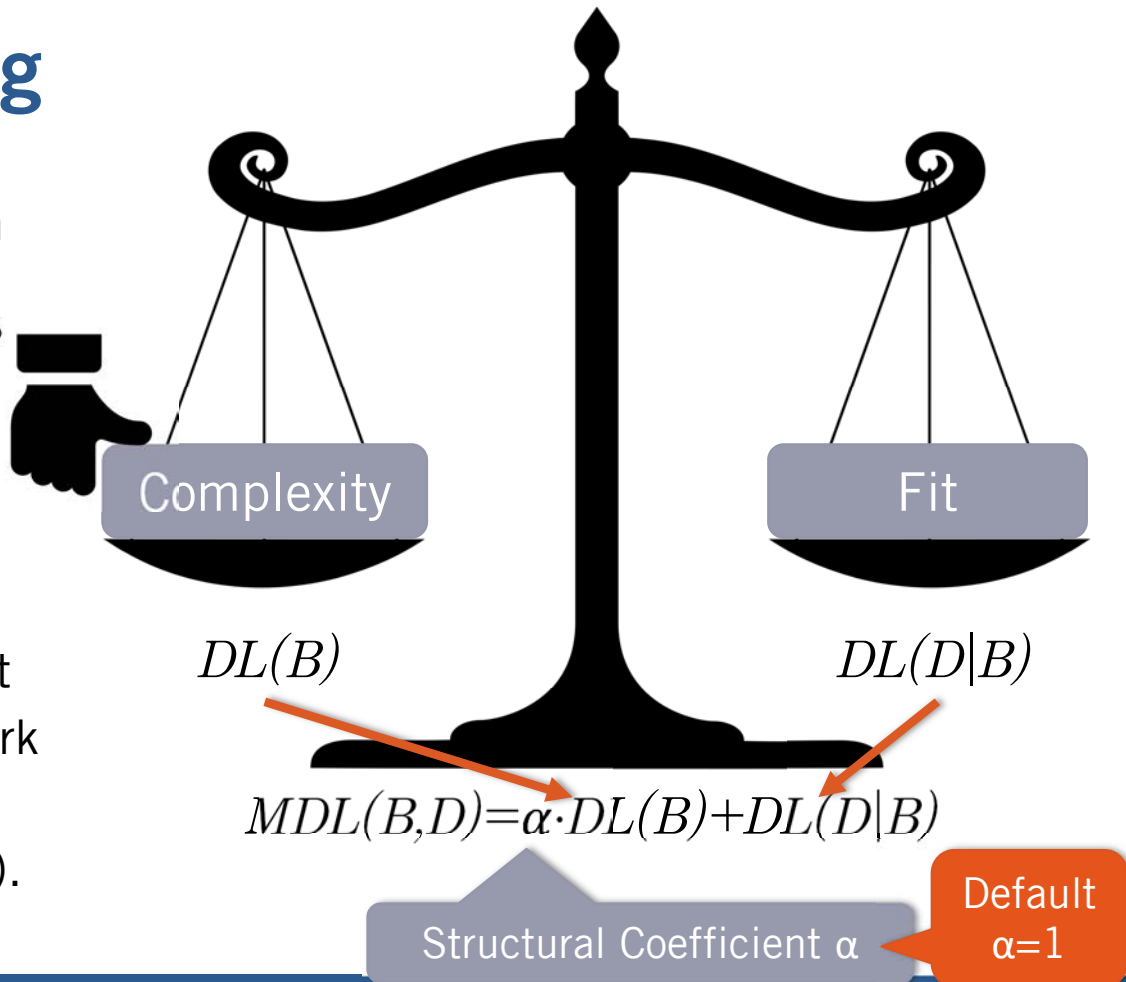




# Learning=Searching

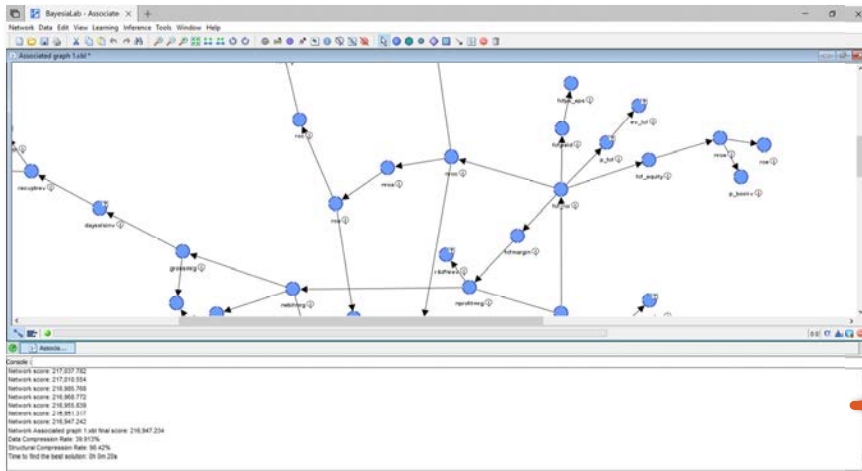
## Minimum Description Length

- $DL(B)$  is the number of bits to represent the Bayesian network  $B$  (graph and probabilities), and
- $DL(D|B)$  is the number of bits to represent the dataset  $D$  given the Bayesian network  $B$  (likelihood of the data given the Bayesian network).



# Learning=Searching

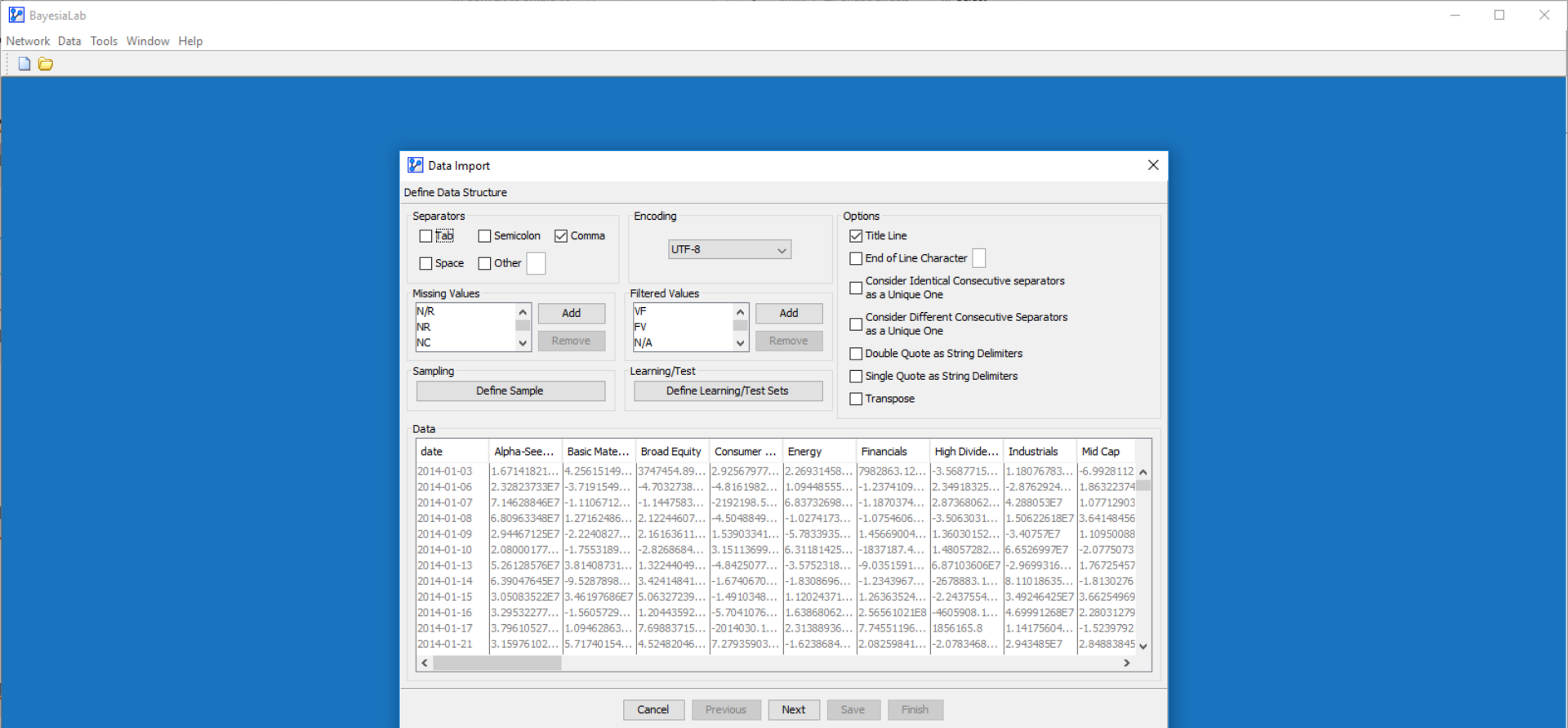
## Minimum Description Length



Network score: 217,884.553  
Network score: 217,743.338  
Network score: 217,610.856  
Network score: 217,483.237  
Network score: 217,359.875  
Network score: 217,241.952  
Network score: 217,195.628  
Network score: 217,152.903  
Network score: 217,113.827  
Network score: 217,075.16  
Network score: 217,037.782  
Network score: 217,010.554  
Network score: 216,985.768  
Network score: 216,968.772  
Network score: 216,955.839  
Network score: 216,951.317  
Network score: 216,947.242

**Network Associated graph 1.xbl final score: 216,947.234**  
**Data Compression Rate: 39.913%**  
**Structural Compression Rate: 98.42%**  
**Time to find the best solution: 0h 0m 20s**

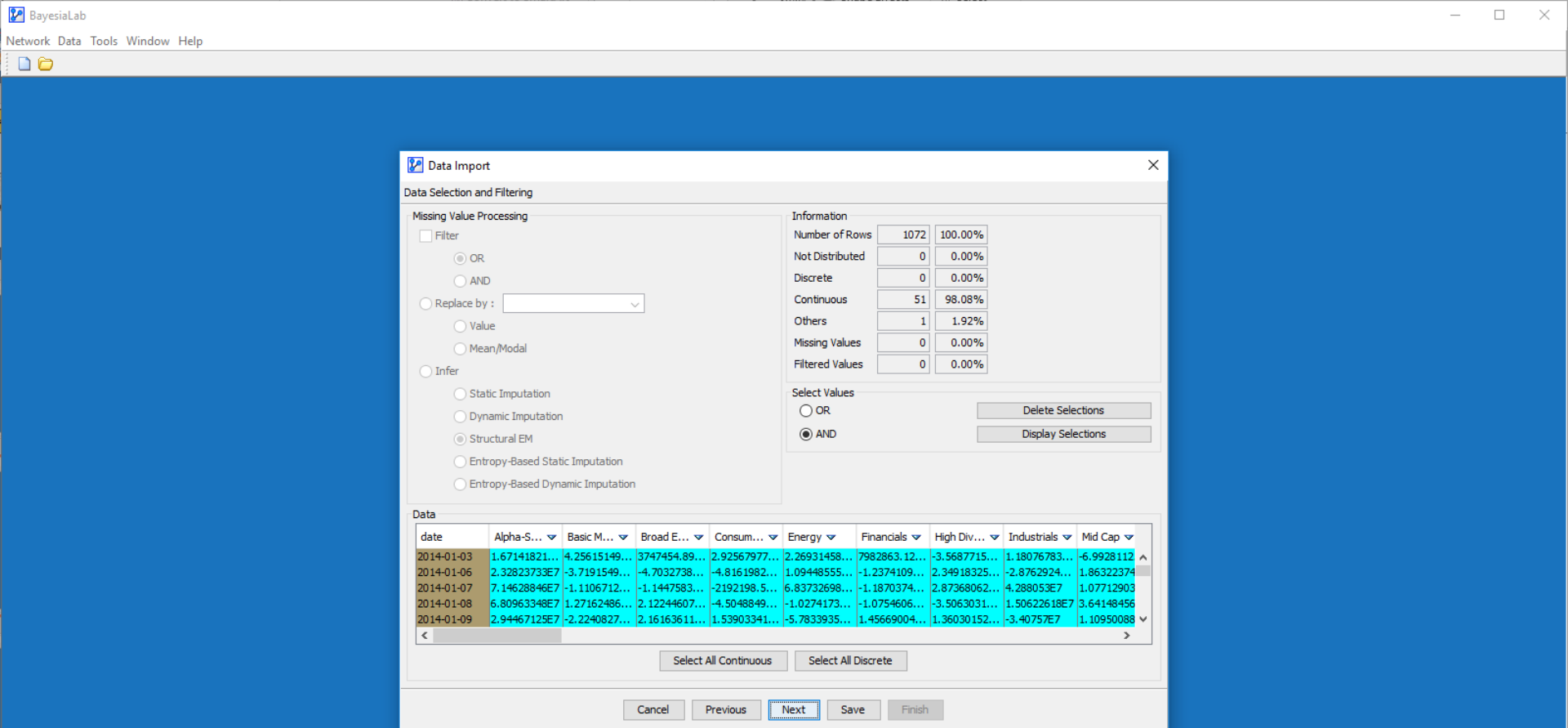
MDL Score



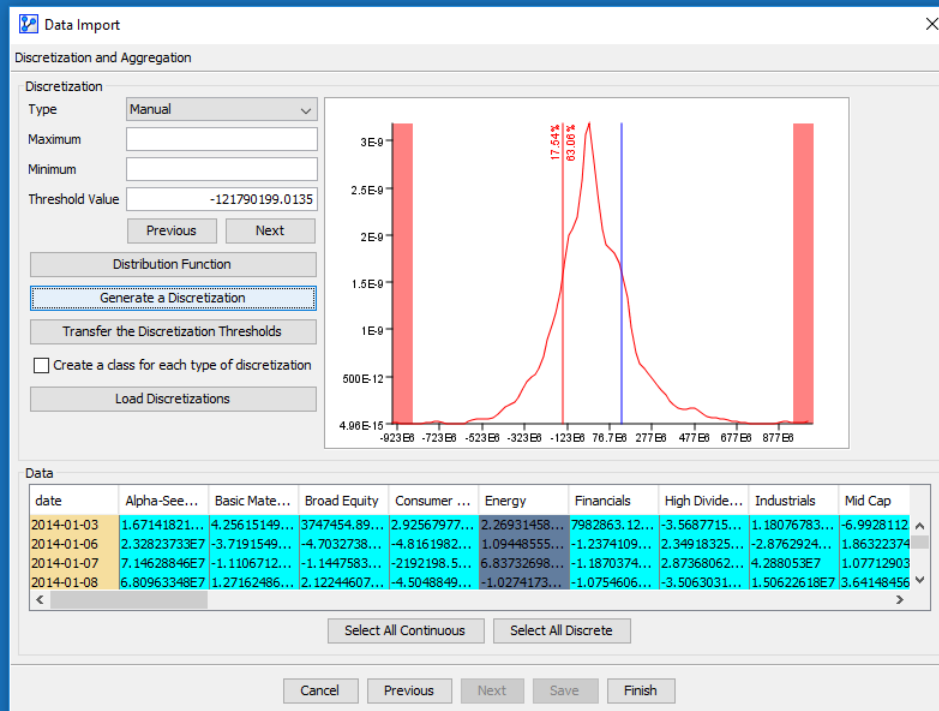
# Data Import Wizard

# Variable Type Definition

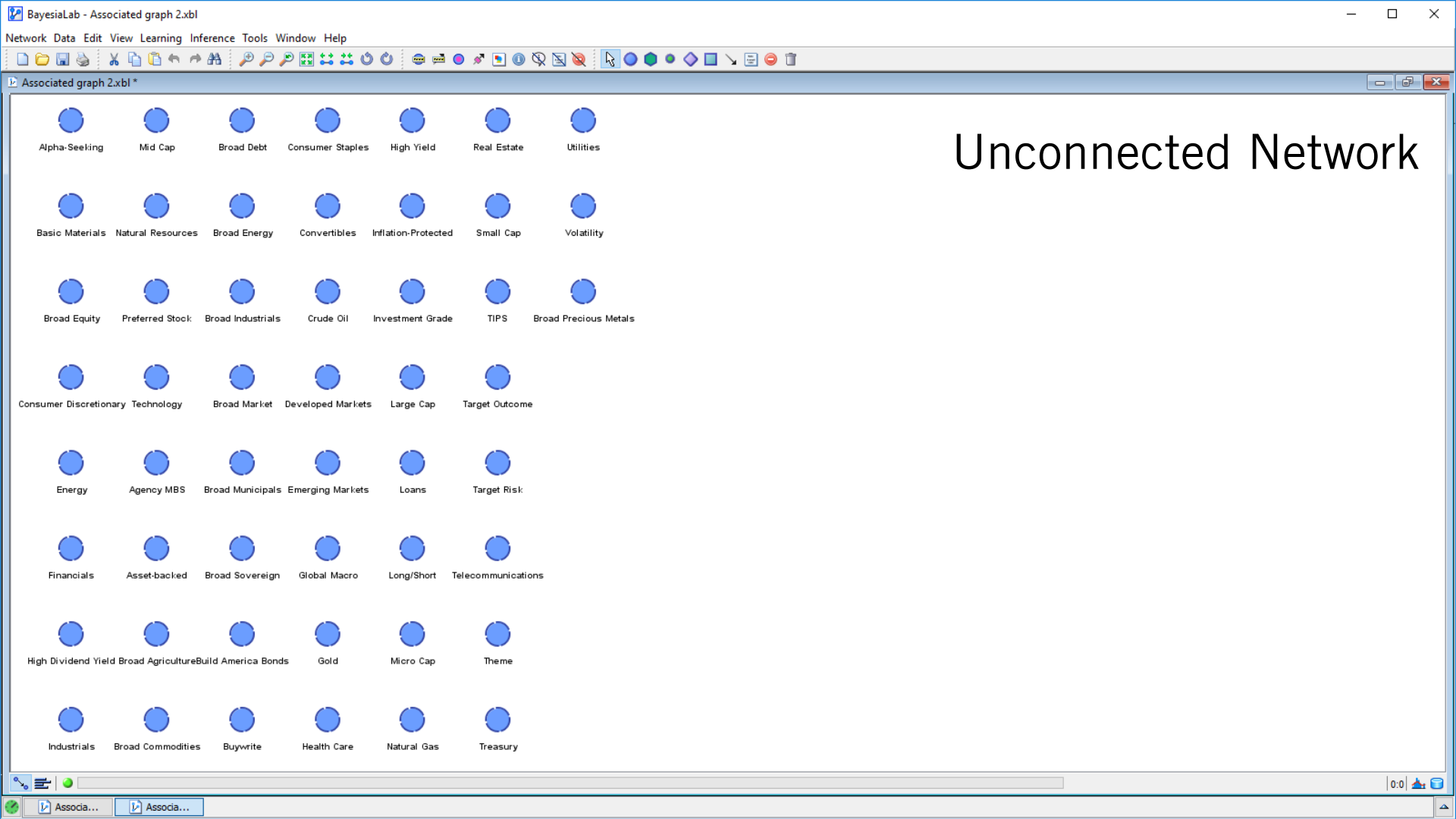


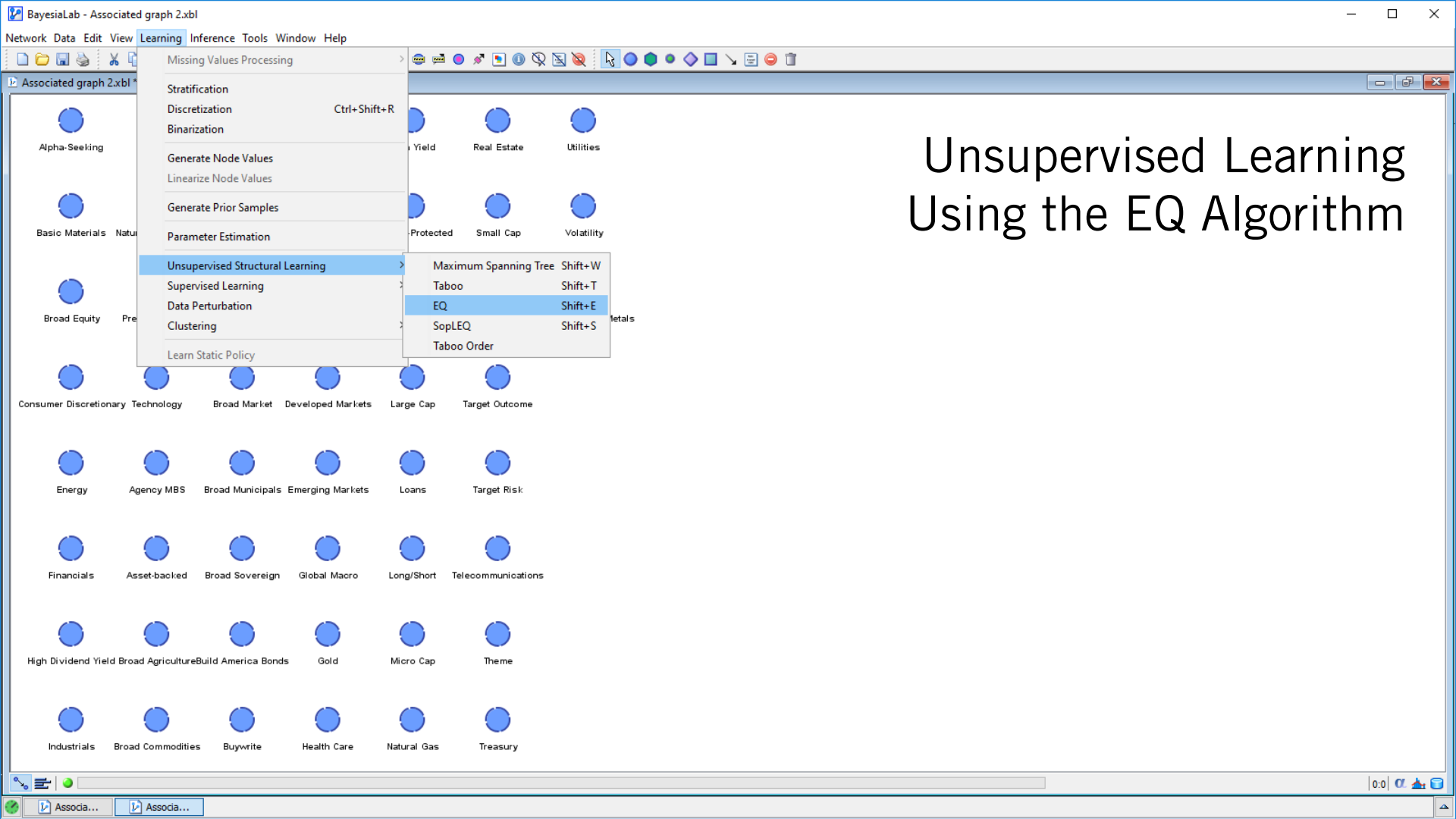


# Missing Values Processing



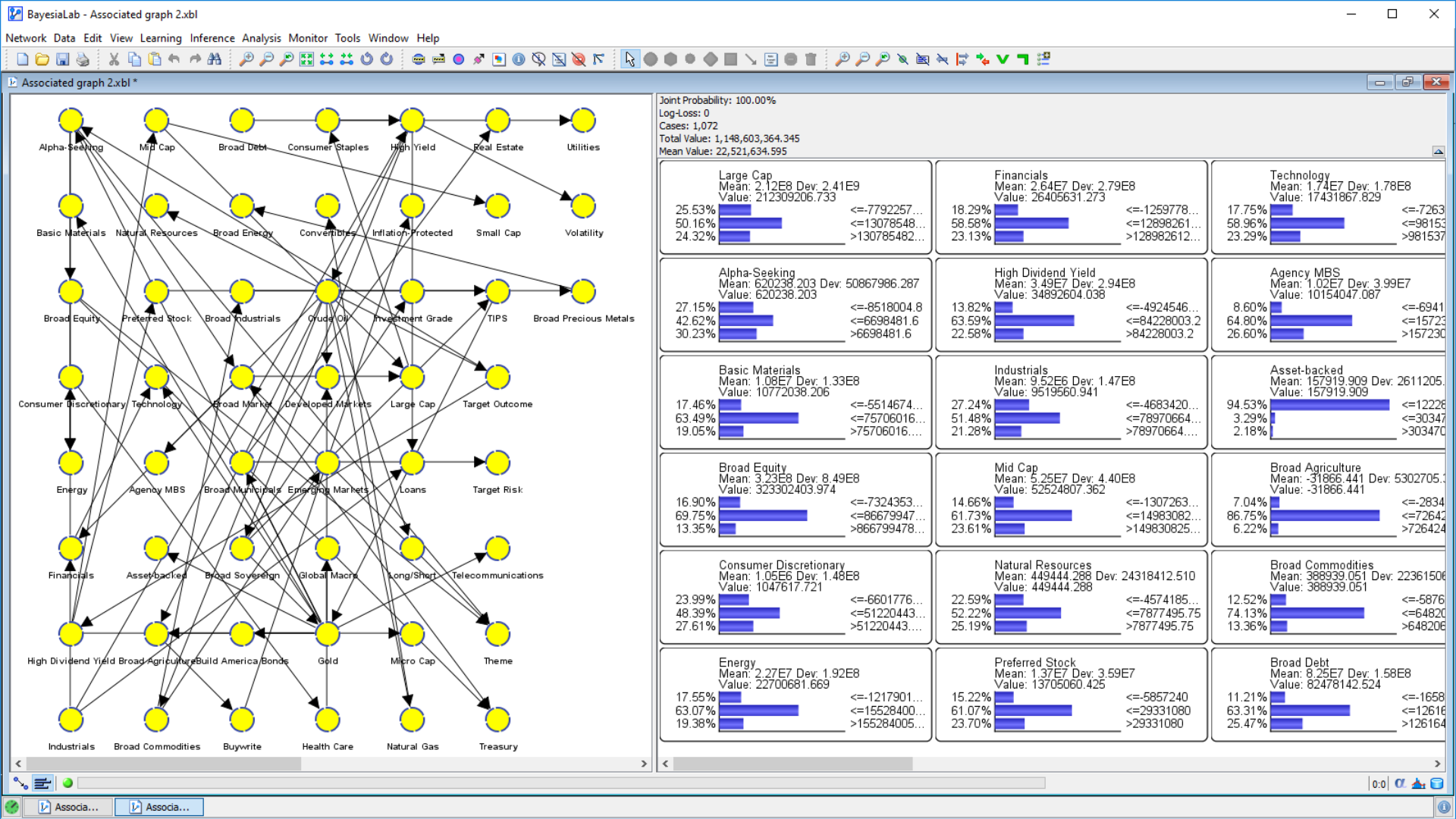
# Discretization

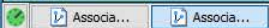


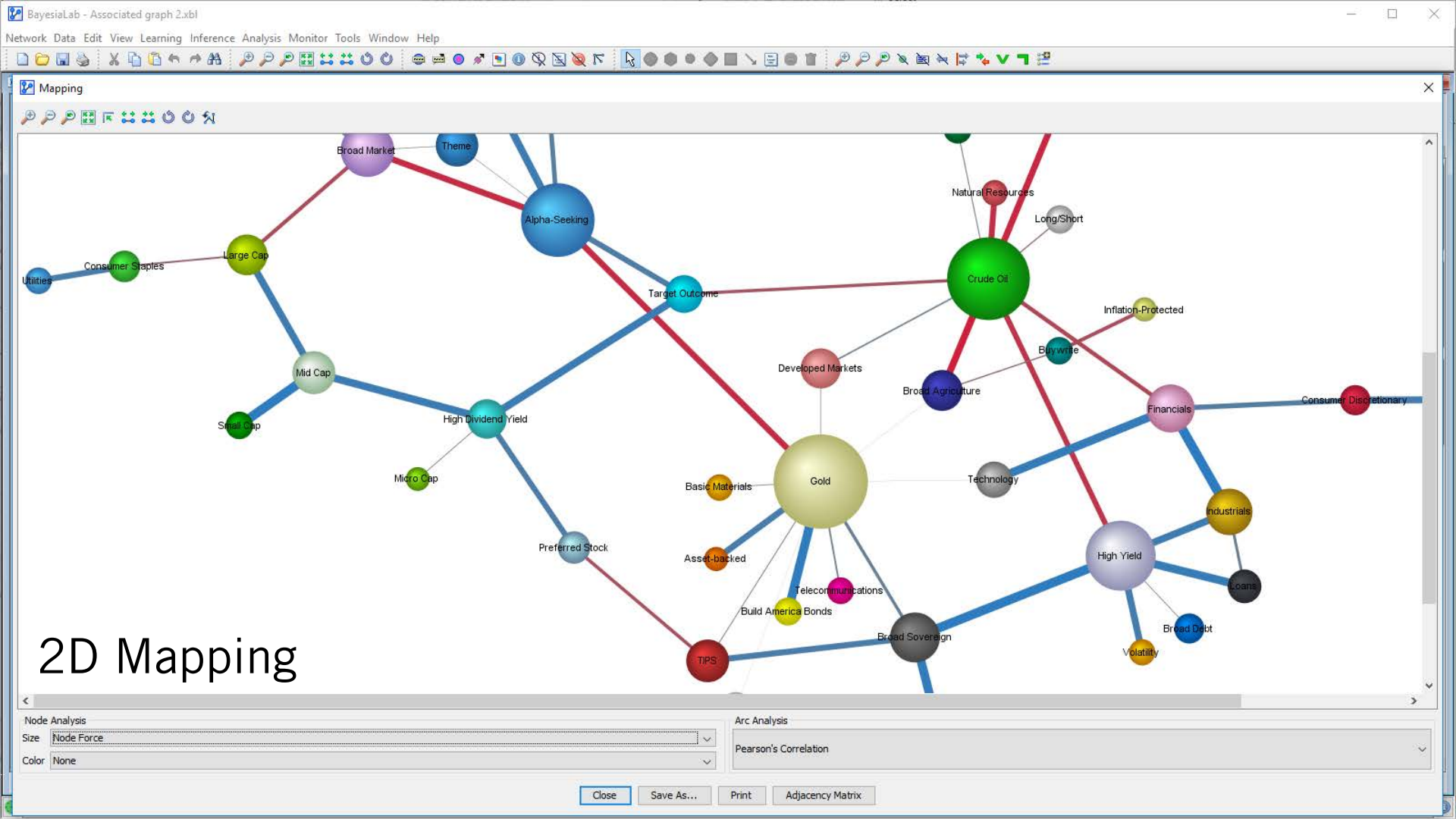


# Unsupervised Learning Using the EQ Algorithm

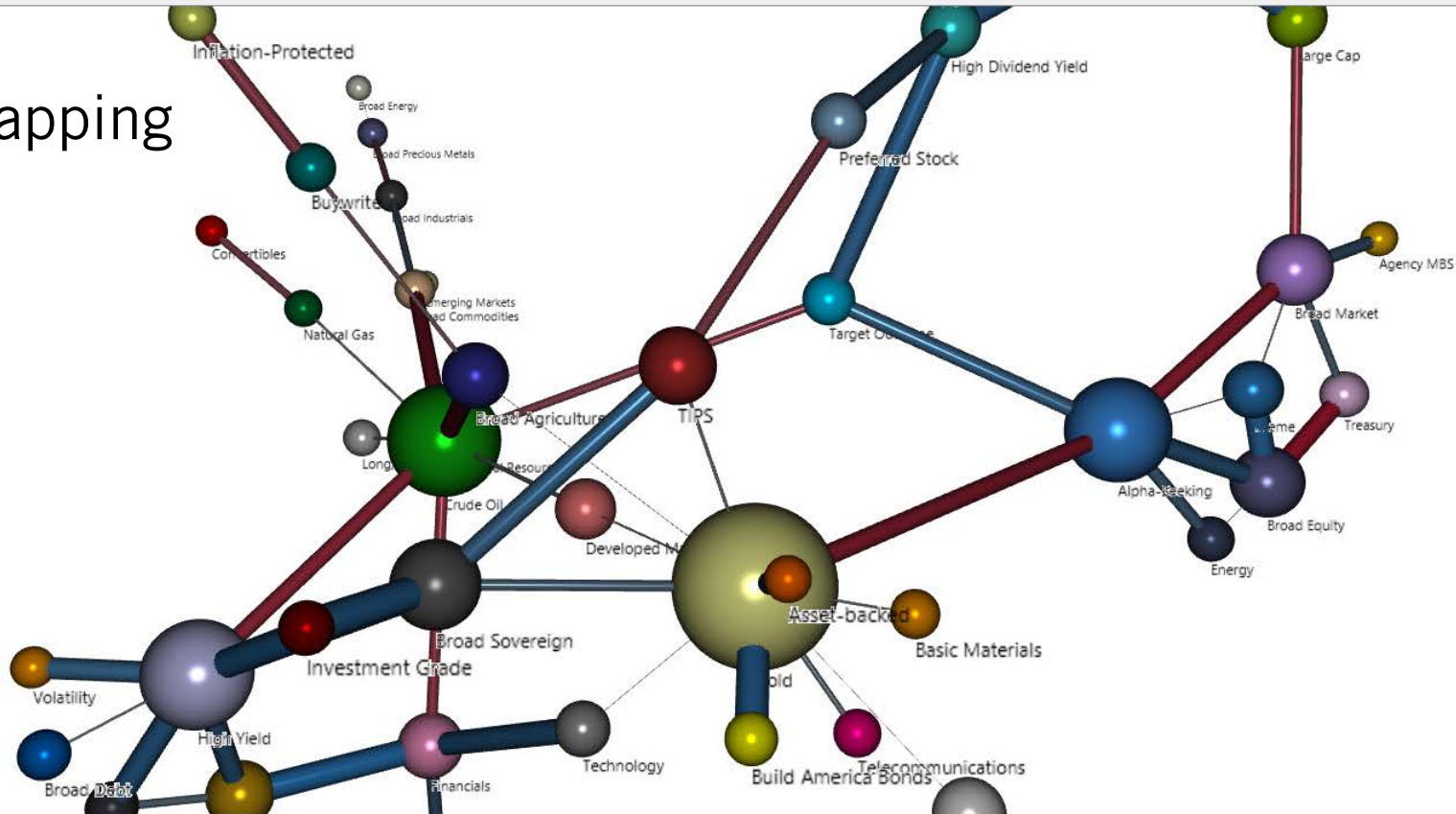




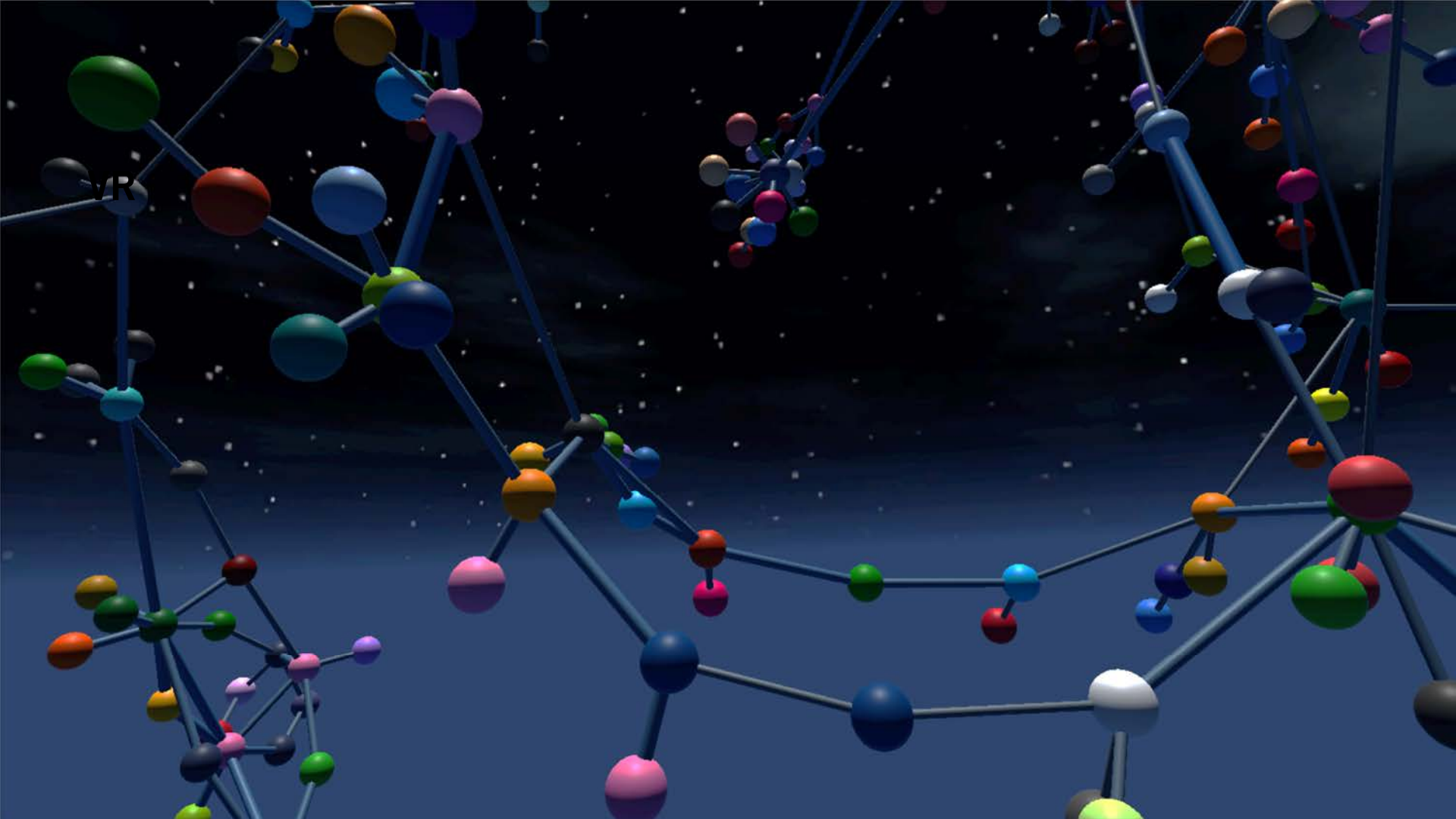




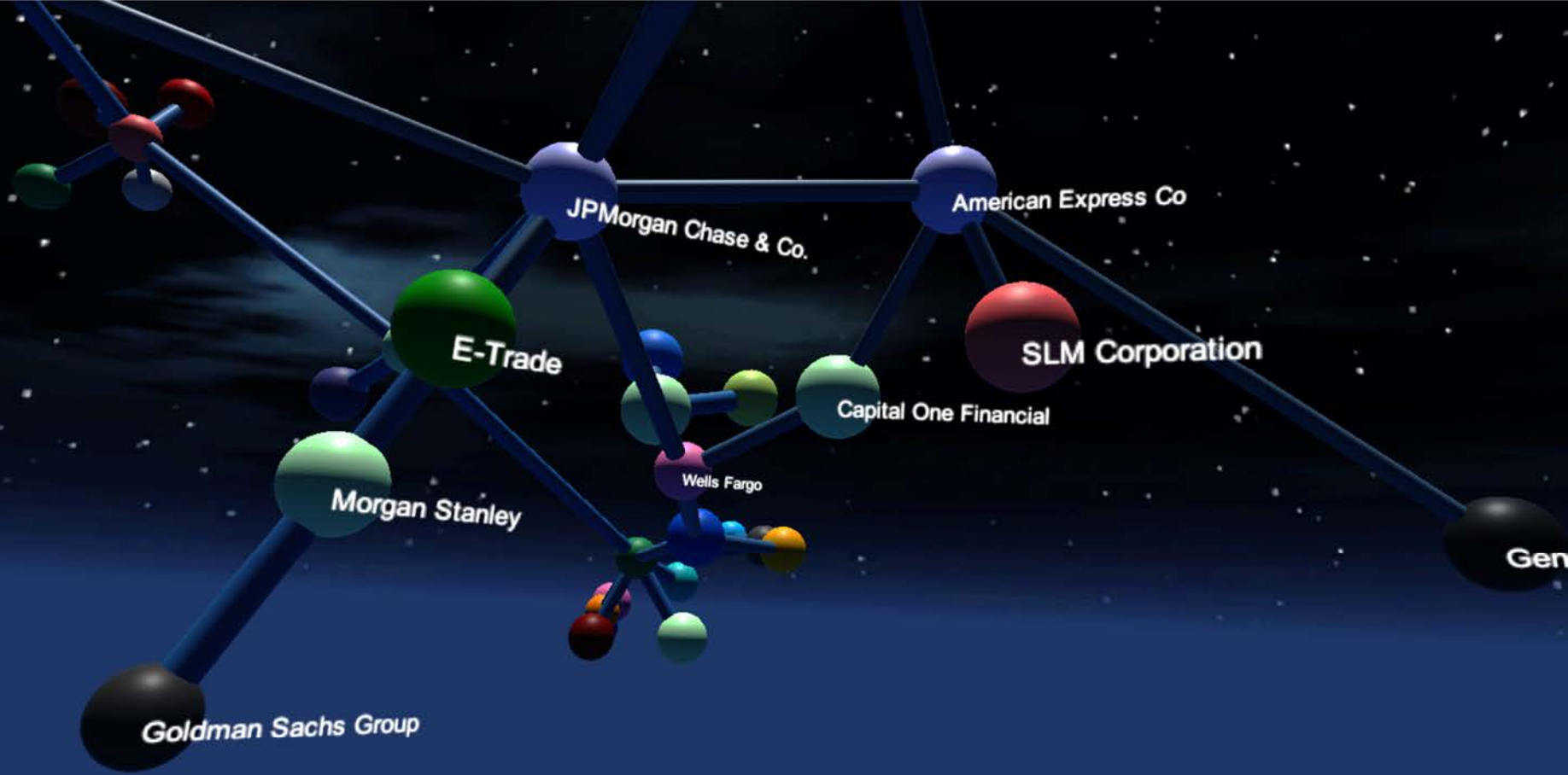
# 3D Mapping

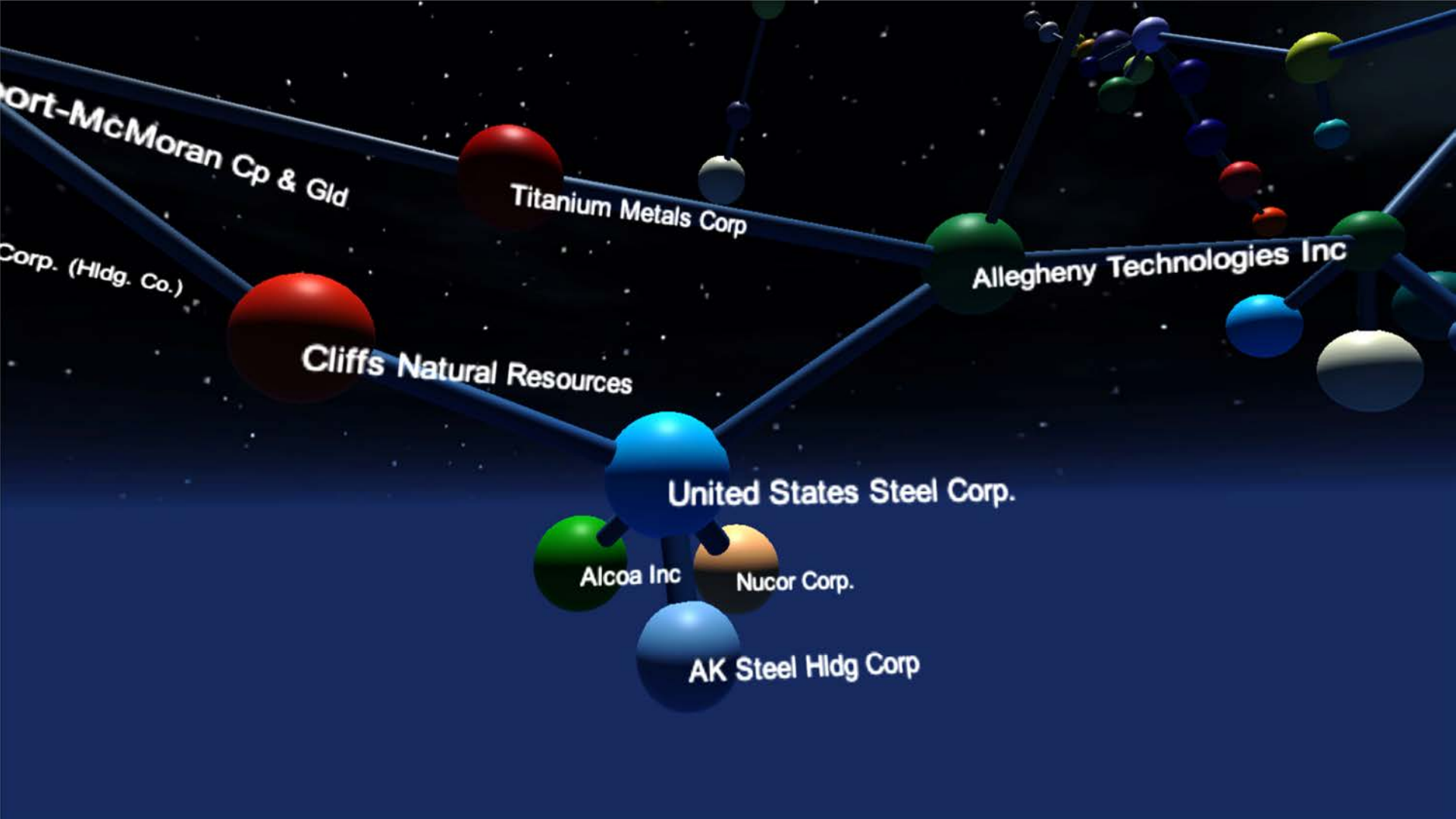




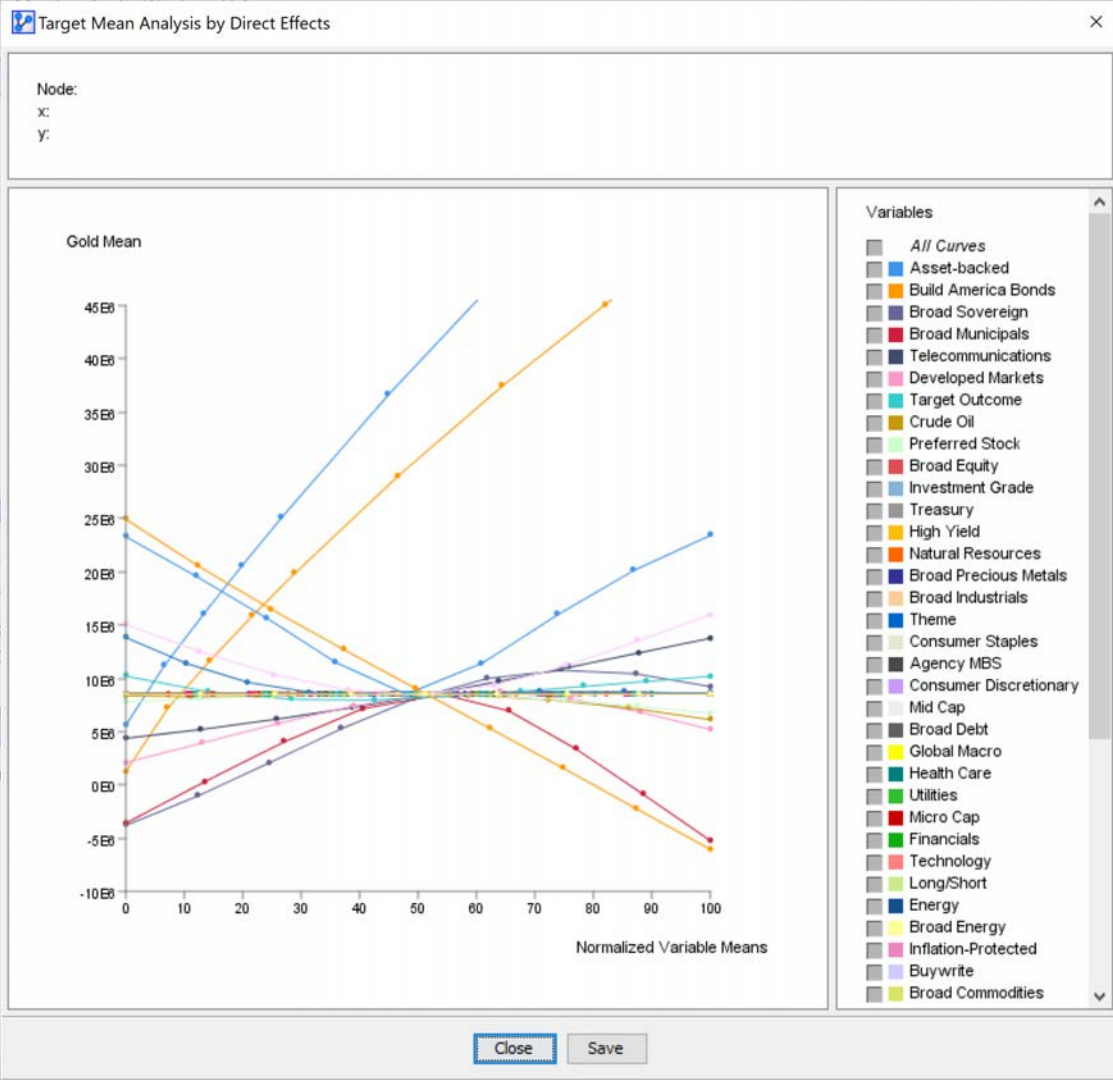


VR





## Target Mean Analysis (Direct Effect)





# Anomaly Detection

## The Curse of Dimensionality

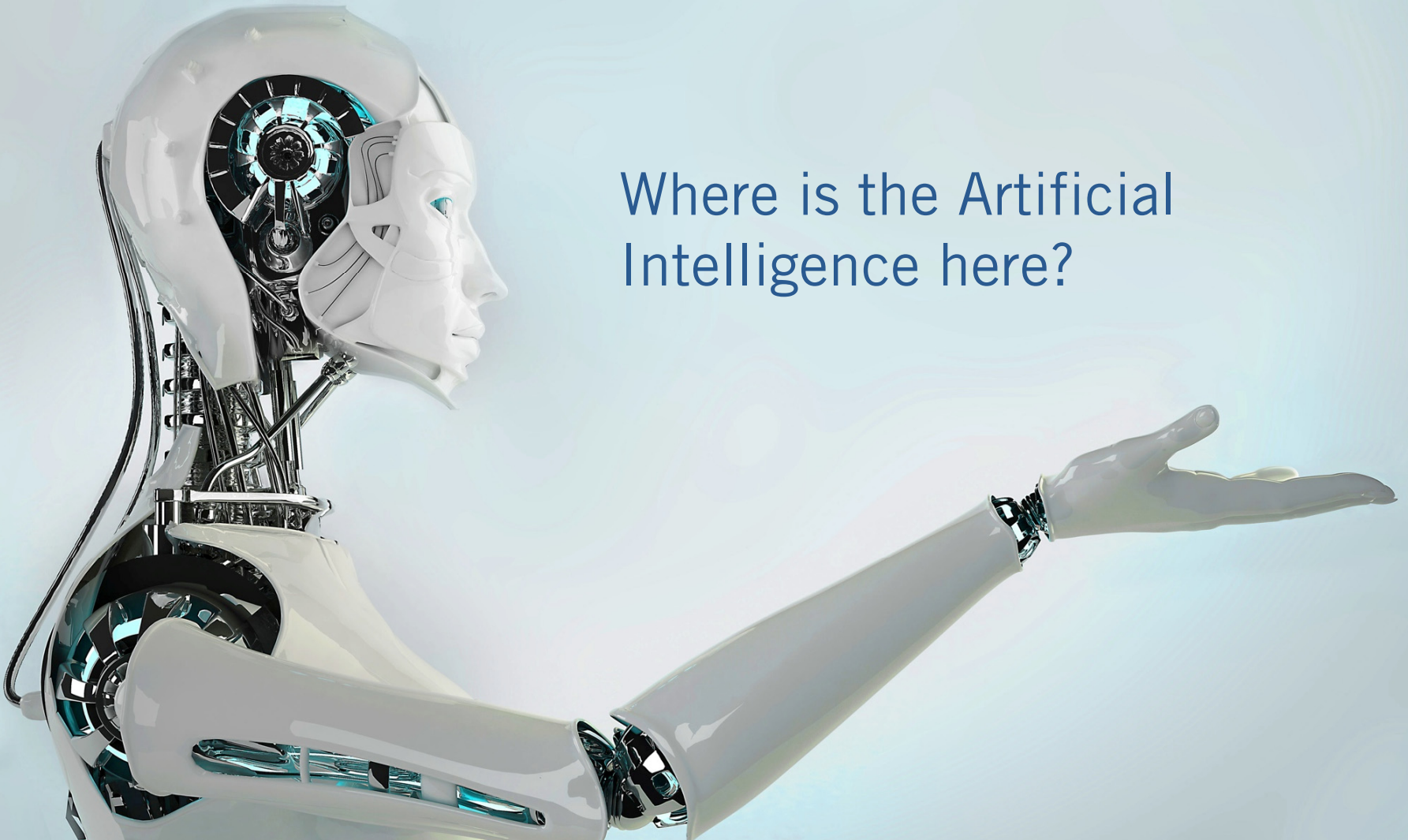
- “...as dimensionality increases, the distance to the nearest data point approaches the distance to the farthest data point.”
- In other words, the contrast in distances of different data points becomes nonexistent. For high dimensional data sets, this means using outlier detection methods that are based on nearest neighbor will lead to outlier scores that are indistinguishable.

# Anomaly Detection

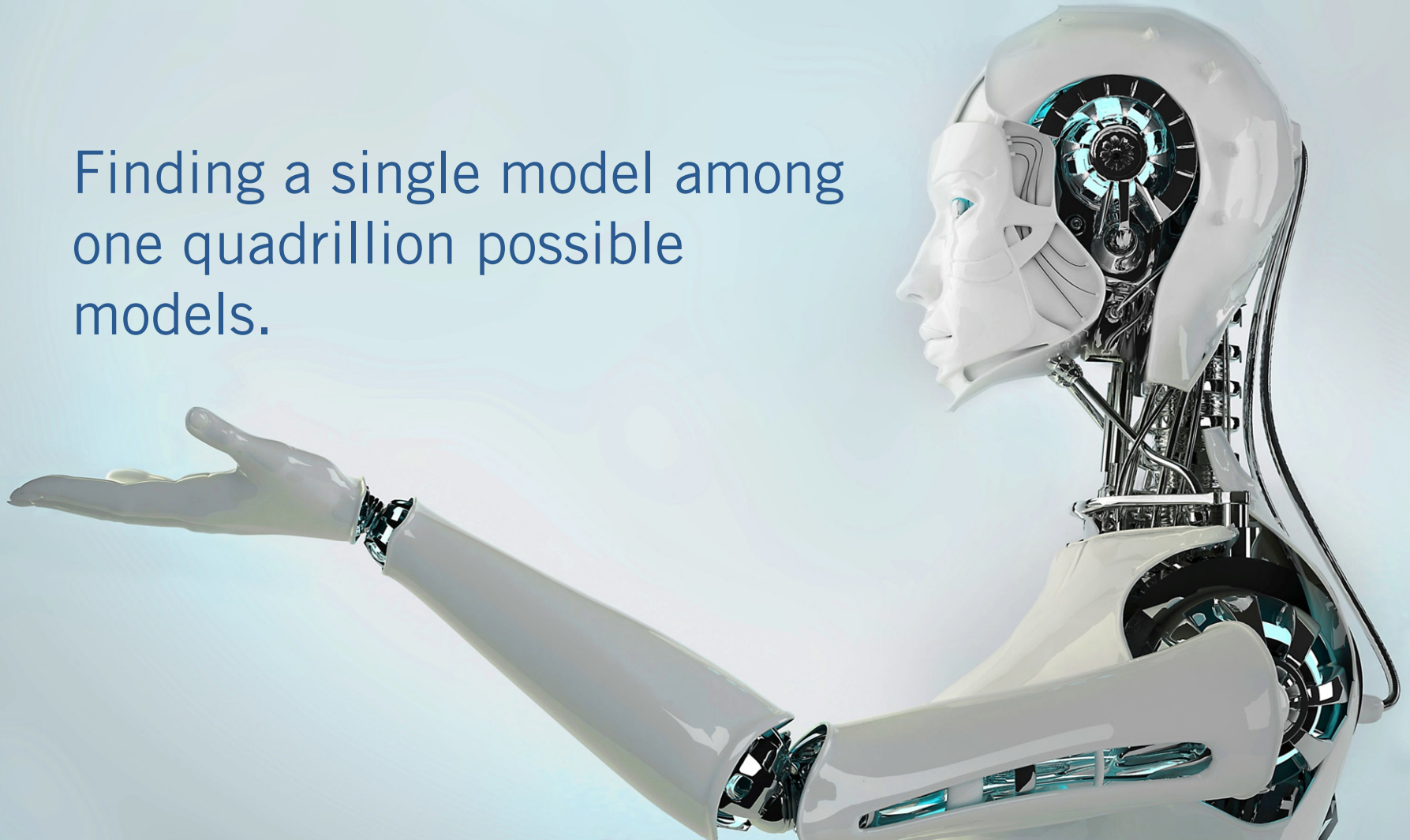
## Anomaly Detection with Bayesian Networks

- With a Bayesian network, we can avoid the problem of the nearest/farthest distance measure, which becomes unreliable in higher dimensions.
- For any new observation, we can compute its likelihood given the network. This tells us how probable or improbable an observation is.

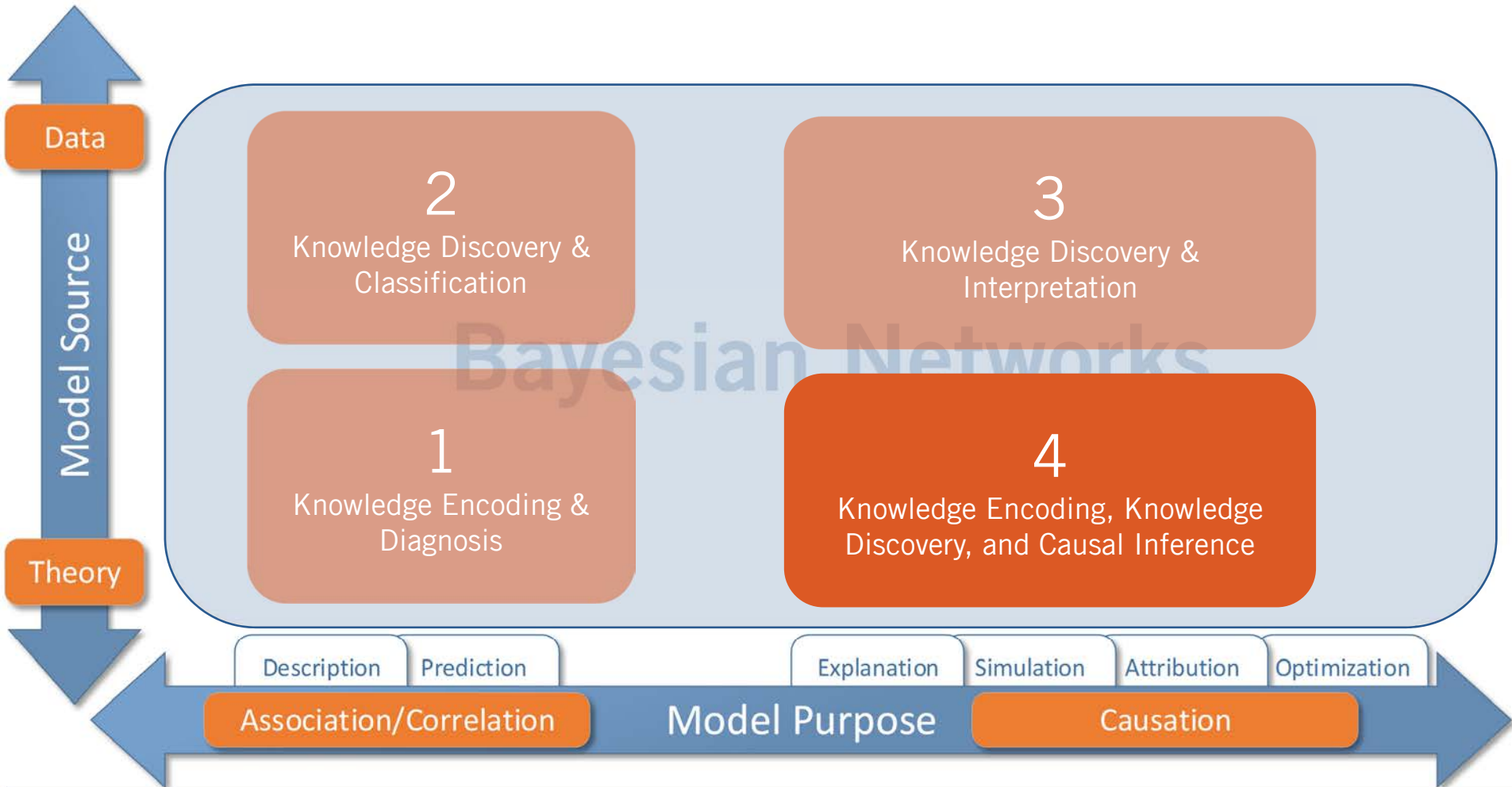
Where is the Artificial  
Intelligence here?



Finding a single model among  
one quadrillion possible  
models.

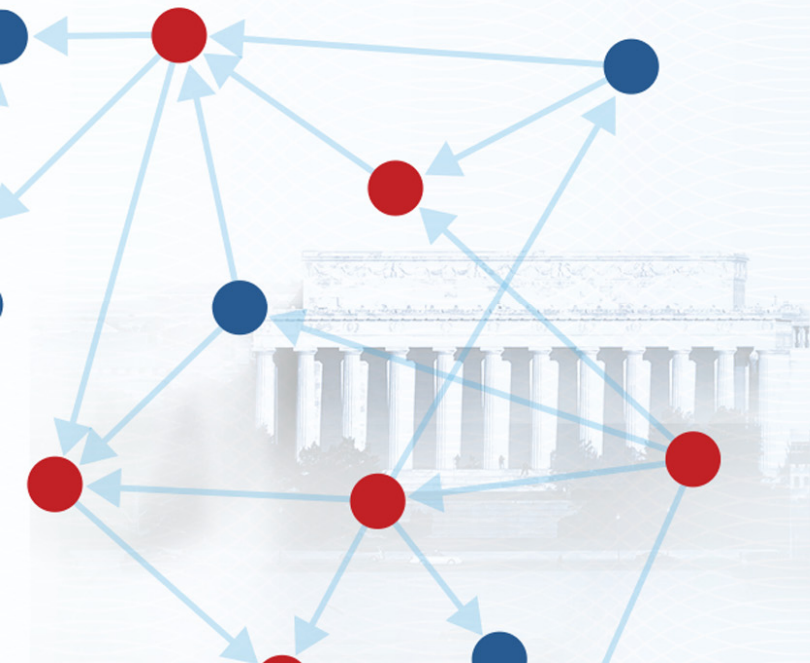








# Causal Inference Evaluating the Effectiveness of Information Campaigns





# Countering Anti-American Attitudes in Germany







# Introductory Example

## Telephone Survey

- Afterwards, a market research firm conducts a telephone survey of 1,000 adults to understand the effect of the promotion on attitudes.

| Ad Exposure | Nationality | Website Visit | Attitude |
|-------------|-------------|---------------|----------|
| 0           | 1           | 0             | 0        |
| 0           | 0           | 1             | 1        |
| 0           | 1           | 0             | 0        |
| 0           | 0           | 0             | 0        |
| 1           | 1           | 0             | 1        |
| 1           | 1           | 0             | 0        |
|             |             | 1             | 1        |
|             |             | 1             | 0        |
|             |             | ⋮             | ⋮        |
|             |             | 1             | 0        |





**Observational Data**

# Introductory Example

Analyzing the survey with a cross-tab...

| Ad Exposure | Nationality | Website Visit | Attitude |
|-------------|-------------|---------------|----------|
| 0           | 1           | 0             | 0        |
| 0           | 0           | 1             | 1        |
| 0           | 1           | 0             | 0        |
| 0           | 0           | 0             | 0        |
| 1           | 1           | 0             | 1        |
| 1           | 1           | 0             | 0        |
| 1           | 0           | 1             | 1        |
| 0           | 1           | 1             | 0        |
| ⋮           | ⋮           | ⋮             | ⋮        |
| 0           | 1           | 1             | 0        |



| Ad Exposure | Attitude  |     |
|-------------|---|-----|
| No          |  | 60% |
| Yes         |  | 45% |



-15%

# Introductory Example

However, grouping the survey data by Gender reveals:

| Ad Exposure | Nationality | Website Visit | Attitude |
|-------------|-------------|---------------|----------|
| 0           | 1           | 0             | 0        |
| 0           | 0           | 1             | 1        |
| 0           | 1           | 0             | 0        |
| 0           | 0           | 0             | 0        |
| 1           | 1           | 0             | 1        |
| 1           | 1           | 0             | 0        |
| 1           | 0           | 1             | 1        |
| 0           | 1           | 1             | 0        |
| ⋮           | ⋮           | ⋮             | ⋮        |
| 0           | 1           | 1             | 0        |

| Nationality | Ad Exposure | Attitude |
|-------------|-------------|----------|
| German      | No          | 30%      |
|             | Yes         | 35%      |
| Other       | No          | 70%      |
|             | Yes         | 75%      |

+5%

# Introductory Example

How is this possible?

| Ad Exposure | Attitude                   |
|-------------|----------------------------|
| No          | <div><div></div></div> 60% |
| Yes         | <div><div></div></div> 45% |

| Nationality | Ad Exposure | Attitude                   |
|-------------|-------------|----------------------------|
| German      | No          | <div><div></div></div> 30% |
|             | Yes         | <div><div></div></div> 35% |
| Other       | No          | <div><div></div></div> 70% |
|             | Yes         | <div><div></div></div> 75% |



## Simpson's Paradox



Simpson's paradox is a phenomenon in probability and statistics, in which an effect appears in subgroups of data but disappears or reverses when these groups are combined.



# Introductory Example

Grouping the data by Website Visit shows:

| Ad Exposure | Nationality | Website Visit | Attitude |
|-------------|-------------|---------------|----------|
| 0           | 1           | 0             | 0        |
| 0           | 0           | 1             | 1        |
| 0           | 1           | 0             | 0        |
| 0           | 0           | 0             | 0        |
| 1           | 1           | 0             | 1        |
| 1           | 1           | 0             | 0        |
| 1           | 0           | 1             | 1        |
| 0           | 1           | 1             | 0        |
| ⋮           | ⋮           | ⋮             | ⋮        |
| 0           | 1           | 1             | 0        |

| Website Visit | Ad Exposure | Attitude                   |
|---------------|-------------|----------------------------|
| No            | No          | <div><div></div></div> 60% |
|               | Yes         | <div><div></div></div> 50% |
| Yes           | No          | <div><div></div></div> 60% |
|               | Yes         | <div><div></div></div> 30% |

-10%

-30%

# Introductory Example

Finally, grouping the data by Gender and Test Drive reveals:

| Ad Exposure | Nationality | Website Visit | Attitude |
|-------------|-------------|---------------|----------|
| 0           | 1           | 0             | 0        |
| 0           | 0           | 1             | 1        |
| 0           | 1           | 0             | 0        |
| 0           | 0           | 0             | 0        |
| 1           | 1           | 0             | 1        |
| 1           | 1           | 0             | 0        |
| 1           | 0           | 1             | 1        |
| 0           | 1           | 1             | 0        |
| ⋮           | ⋮           | ⋮             | ⋮        |
| 0           | 1           | 1             | 0        |



| Website Visit | Nationality | Ad Exposure | Attitude                   |
|---------------|-------------|-------------|----------------------------|
| No            | German      | No          | <div><div></div></div> 30% |
|               |             | Yes         | <div><div></div></div> 40% |
|               | Other       | No          | <div><div></div></div> 70% |
|               |             | Yes         | <div><div></div></div> 80% |
| Yes           | German      | No          | <div><div></div></div> 30% |
|               |             | Yes         | <div><div></div></div> 20% |
|               | Other       | No          | <div><div></div></div> 70% |
|               |             | Yes         | <div><div></div></div> 60% |



# So, what's the advertising effect?

| Website Visit | Nationality | Ad Exposure | Attitude |
|---------------|-------------|-------------|----------|
| No            | German      | No          | 30%      |
|               |             | Yes         | 40%      |
|               | Other       | No          | 70%      |
|               |             | Yes         | 80%      |
| Yes           | German      | No          | 30%      |
|               |             | Yes         | 20%      |
|               | Other       | No          | 70%      |
|               |             | Yes         | 60%      |

$\approx 0$

| Nationality | Ad Exposure | Attitude |
|-------------|-------------|----------|
| German      | No          | 30%      |
|             | Yes         | 35%      |
| Other       | No          | 70%      |
|             | Yes         | 75%      |

+0.05

| Website Visit | Ad Exposure | Attitude |
|---------------|-------------|----------|
| No            | No          | 60%      |
|               | Yes         | 50%      |
| Yes           | No          | 60%      |
|               | Yes         | 30%      |

-0.2

| Ad Exposure | Attitude |
|-------------|----------|
| No          | 60%      |
| Yes         | 45%      |

-0.15



RUSSELL GLASS · SEAN CALLAHAN

THE

BIG DATA  
DRIVEN

BUSINESS

DATA  
DRIVEN



Data-Driven

Decision-Making

O'REILL

Data  
Driven

Creating a Data Culture

5 Steps To Powering  
Data Driven Decision Making

increasing sales with  
DATA - DRIVEN  
MARKETING



loginradius

DATA-DRIVEN  
FORTUNE 500

decisions in a



Data  
driven  
decisions



GET #DATADRIVEN

Data-Driven  
Marketing

THE DATA-DRIVEN  
FUTURE

with



+



Data Driven  
Business



# Observational vs. Causal Inference

## Observational Inference (Prediction)

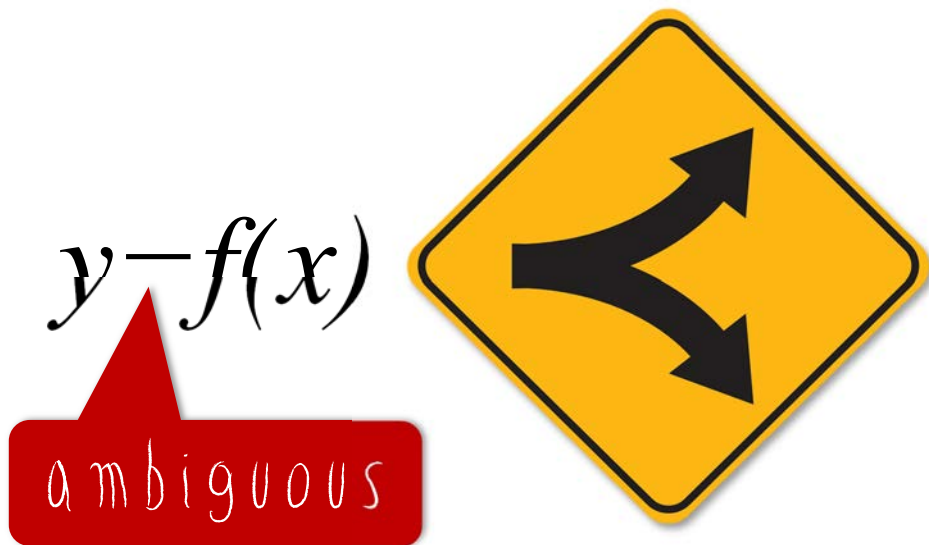
$$y = f(\textit{see}(x))$$

“given that I **see**”

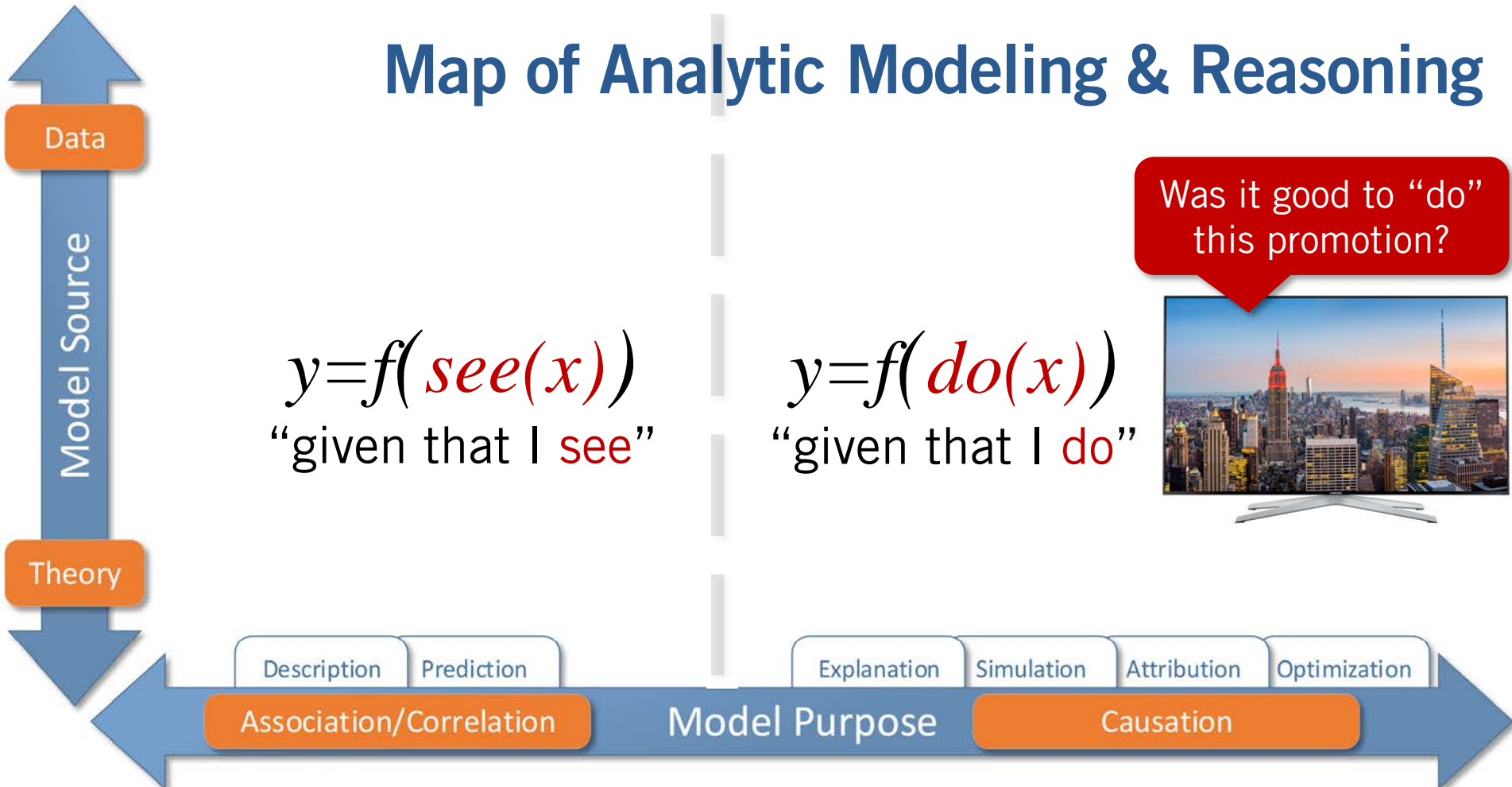
## Causal Inference (Intervention)

$$y = f(\textit{do}(x))$$

“given that I **do**”



# Map of Analytic Modeling & Reasoning



# So, what's the advertising effect?

"given that I see"

| Website Visit | Nationality | Ad Exposure | Attitude |
|---------------|-------------|-------------|----------|
| No            | German      | No          | 30%      |
|               |             | Yes         | 40%      |
|               | Other       | No          | 70%      |
|               |             | Yes         | 80%      |
| Yes           | German      | No          | 30%      |
|               |             | Yes         | 20%      |
|               | Other       | No          | 70%      |
|               |             | Yes         | 60%      |

$\approx 0$

"given that I see"

| Website Visit | Ad Exposure | Attitude |
|---------------|-------------|----------|
| No            | No          | 60%      |
| Yes           | No          | 50%      |
|               | Yes         | 30%      |

$-0.2$

"given that I see"

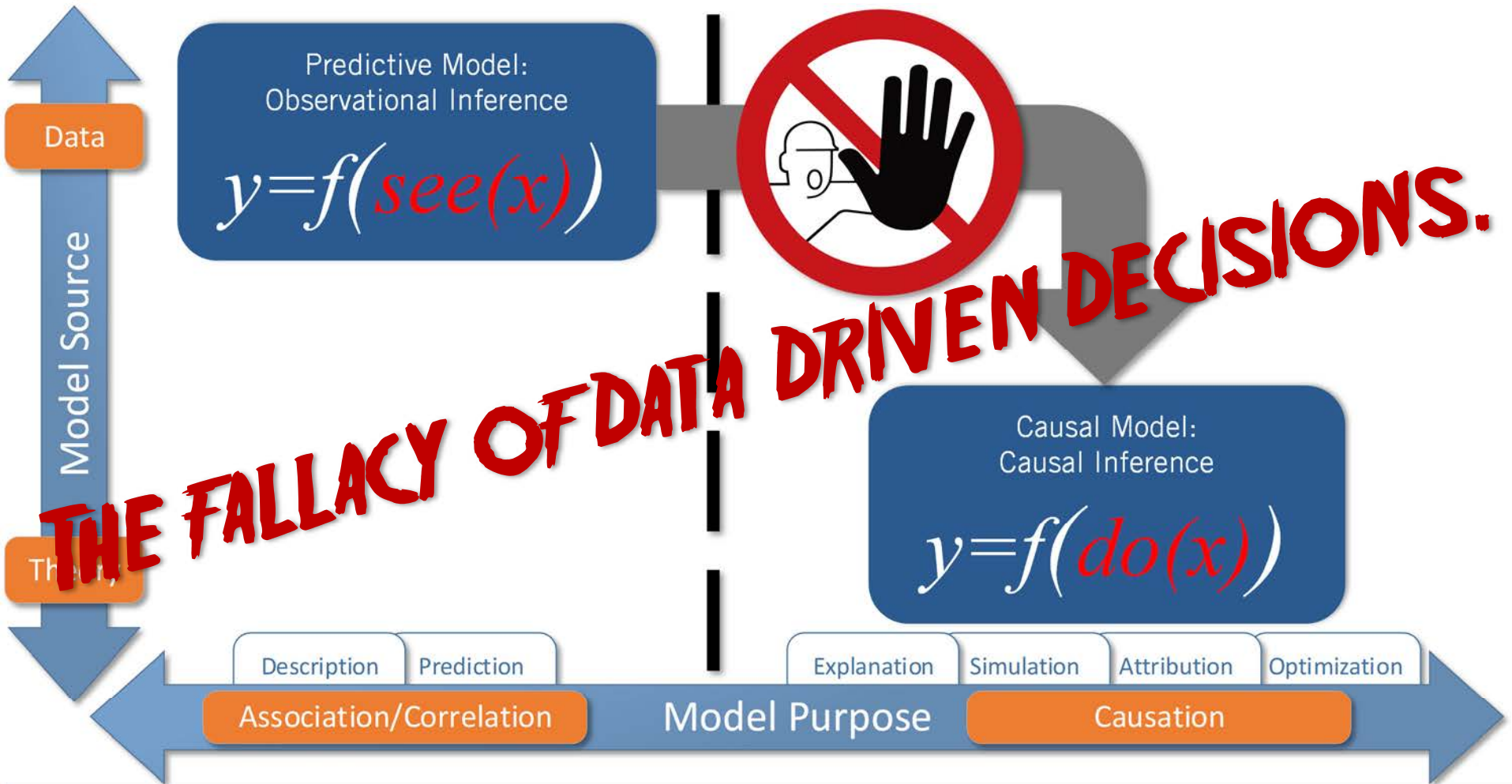
| Nationality | Ad Exposure | Attitude |
|-------------|-------------|----------|
| German      | No          | 30%      |
|             | Yes         | 35%      |
| Other       | No          | 70%      |
|             | Yes         | 75%      |

$+0.05$

| Ad Exposure | Attitude |
|-------------|----------|
| No          | 60%      |
| Yes         | 45%      |

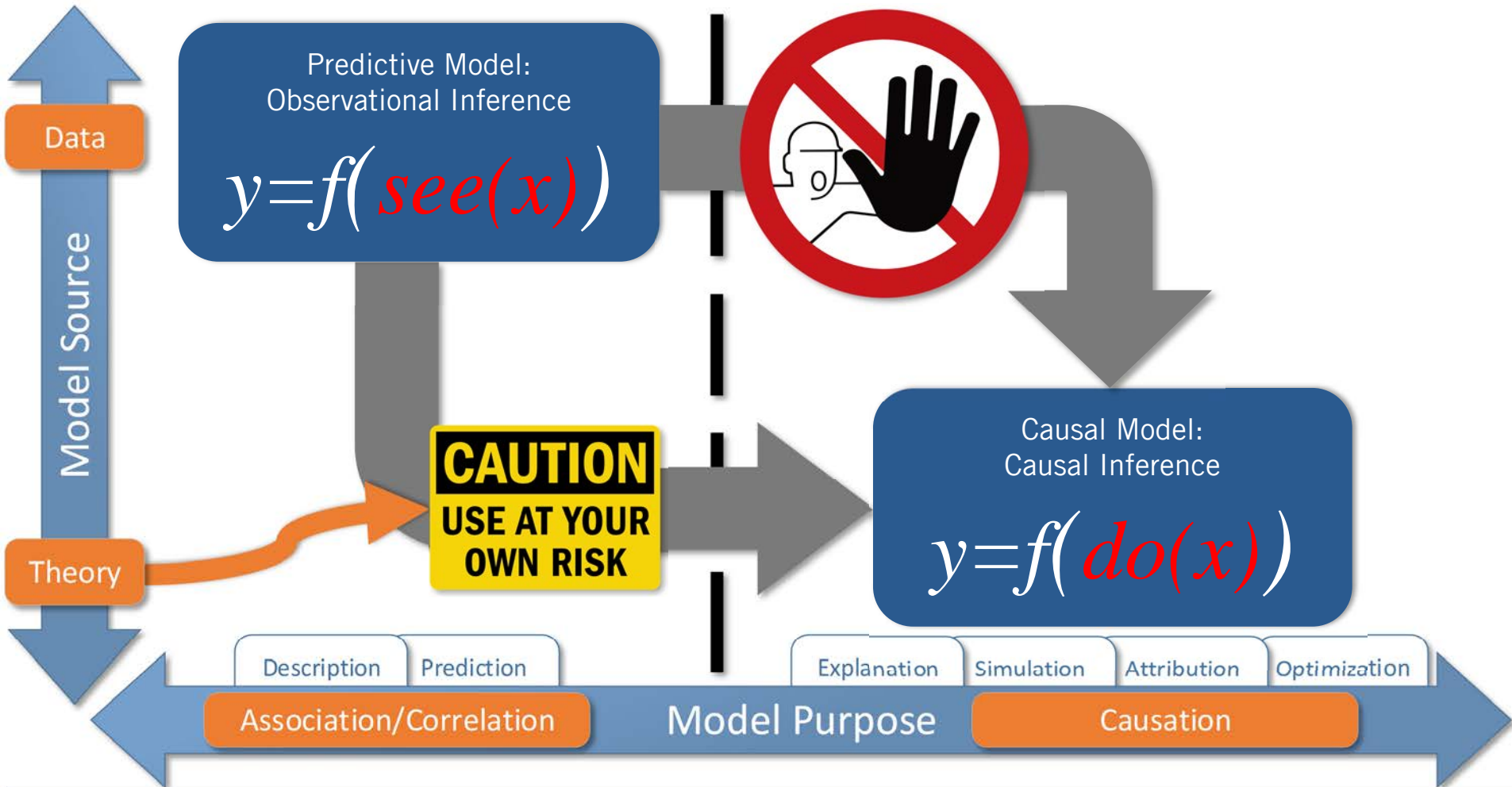
$-0.15$

"given that I see"

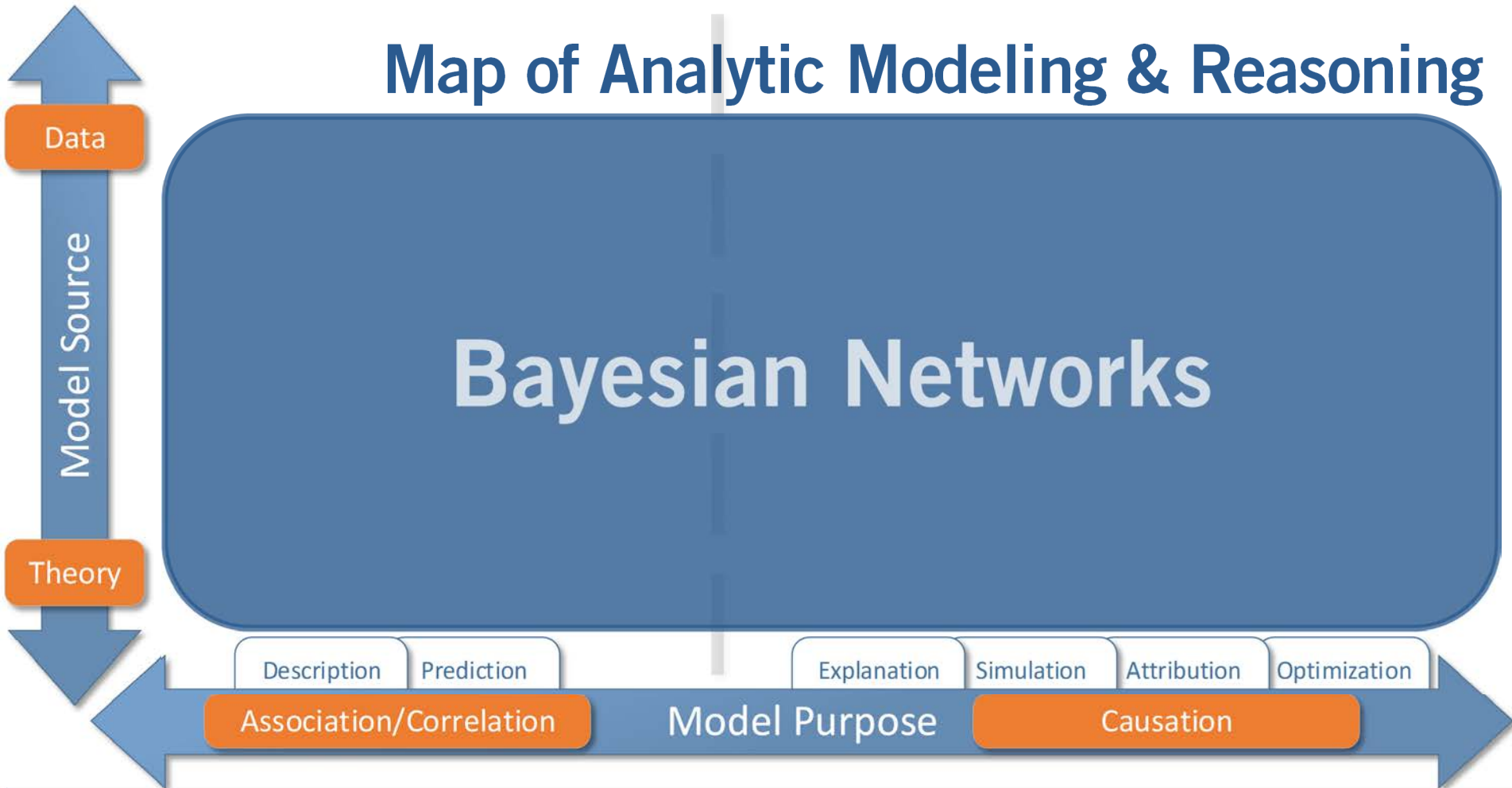




*Once upon a time. . .*



# Map of Analytic Modeling & Reasoning



# Introductory Example

**Develop Theory**

What's the story here?

  
**Nationality**

  
**Ad Exposure**



  
**Website Visit**

  
**Attitude**

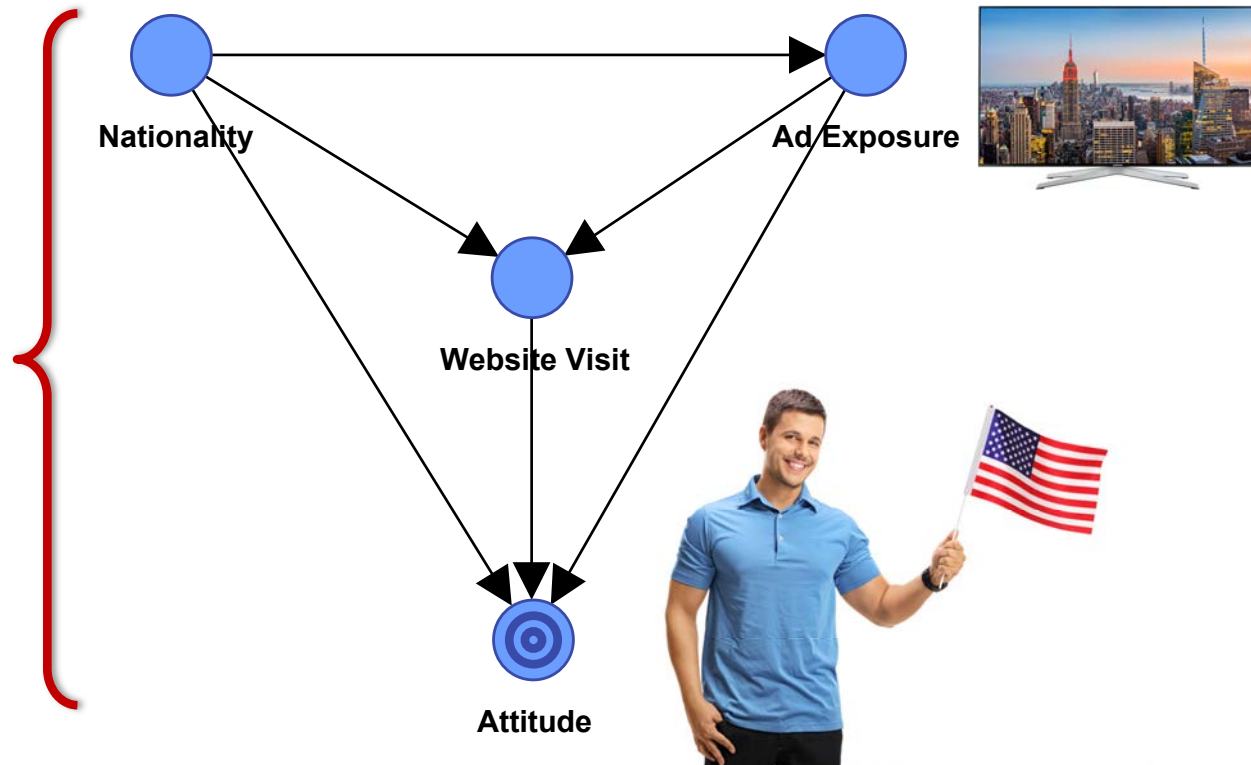




# Introductory Example

## Our Theory!

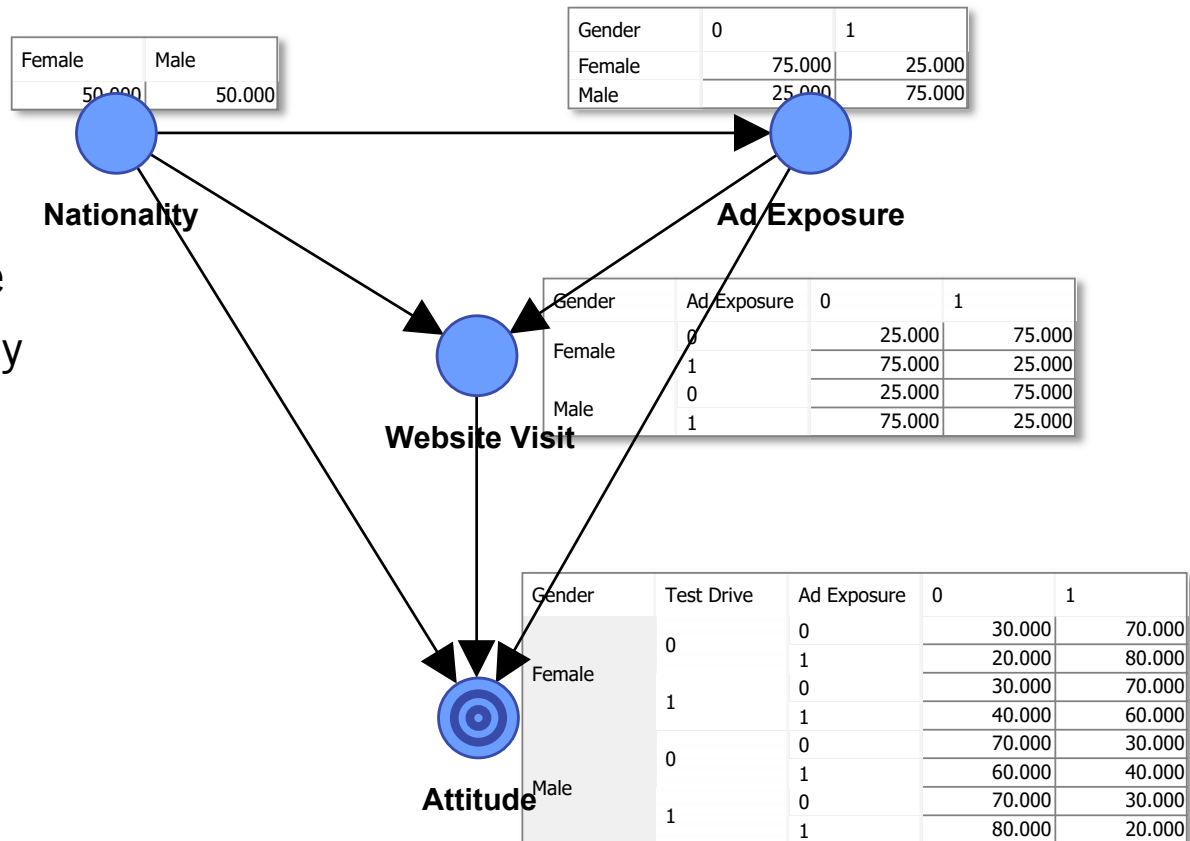
That's the story! Now we have the qualitative part of a causal Bayesian network.



# Introductory Example

## “Parameters”

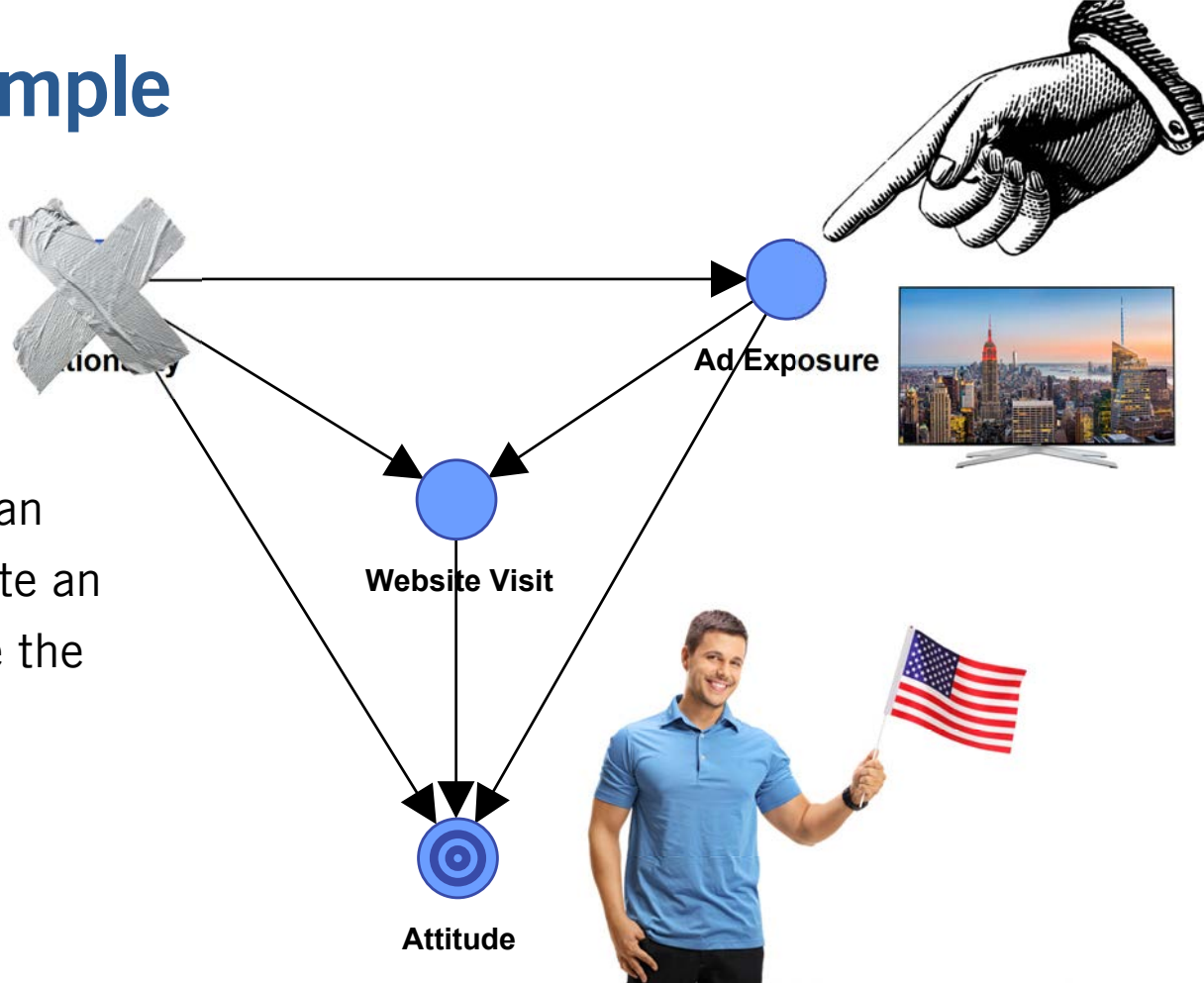
- We can estimate the quantitative part of the network from the survey data.
- As a result, we have a Bayesian network, which we can use for inference.



# Introductory Example

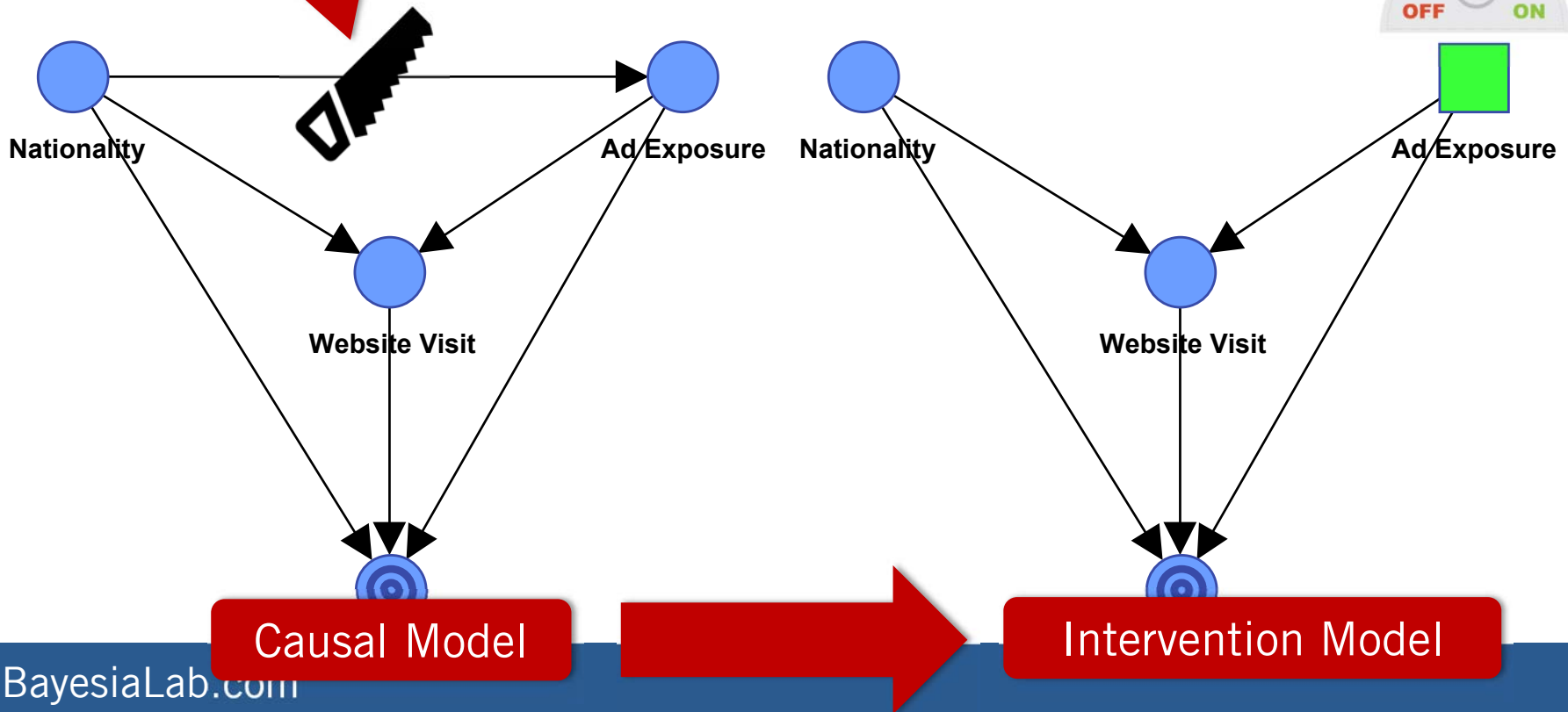
## Our “Model of the World”

- How can we obtain the effect of Ad Exposure?
- With this causal Bayesian network, we can simulate an intervention to estimate the causal effect.



# Introductory Example

Causal Model **“Graph Surgery”** Intervening an Intervention

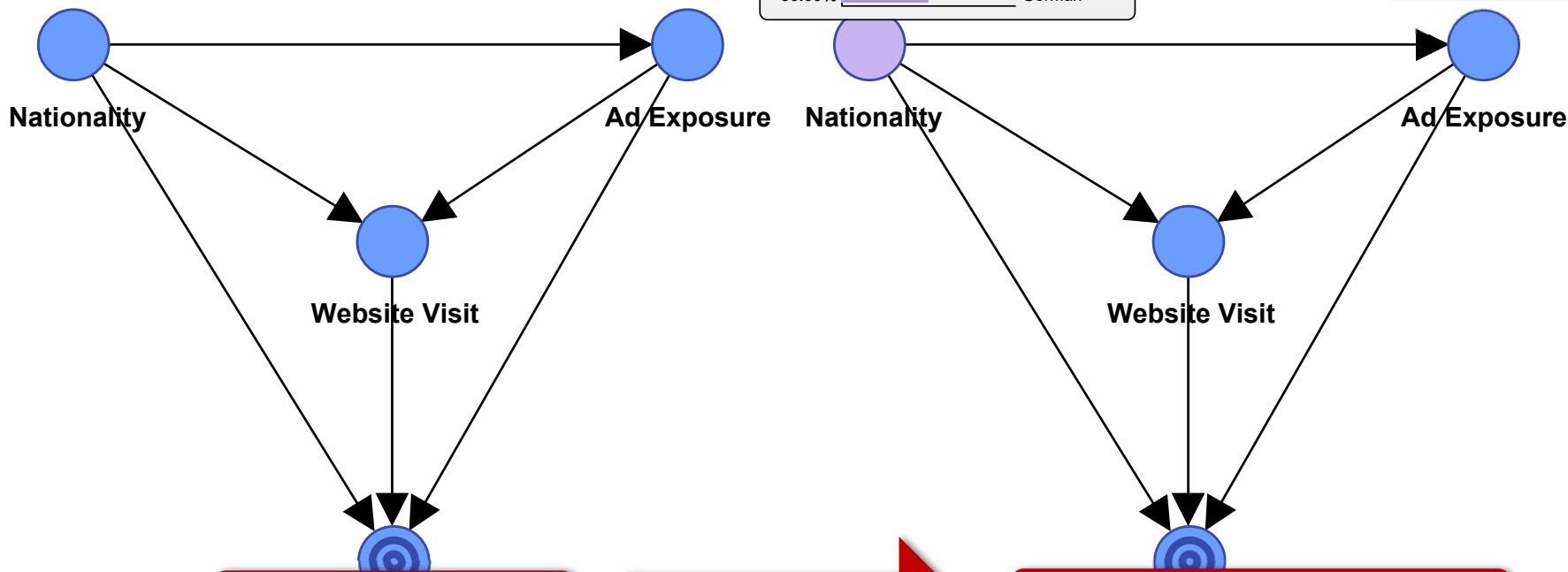
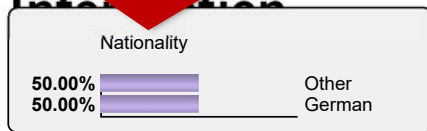




# Introductory Example

Causal Inference: Simulating an Intervention

Fix Probabilities with Likelihood Matching

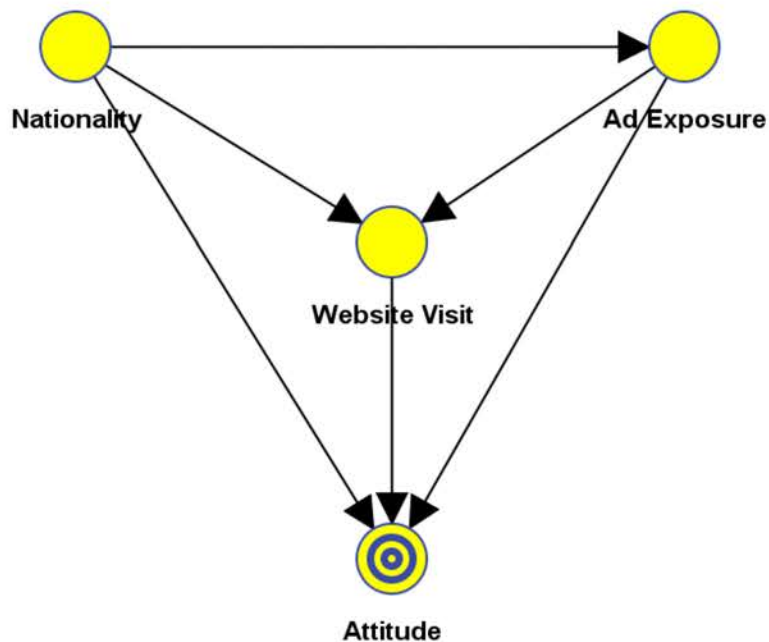


Causal Model

Intervention Model



Simpsons.xbl \*



Joint Probability: 100.00%

Log-Loss: 0

Cases: 1,000

Total Value: 1.522

Mean Value: 0.507

Nationality

47.60%

52.40%

Intervention Node

German

Ad Exposure

Mean: 0.512 Dev: 0.500

Value: 0.512

48.80%

51.20%

0

1

Website Visit

Mean: 0.494 Dev: 0.500

Value: 0.494

50.60%

49.40%

0

1

Attitude

Mean: 0.516 Dev: 0.500

Value: 0.516

48.40%

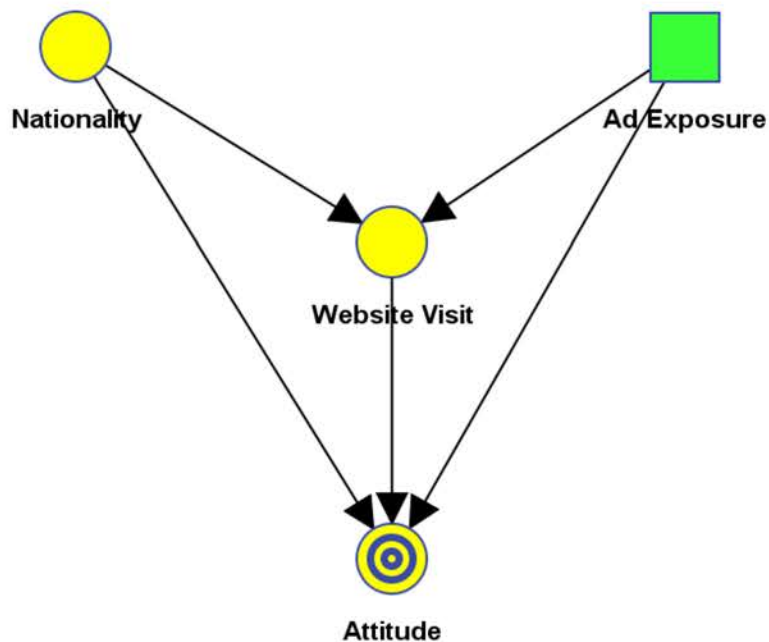
51.60%

0

1



Simpsons.xbl \*



Joint Probability: 48.80%  
Log-Loss: 1.04  
Cases: 488.01  
Total Value: 1.240  
Mean Value: 0.413

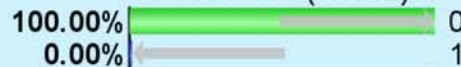
Nationality



Intervention

Ad Exposure

Mean: 0.000 Dev: 0.000  
Value: 0.000 (-0.512)



Website Visit

Mean: 0.750 Dev: 0.433  
Value: 0.750 (+0.256)



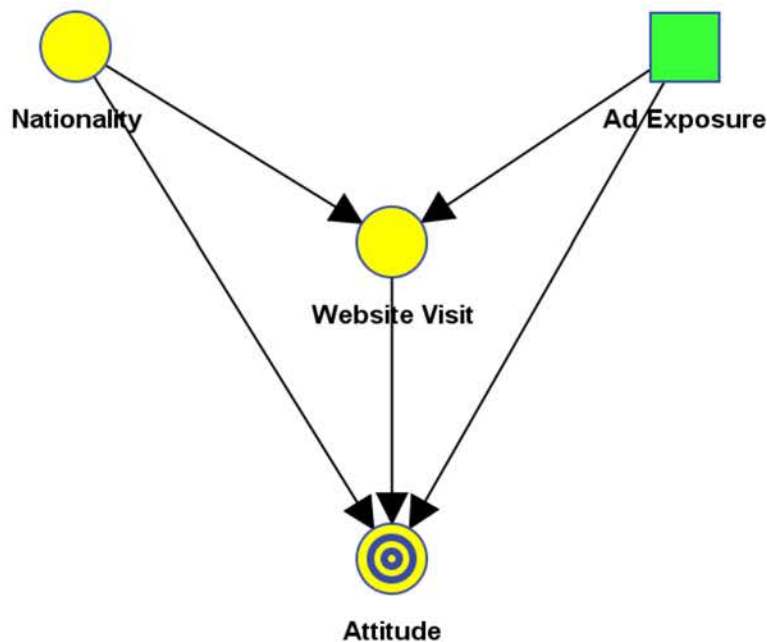
Attitude

Mean: 0.490 Dev: 0.500  
Value: 0.490 (-0.026)





Simpsons.xbl \*



Joint Probability: 51.20%  
Log-Loss: 0.97  
Cases: 511.99  
Total Value: 1.790  
Mean Value: 0.597

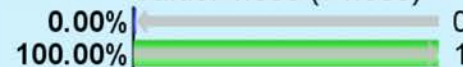
Nationality



Intervention

Ad Exposure

Mean: 1.000 Dev: 0.000  
Value: 1.000 (+1.000)



Website Visit

Mean: 0.250 Dev: 0.433  
Value: 0.250 (-0.500)



Effect

Attitude

Mean: 0.540 Dev: 0.498  
Value: 0.540 (+0.050)



# So, what's the advertising effect?

| Website Visit | Nationality | Ad Exposure | Attitude |
|---------------|-------------|-------------|----------|
| No            | German      | No          | 30%      |
|               |             | Yes         | 40%      |
|               | Other       | No          | 70%      |
|               |             | Yes         | 80%      |
| Yes           | German      | No          | 30%      |
|               |             | Yes         | 20%      |
|               | Other       | No          | 70%      |
|               |             | Yes         | 60%      |

$\approx 0$

| Website Visit | Ad Exposure | Attitude |
|---------------|-------------|----------|
| No            | No          | 60%      |
|               | Yes         | 50%      |
| Yes           | No          | 60%      |
|               | Yes         | 30%      |

$-0.2$

| Nationality | Ad Exposure | Attitude |
|-------------|-------------|----------|
| German      | No          | 30%      |
|             | Yes         | 35%      |
| Other       | No          | 70%      |
|             | Yes         | 75%      |

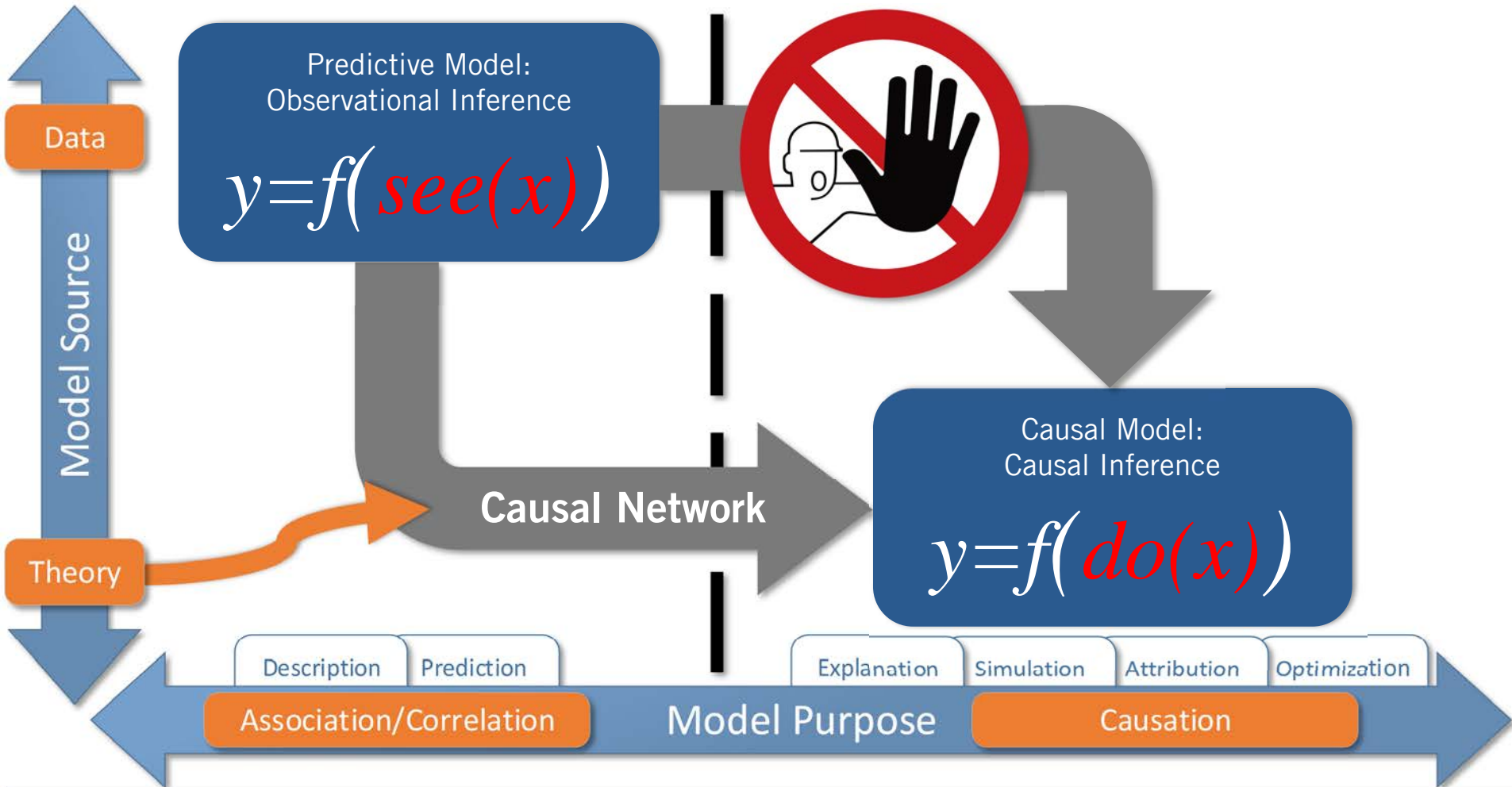
$+0.05$

| Ad Exposure | Attitude |
|-------------|----------|
| No          | 60%      |
| Yes         | 45%      |

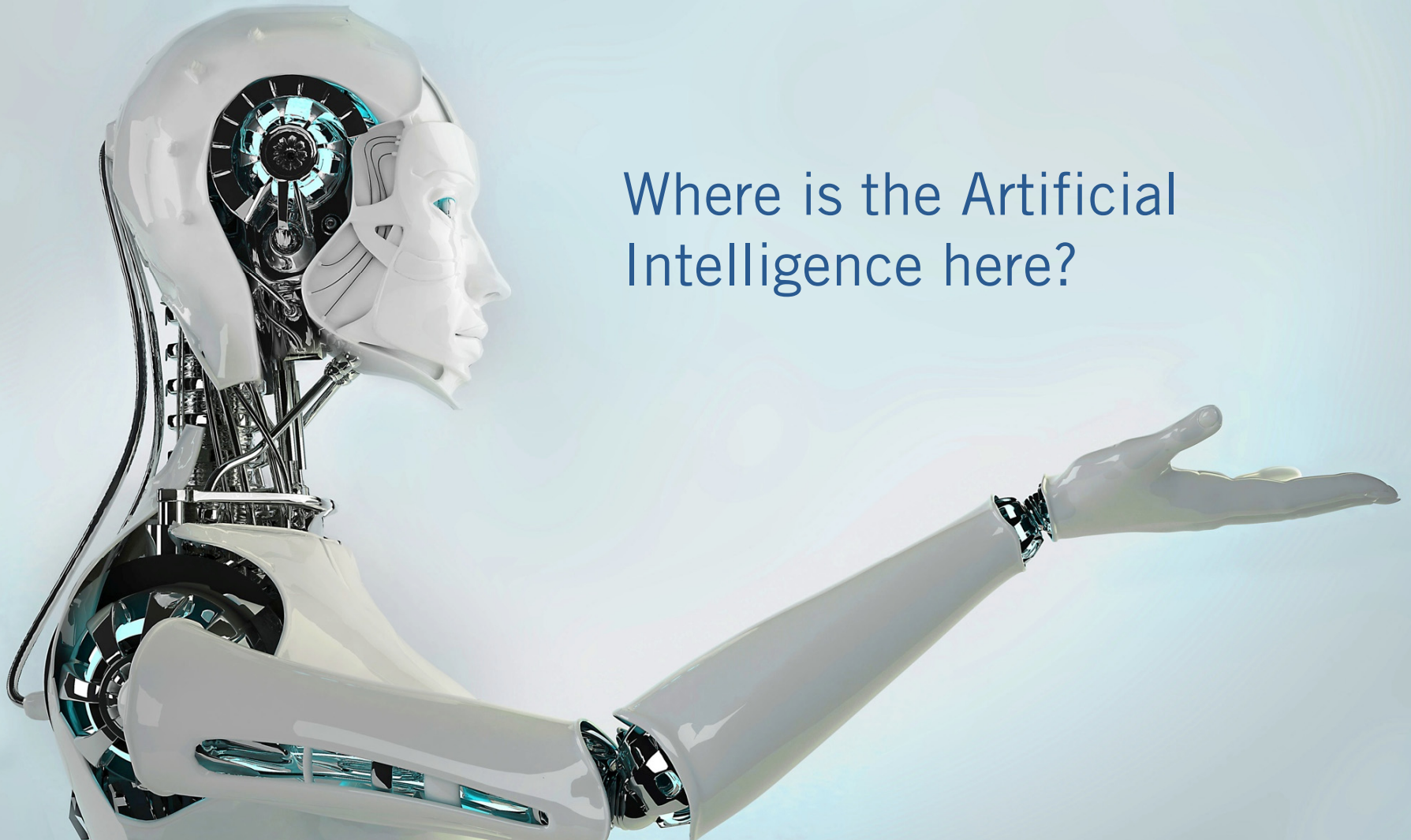
$-0.15$







Where is the Artificial  
Intelligence here?



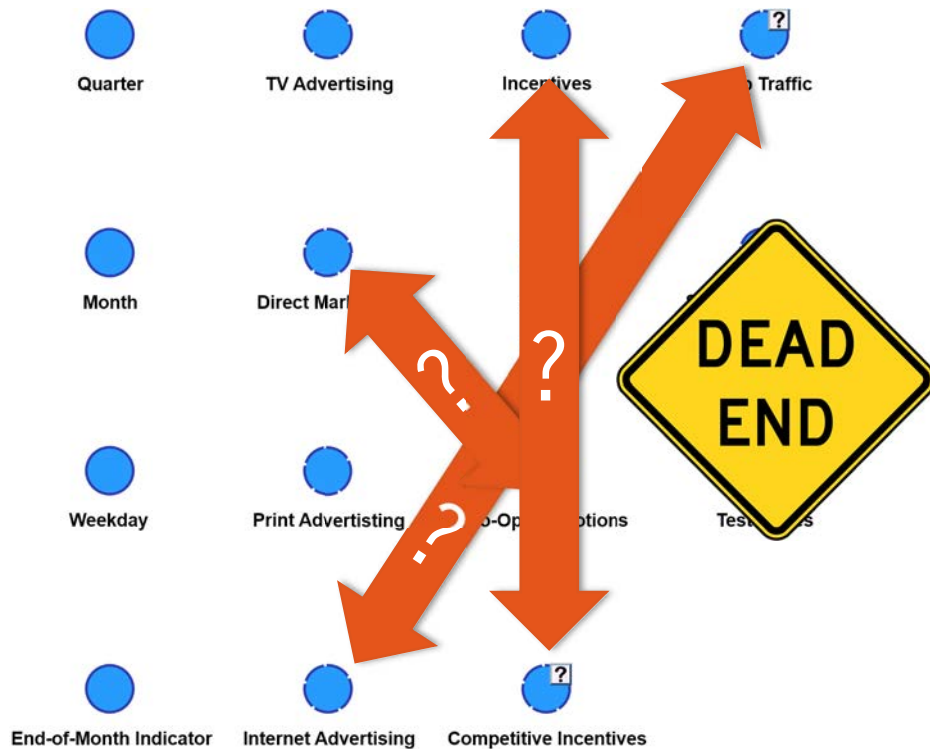
No Artificial Intelligence. Here,  
we need human intelligence!



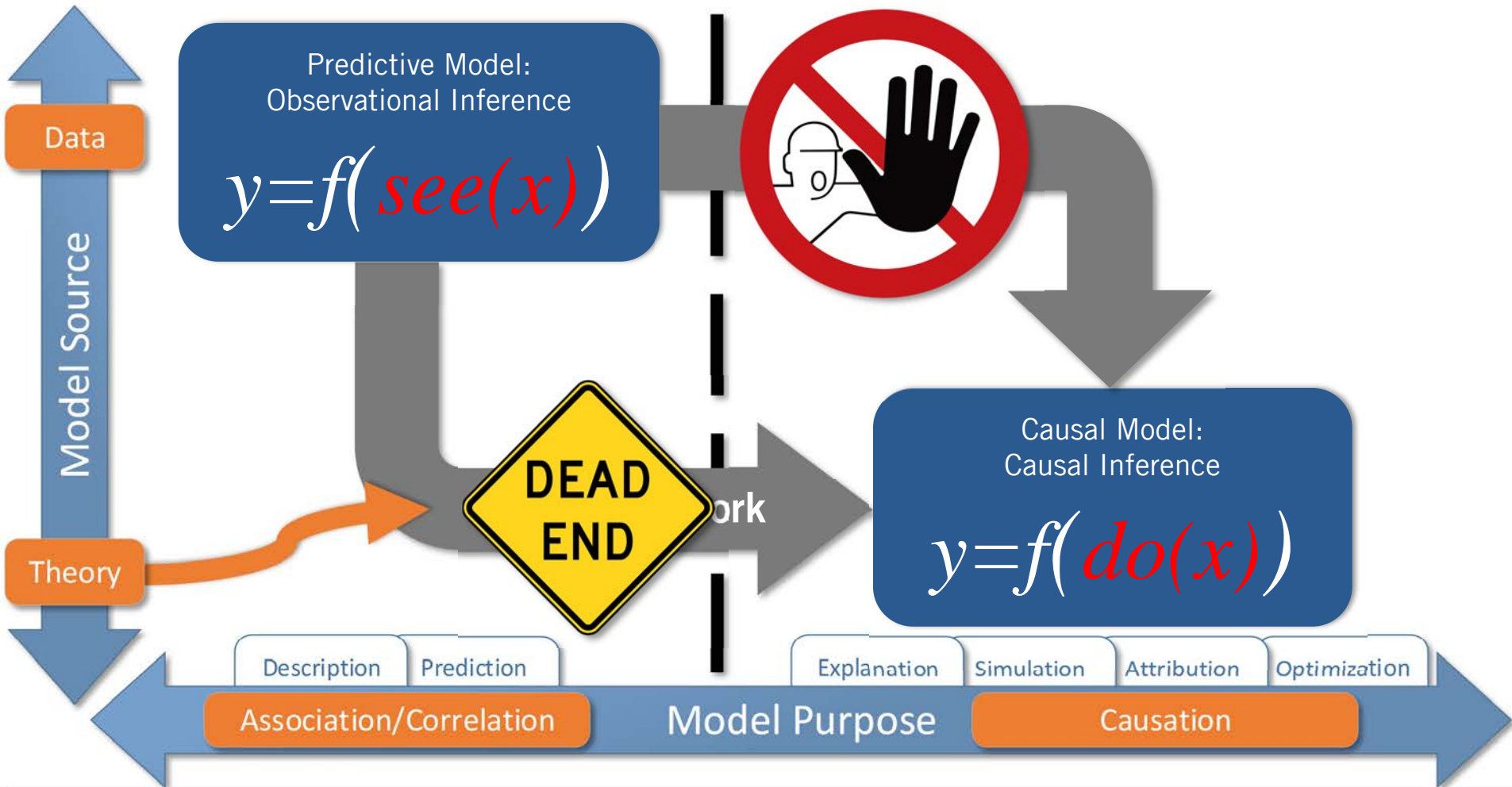
# Resource Allocation Optimization

## Causal Assumptions?

- Recall: Causal inference requires causal assumptions, e.g., a causal networks!
- But, given the number of variables, there are  $2.38 \times 10^{41}$  possible causal network graphs!
- Causal directions are not always obvious.










Now What?

**We need a different  
kind of theory** 

# Disjunctive Cause Criterion



NIH Public Access

Author Manuscript

*Biometrics*. Author manuscript; available in PMC 2012 December 1.

Published in final edited form as:

*Biometrics*. 2011 December ; 67(4): 1406–1413. doi:10.1111/j.1541-0420.2011.01619.x.

## A new criterion for confounder selection

**Tyler J. VanderWeele** and

Departments of Epidemiology and Biostatistics, Harvard School of Public Health 677 Huntington Avenue, Boston, MA 02115, Phone: 617-432-7855; Fax: 617-4321884

**Ilya Shpitser**

Department of Epidemiology, Harvard School of Public Health 677 Huntington Avenue, Boston, MA 02115

Tyler J. VanderWeele: tvanderw@hsph.harvard.edu

## Abstract

We propose a new criterion for confounder selection when the underlying causal structure is unknown and only limited knowledge is available. We assume all covariates being considered are pretreatment variables and that for each covariate it is known (i) whether the covariate is a cause of treatment, and (ii) whether the covariate is a cause of the outcome. The causal relationships the covariates have with one another is assumed unknown. We propose that control be made for any covariate that is either a cause of treatment or of the outcome or both. We show that irrespective of the actual underlying causal structure, if any subset of the observed covariates suffices to control

# Disjunctive Cause Criterion

## VanderWeele and Shpitser (2011)

- “We propose that control be made for any [pre-treatment] **covariate** that is either a cause of **treatment** or of the **outcome** or both.”

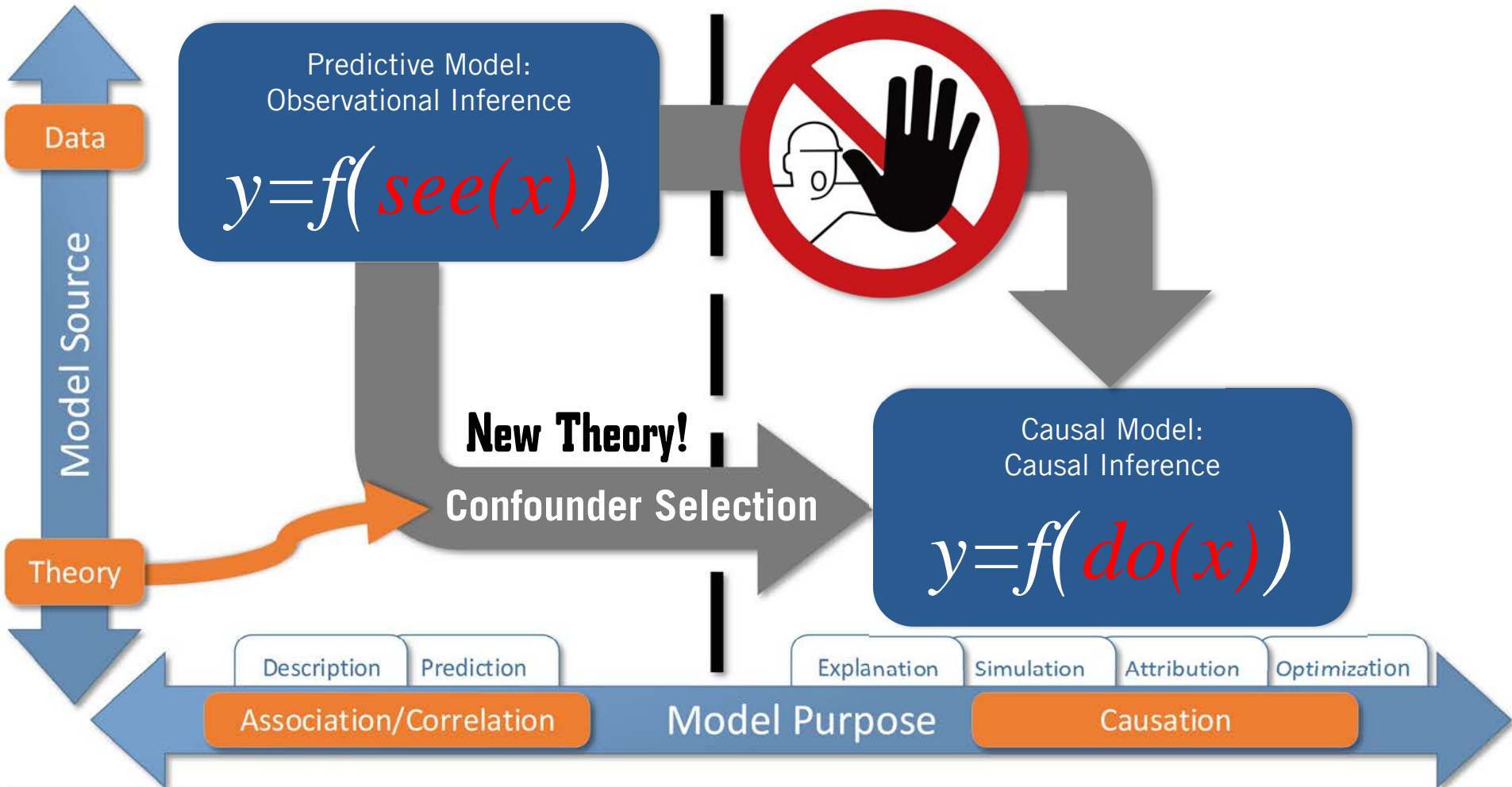
Confounder

Advertisement

Sales

Implementation in BayesiaLab:  
Likelihood Matching on Confounders in  
**Direct Effects Analysis**  
→ Causal Effect, i.e., the Advertising Effect

**IMPORTANT ASSUMPTION:  
NO UNOBSERVED CONFOUNDERS**



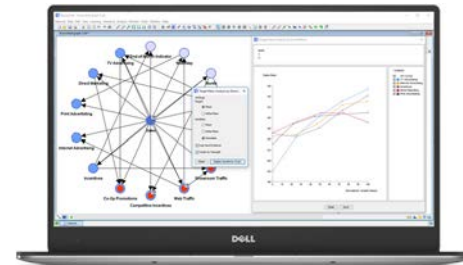
# Resource Allocation Optimization



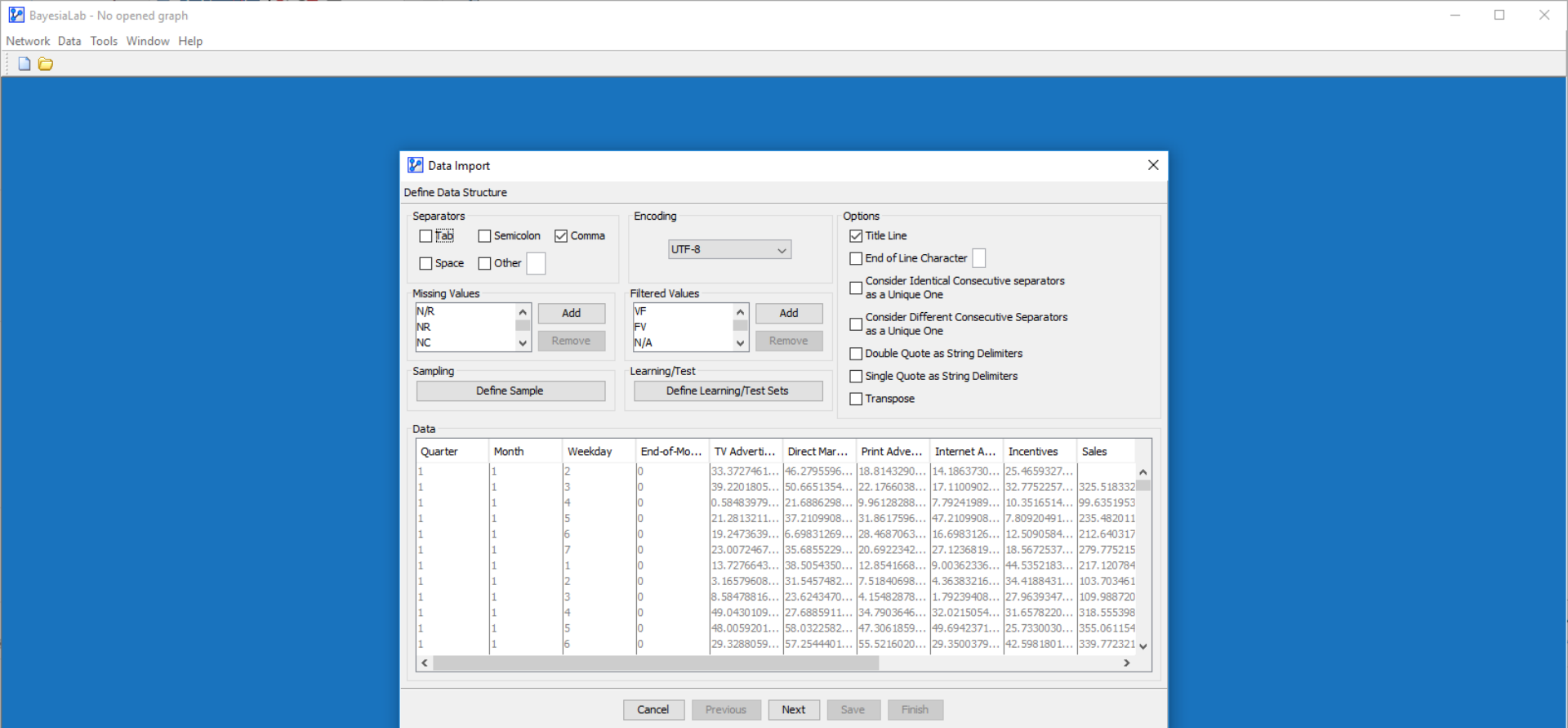
All Data is Synthetic

## Proposed Workflow

- Import historical sales and marketing data.
- Machine-learn a predictive model with BayesiaLab.
- Determine **Confounders** vs. **Non-Confounders**, using the **Disjunctive Cause Criterion**.
- Estimate and evaluate **Direct Effects** response curves.
- Introduce **Function Node** and assign media costs.
- Perform **Genetic Target Optimization**.
- Apply **Network Temporalization**.
- Add **Constraint Nodes** between  $t$  and  $t-1$  marketing variables.
- Perform **Genetic Target Optimization** on dynamic network.







# Data Import Wizard

**Data Import**

Define Variable Type

Type

☐ Not Distributed  
☒ Discrete  
☐ Continuous  
☐ Weight  
☐ Learning/Test  
☐ Row Identifier

Action

Information

|                 |       |         |
|-----------------|-------|---------|
| Number of Rows  | 16801 | 100.00% |
| Not Distributed | 0     | 0.00%   |
| Discrete        | 4     | 26.67%  |
| Continuous      | 11    | 73.33%  |
| Others          | 0     | 0.00%   |
| Missing Values  | 6     | 0.00%   |
| Filtered Values | 0     | 0.00%   |

Data

| Quarter | Month | Weekday | End-of-Mo... | TV Adverti... | Direct Mar... | Print Adve... | Internet A... | Incentives    | Sales         |
|---------|-------|---------|--------------|---------------|---------------|---------------|---------------|---------------|---------------|
| 1       | 1     | 2       | 0            | 33.3727461... | 46.2795596... | 18.8143290... | 14.1863730... | 25.4659327... | 325.518332    |
| 1       | 1     | 3       | 0            | 39.2201805... | 50.6651354... | 22.1766038... | 17.1100902... | 32.7752257... | 99.6351953    |
| 1       | 1     | 4       | 0            | 0.58483979... | 21.6886298... | 9.96128288... | 7.79241989... | 10.3516514... | 235.482011    |
| 1       | 1     | 5       | 0            | 21.2813211... | 37.2109908... | 31.8617596... | 47.2109908... | 7.80920491... | 1212.640317   |
| 1       | 1     | 6       | 0            | 19.2473639... | 6.69831269... | 28.4687063... | 16.6983126... | 12.5090584... | 279.775215    |
| 1       | 1     | 7       | 0            | 23.0072467... | 35.6855229... | 20.6922342... | 27.1236819... | 18.5672537... | 217.120784    |
| 1       | 1     | 1       | 0            | 13.7276643... | 38.5054350... | 12.8541668... | 9.00362336... | 44.5352183... | 103.703461    |
| 1       | 1     | 2       | 0            | 3.16579608... | 31.5457482... | 7.51840698... | 4.36383216... | 34.4188431... | 27.9639347... |
| 1       | 1     | 3       | 0            | 8.58478816... | 23.6243470... | 4.15482878... | 1.79239408... | 27.9639347... | 318.555398    |
| 1       | 1     | 4       | 0            | 49.0430109... | 27.6885911... | 34.7903646... | 32.0215054... | 31.6578220... | 355.061154    |
| 1       | 1     | 5       | 0            | 48.0059201... | 58.0322582... | 47.3061859... | 49.6942371... | 25.7330030... | 339.772321    |
| 1       | 1     | 6       | 0            | 29.3288059... | 57.2544401... | 55.5216020... | 29.3500379... | 42.5981801... | 304.693249    |
| 1       | 1     | 7       | 0            | 44.4346604... | 43.2466044... | 10.5580191... | 32.0630377... | 48.8700524... | 287.837859    |
| 1       | 1     | 1       | 0            | 29.1636534... | 54.5759953... | 17.5206372... | 12.6097153... | 36.6784392... |               |

# Variable Type Definition

**Data Import**

Data Selection and Filtering

Missing Value Processing

☐ Filter

☒ OR

☐ AND

☐ Replace by :

☐ Value

☐ Mean/Modal

☐ Infer

☐ Static Imputation

☐ Dynamic Imputation

☒ Structural EM

☐ Entropy-Based Static Imputation

☐ Entropy-Based Dynamic Imputation

Information

|                 |       |         |
|-----------------|-------|---------|
| Number of Rows  | 16801 | 100.00% |
| Not Distributed | 0     | 0.00%   |
| Discrete        | 4     | 26.67%  |
| Continuous      | 11    | 73.33%  |
| Others          | 0     | 0.00%   |
| Missing Values  | 6     | 0.00%   |
| Filtered Values | 0     | 0.00%   |

Select Values

☐ OR

☒ AND

Delete Selections

Display Selections

Data

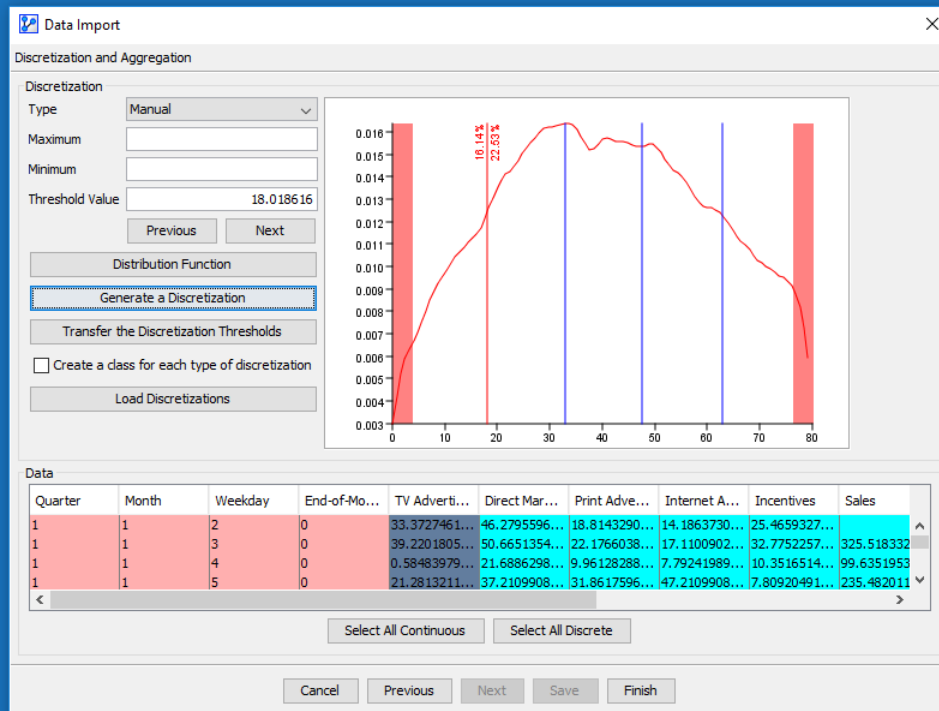
| Quarter | Month | Weekday | End-of... | TV Adv...     | Direct M...   | Print Ad...   | Interne...    | Incentives    | Sales      |
|---------|-------|---------|-----------|---------------|---------------|---------------|---------------|---------------|------------|
| 1       | 1     | 2       | 0         | 33.3727461... | 46.2795596... | 18.8143290... | 14.1863730... | 25.4659327... |            |
| 1       | 1     | 3       | 0         | 39.2201805... | 50.6651354... | 22.1766038... | 17.1100902... | 32.7752257... | 325.518332 |
| 1       | 1     | 4       | 0         | 0.58483979... | 21.6886298... | 9.96128288... | 7.79241989... | 10.3516514... | 99.6351953 |
| 1       | 1     | 5       | 0         | 21.2813211... | 37.2109908... | 31.8617596... | 47.2109908... | 7.80920491... | 235.482011 |
| 1       | 1     | 6       | 0         | 19.2473639... | 6.69831269... | 28.4687063... | 16.6983126... | 12.5090584... | 212.640317 |

Select All Continuous

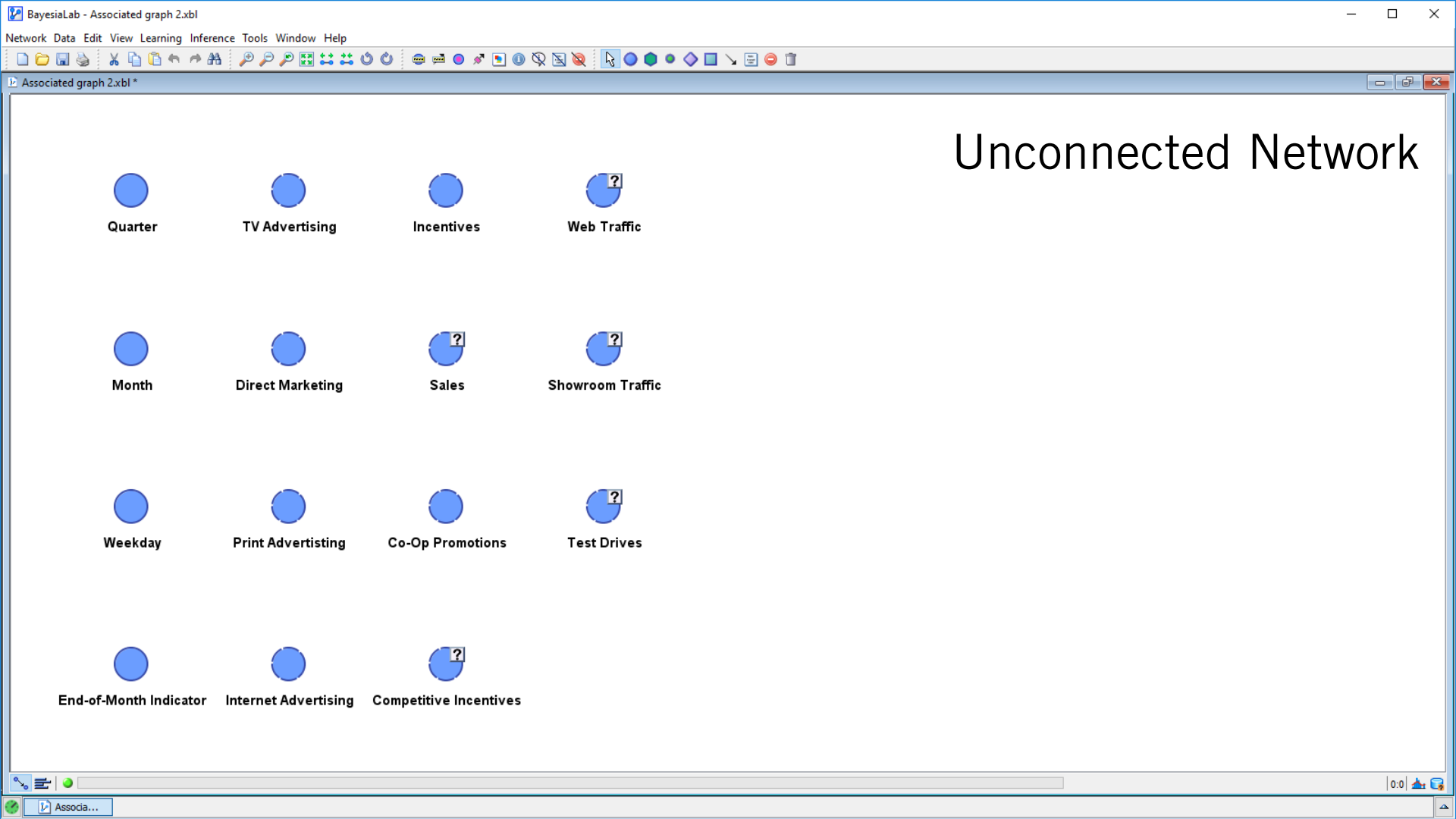
Select All Discrete

Cancel Previous **Next** Save Finish

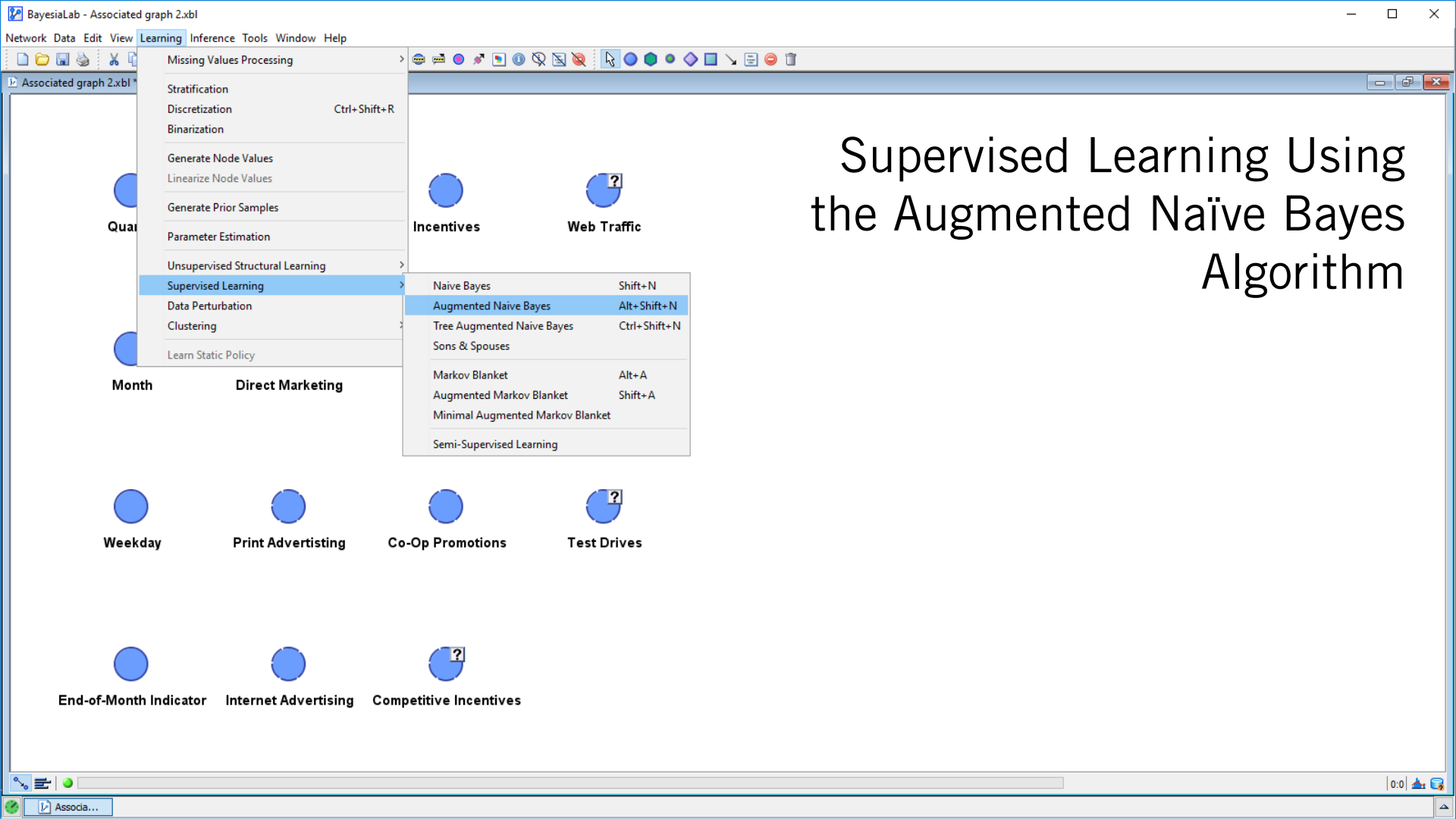
# Missing Values Processing

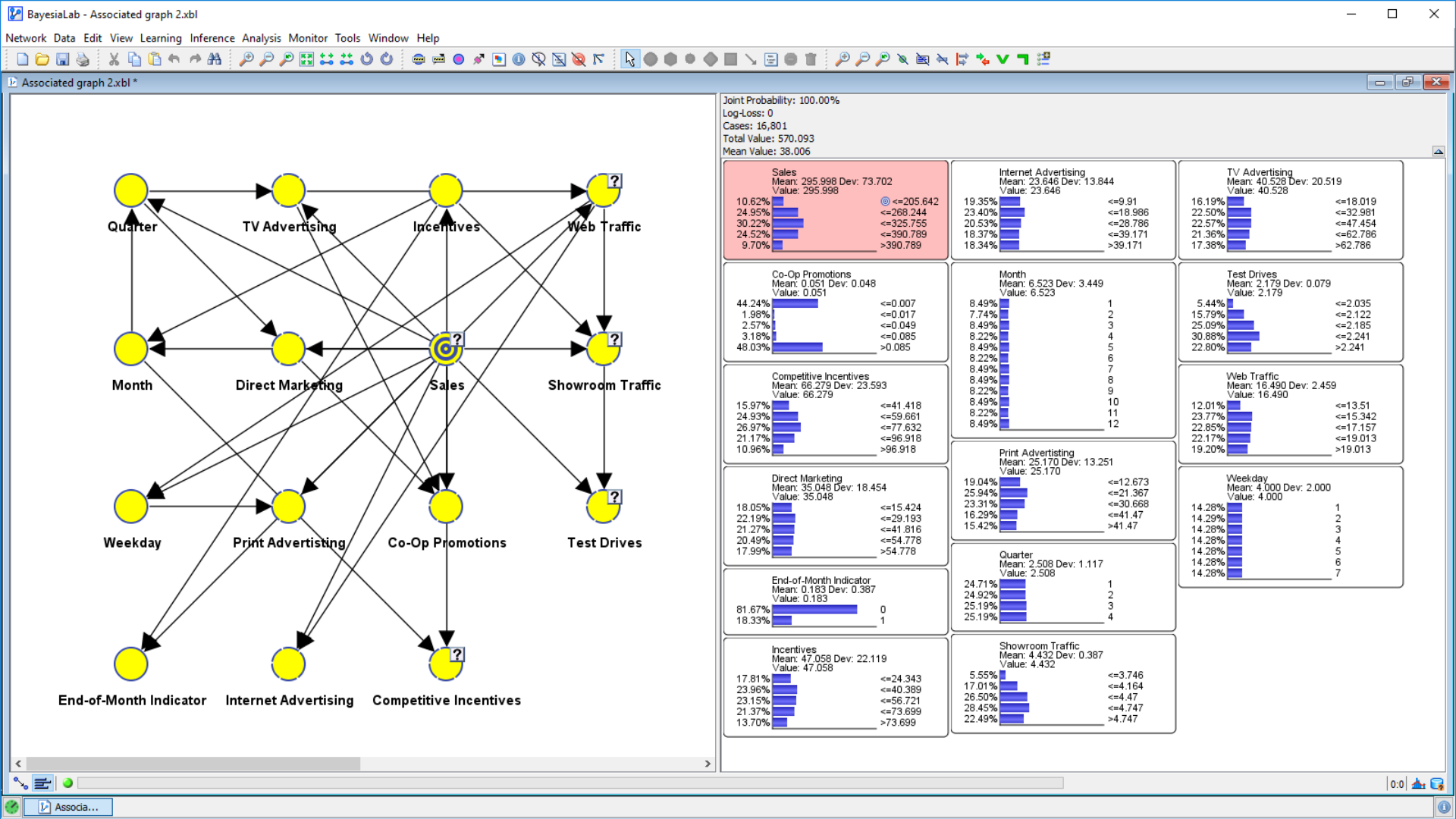


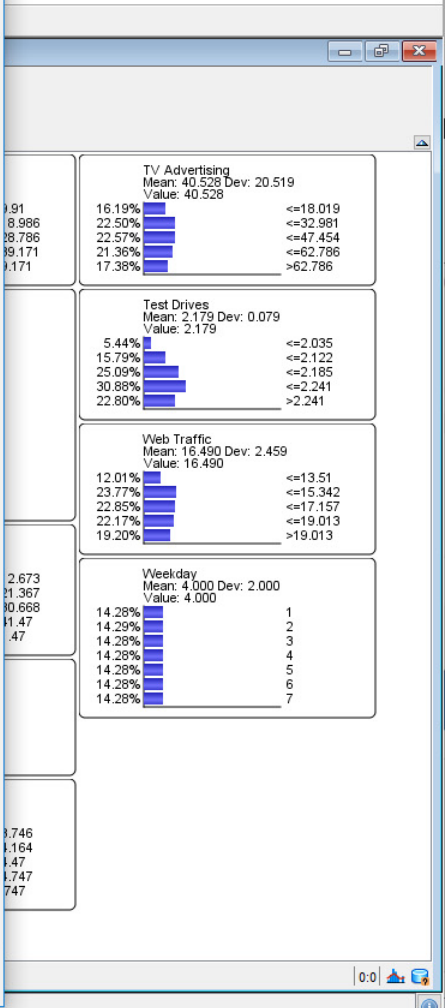
# Discretization

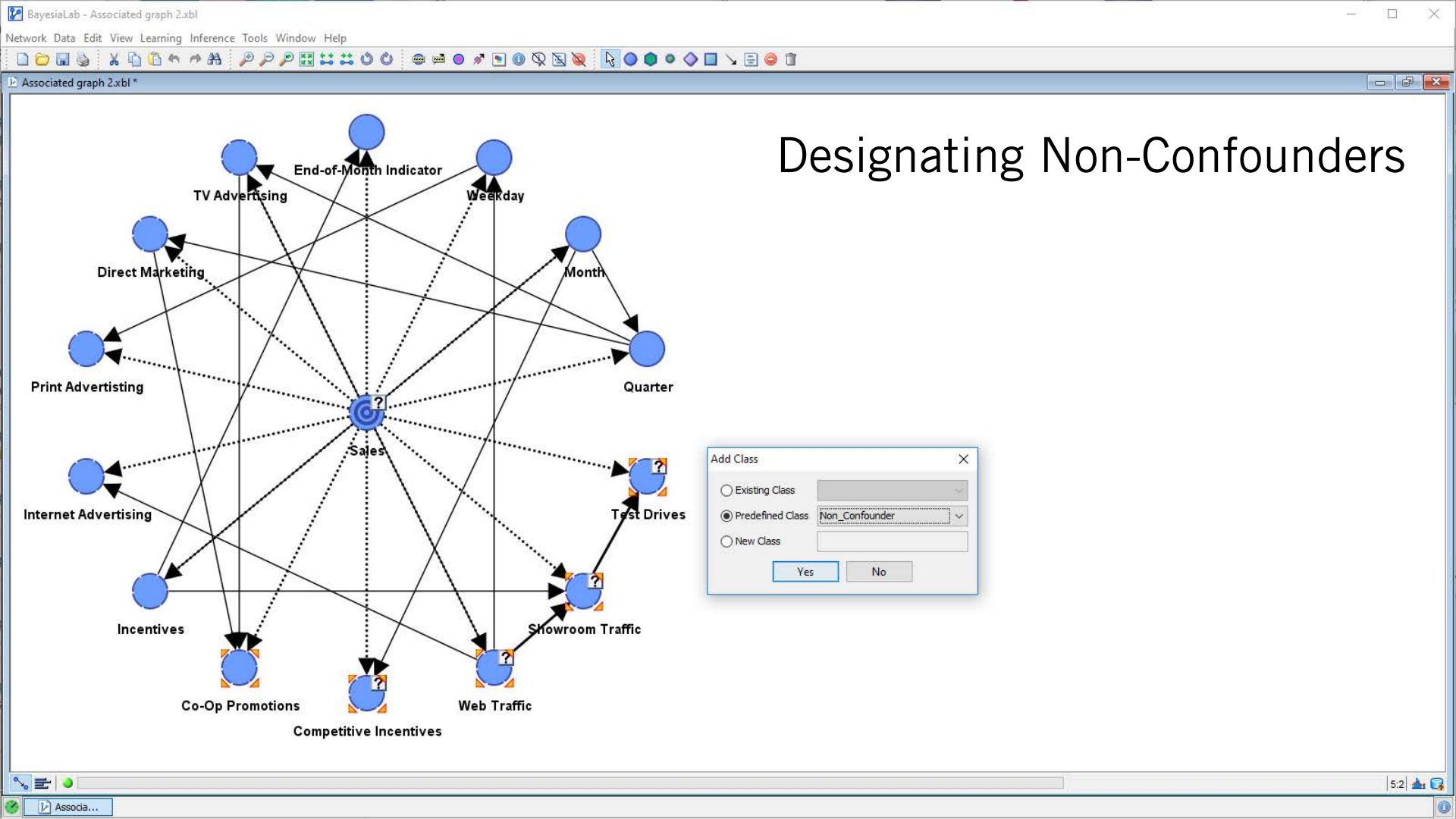


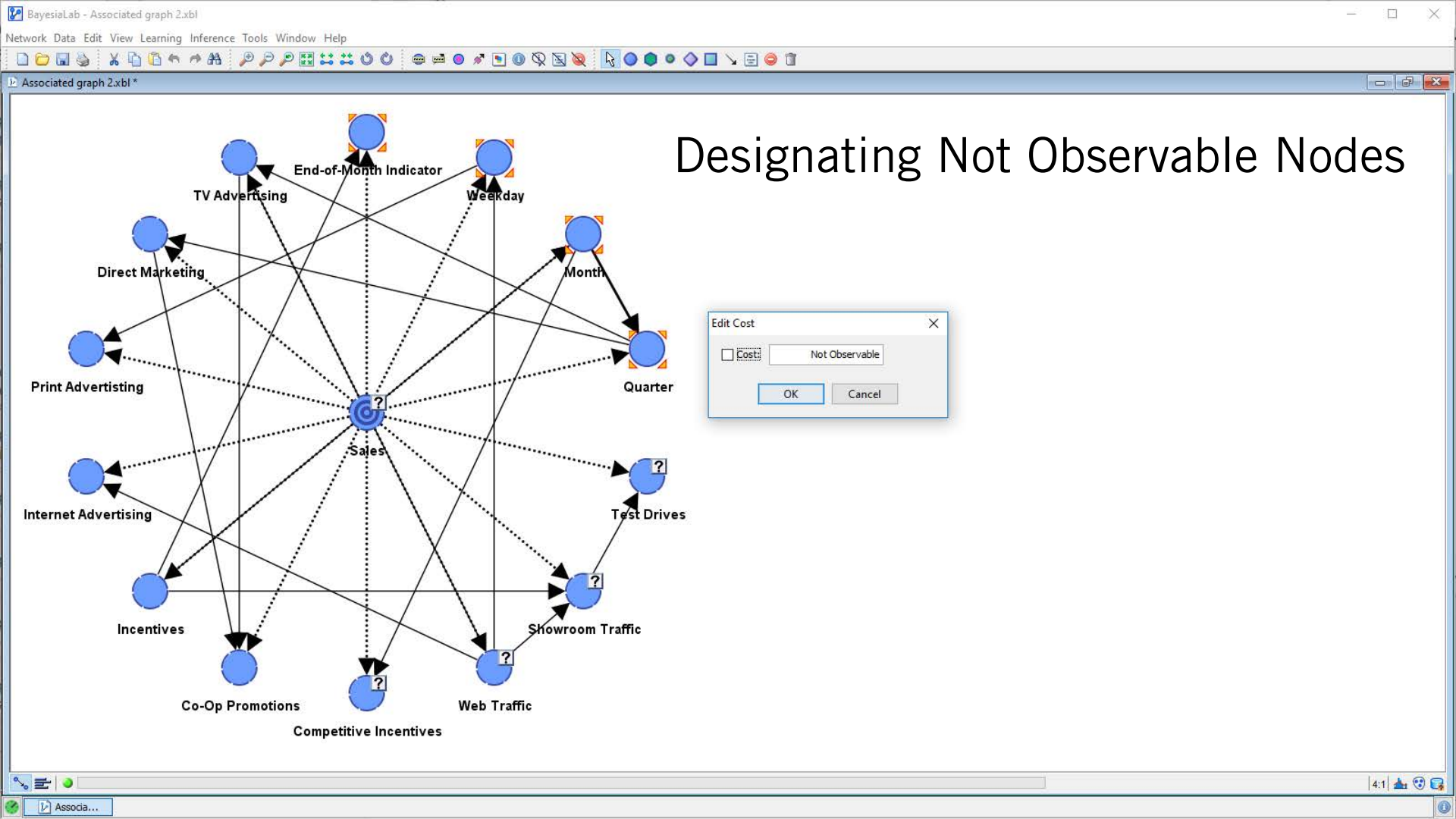




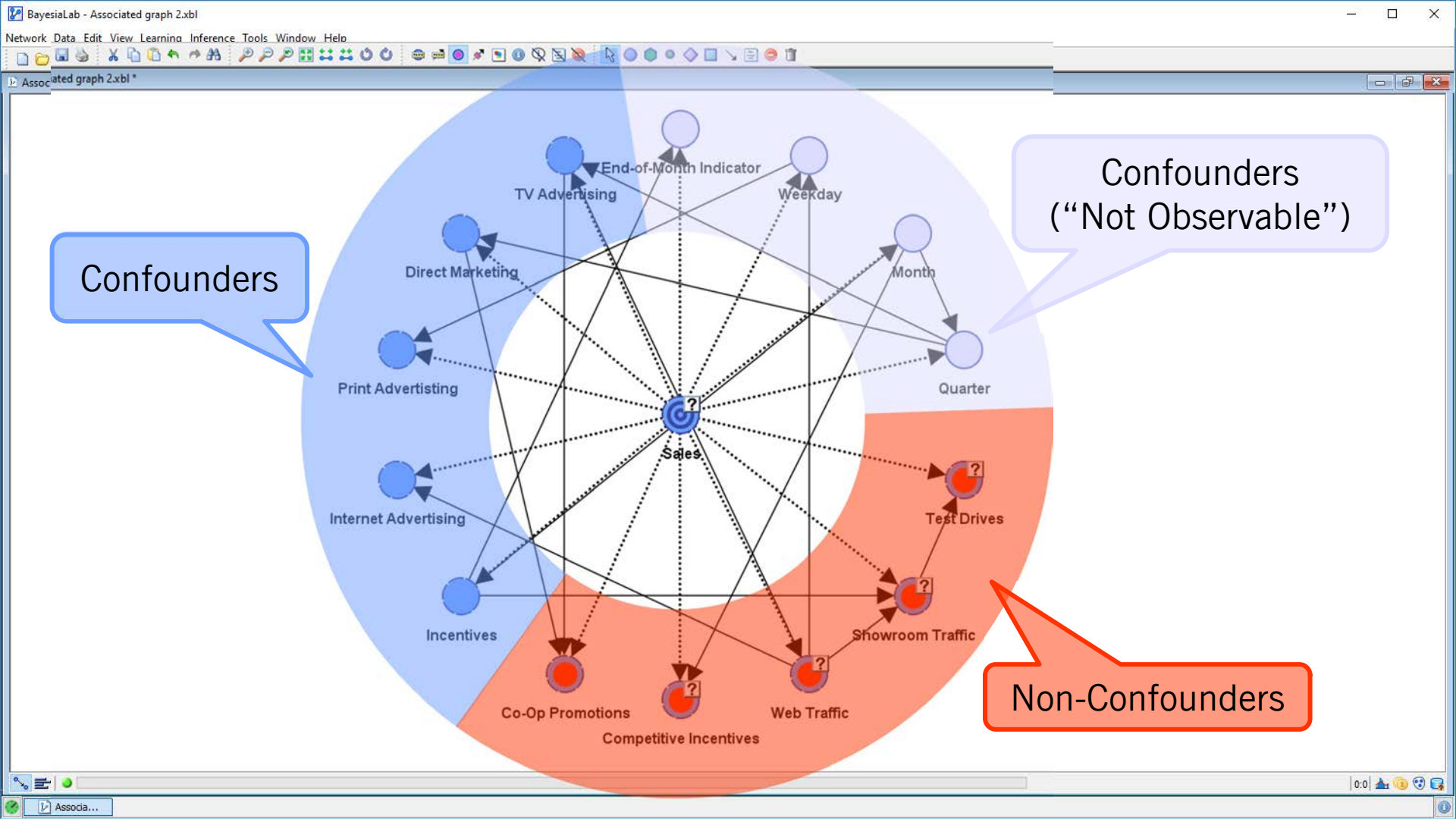


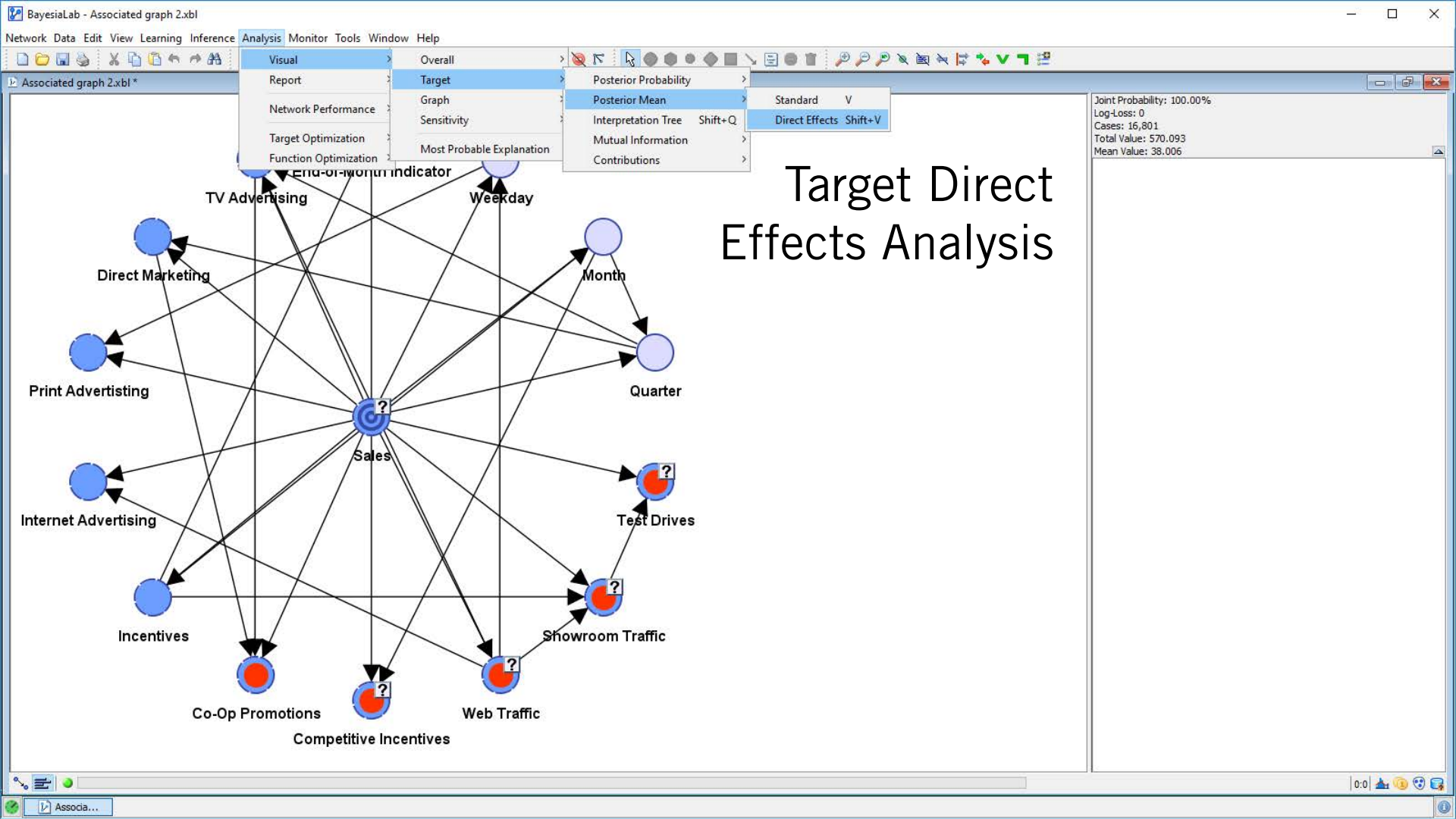


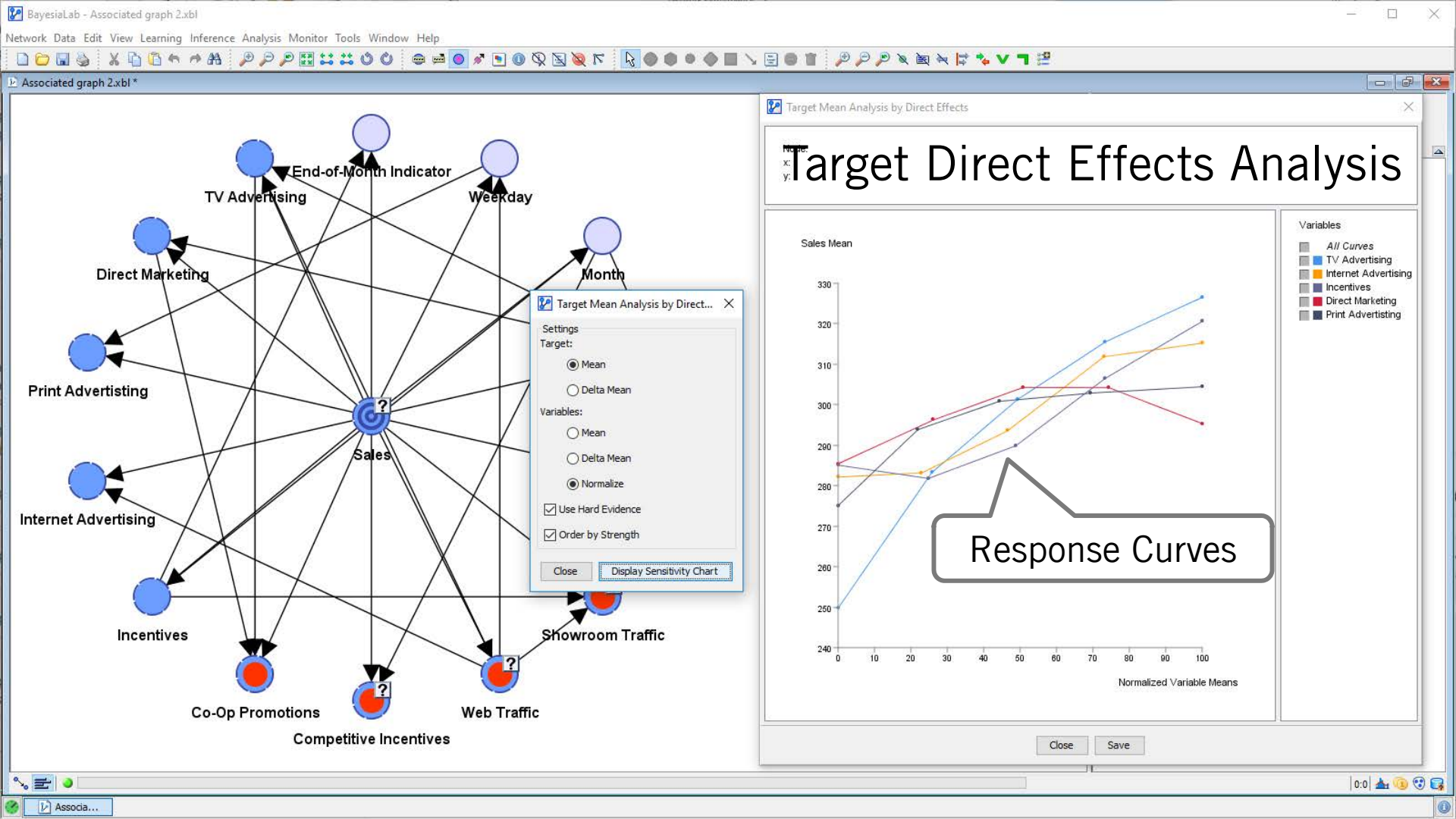






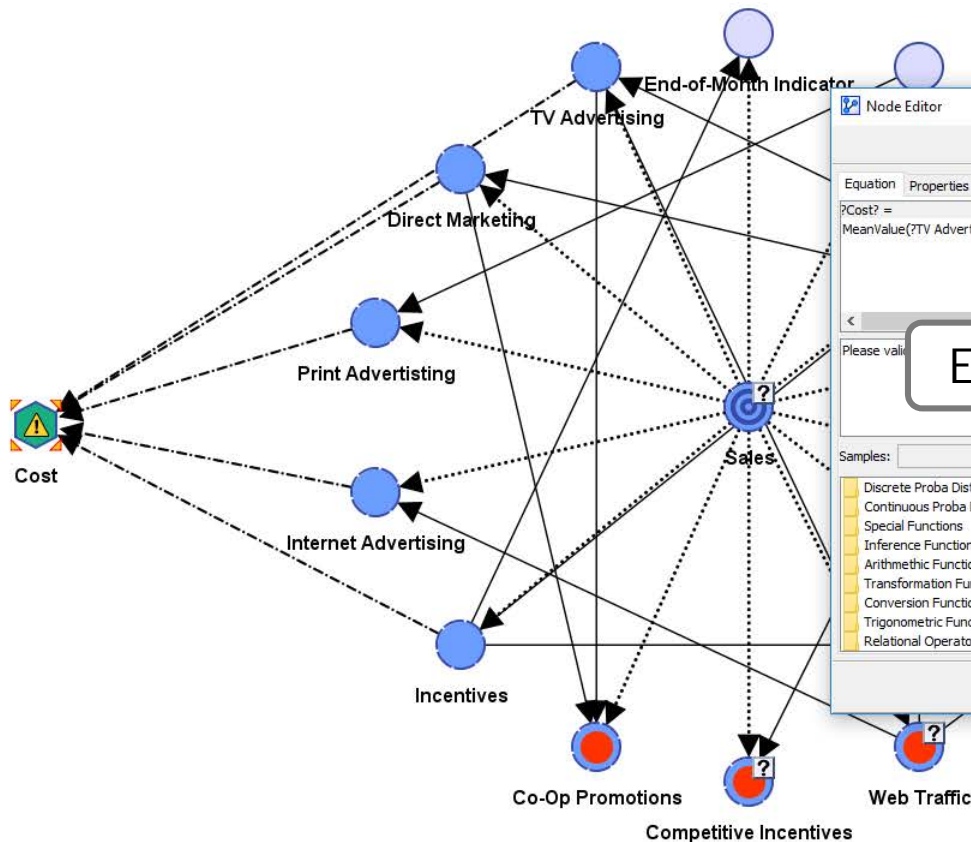








Associated graph 2.xbl \*



# Defining Media Costs

Node Editor

Node Selection: Cost Rename

Equation Properties Classes Comment

?Cost? =  
MeanValue(?TV Advertising?) + MeanValue(?Direct Marketing?) + MeanValue(?Print Advertising?) + MeanValue(?Internet Advertising?) + MeanValue(?Inc

Please validate

Excel-style formula

Samples: 1 ☒ Fixed Seed: 31 Validate

- Discrete Proba Distributions
- Continuous Proba Distributions
- Special Functions
- Inference Functions
- Arithmetic Functions
- Transformation Functions
- Conversion Functions
- Trigonometric Functions
- Relational Operators

- TV Advertising
- Direct Marketing
- Print Advertising
- Internet Advertising
- Incentives

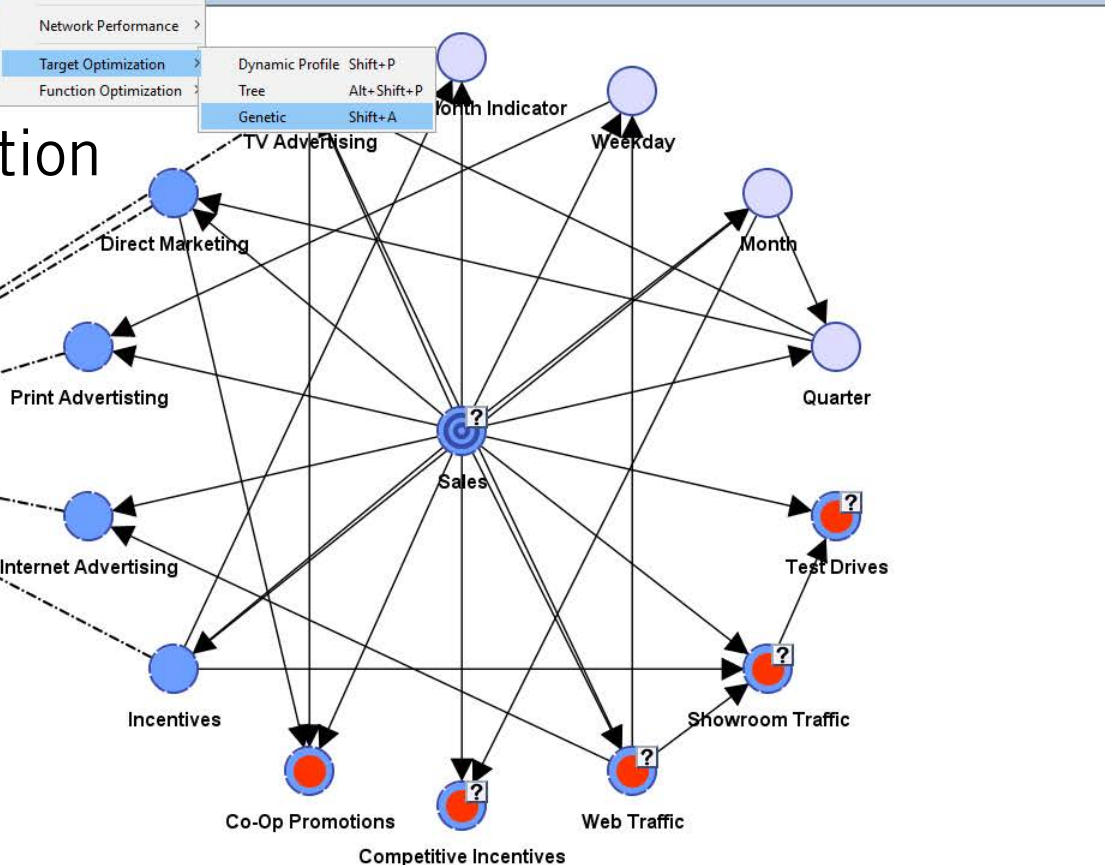
Domain: [0.2759110152971571, 104.231996355]

OK Cancel



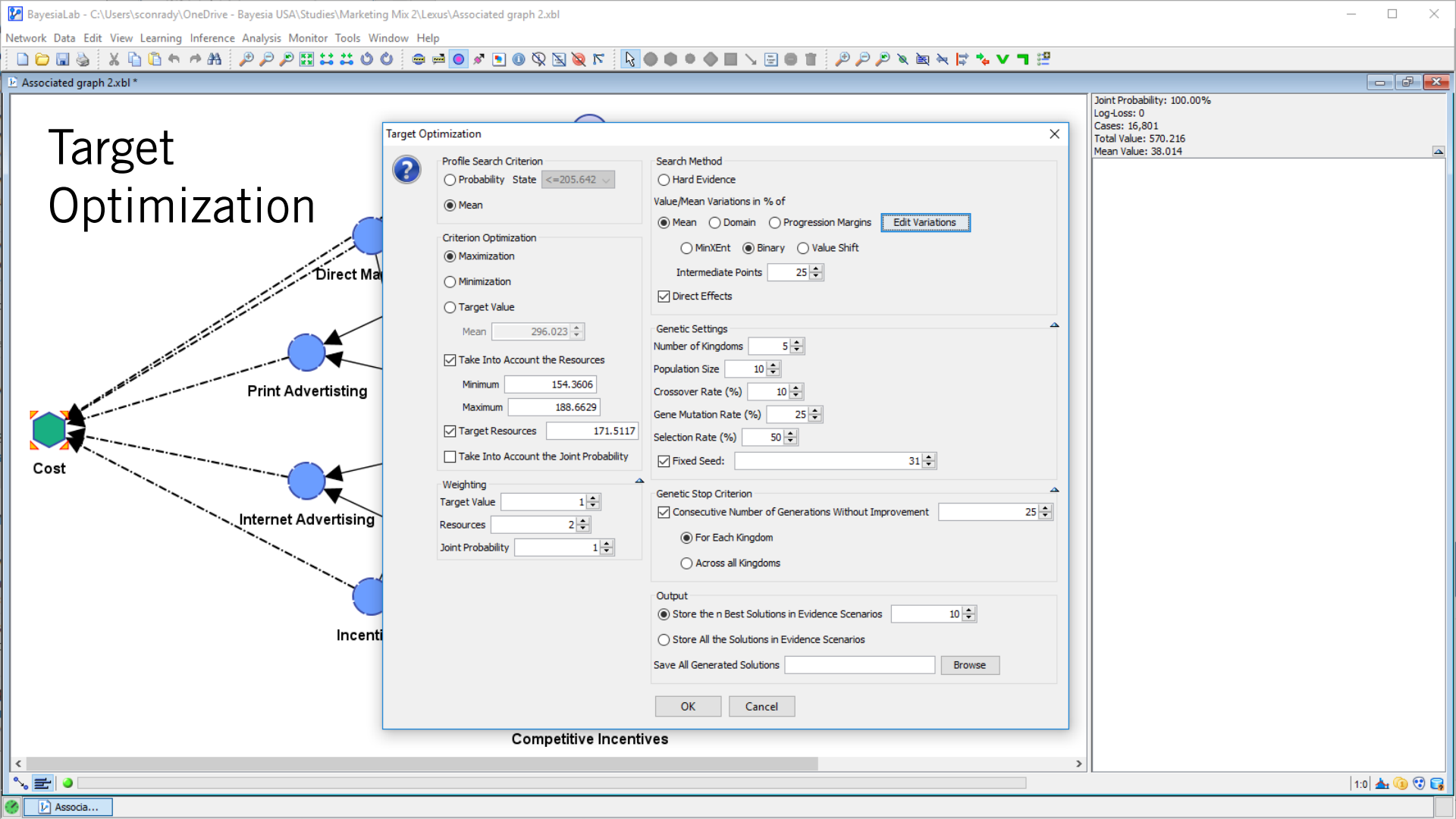
Associated graph 2.xbl

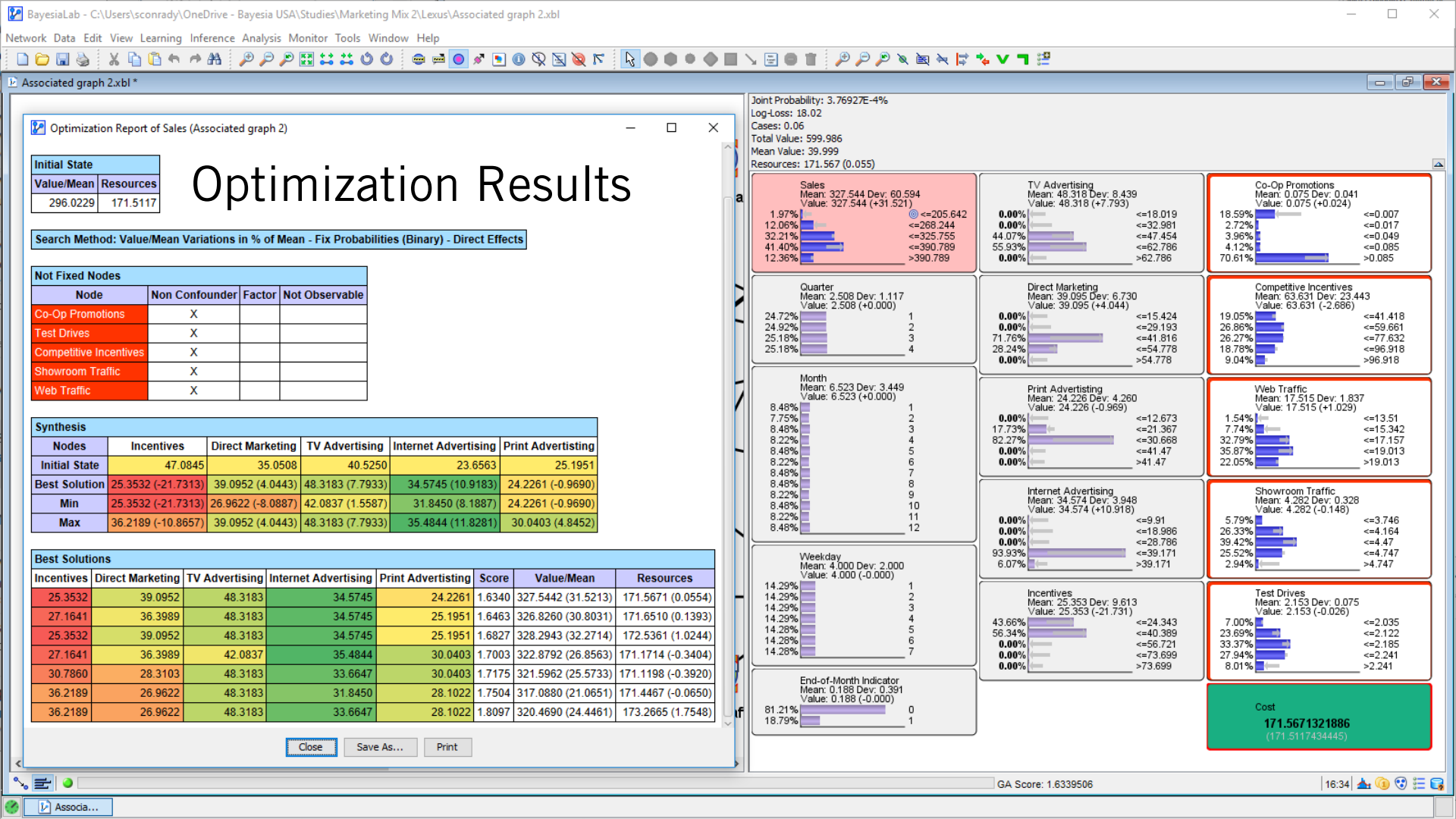
# Target Optimization



Joint Probability: 100.00%  
 Log-Loss: 0  
 Cases: 16,801  
 Total Value: 570.216  
 Mean Value: 38.014







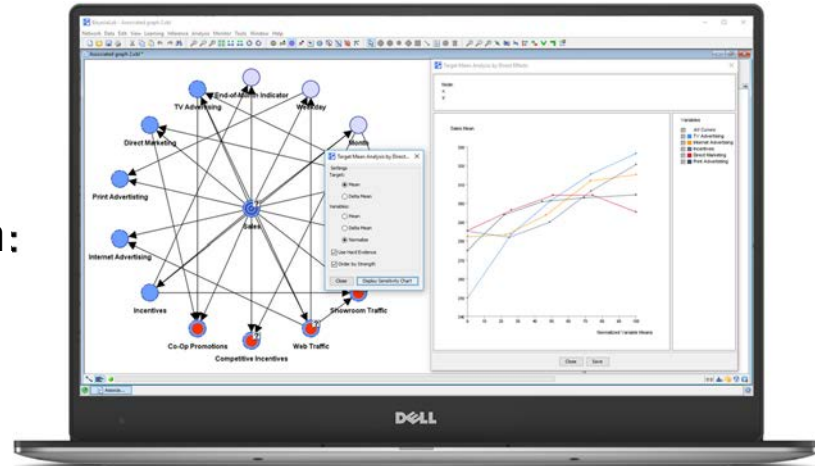


Concluding Remarks

# BayesiaLab Trial

## Try BayesiaLab Today!

- Download Demo Version:  
[www.bayesia.com/trial-download](http://www.bayesia.com/trial-download)
- Apply for Unrestricted Evaluation Version:  
[www.bayesia.com/evaluation](http://www.bayesia.com/evaluation)



# Upcoming Events

## Webinars & Seminars:

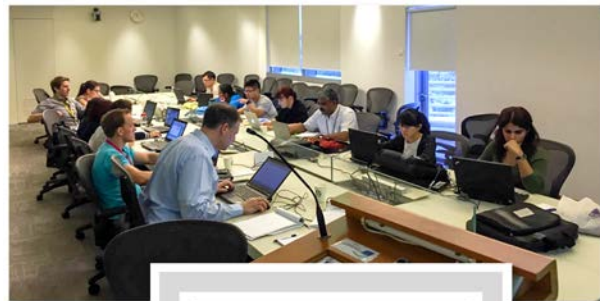
- September 21      Webinar: Adversarial Reasoning
- November 13      Seminar in Arlington, VA  
Artificial Intelligence for Intelligence Analysis
- November 15      Seminar in New York City:  
Health Economics with Bayesian Networks

**Register here: [bayesia.com/events](https://bayesia.com/events)**



# BayesiaLab Courses Around the World in 2018

- October 29–31  
Introductory Course  
Chicago, IL
- November 13–15  
Introductory Course  
McLean, VA (internal)
- November 16–20  
Advanced Course  
McLean, VA (internal)
- December 10–12  
Introductory Course  
Sydney, Australia



Learn More & Register: [bayesia.com/events](https://bayesia.com/events)



# CHICAGO

6TH ANNUAL

**BAYESIALAB CONFERENCE | 2018**

# Thank You!



[stefan.conrady@bayesia.us](mailto:stefan.conrady@bayesia.us)



[BayesianNetwork](#)



[linkedin.com/in/stefanconrady](https://www.linkedin.com/in/stefanconrady)



[facebook.com/bayesia](https://www.facebook.com/bayesia)